

















## The collective regime



Hochberg et al. [2018]

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## DM does not interact with just one electron.

Response described by complex dielectric function,

$$\boldsymbol{\epsilon}(\mathbf{q}, \boldsymbol{\omega}) = \frac{V_{\text{applied}}}{V_{\text{applied}} + V_{\text{induced}}}$$

 $\begin{cases} \mathbf{q} = \text{momentum transfer} \\ \boldsymbol{\omega} = \text{deposited energy} \end{cases}$ 

$$\Gamma = \int \frac{\mathrm{d}^{3}\mathbf{q}}{(2\pi)^{3}} |V(q)|^{2} \left[ 2\frac{q^{2}}{e^{2}} \operatorname{Im}\left(-\frac{1}{\epsilon(\mathbf{q},\omega_{\mathbf{q}})}\right) \right]$$
"Loss function" W

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Hochberg+ & BVL 2101.08263; Boyd+ & BVL 2212.04505





#### 1. Data-driven detector design

Materials physics for sensitive experiments



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Materials physics for sensitive experiments

#### 2. Leveraging detector geometry

Thin-layer enhancement in a real detector



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Materials physics for sensitive experiments

#### 2. Leveraging detector geometry

Thin-layer enhancement in a real detector

#### 3. Recovering nuclear recoils

Electron recoil detectors do double-duty

## [1/3] Data-driven material selection

Sinéad M. Griffin, Yonit Hochberg, **BVL,** Rotem Ovadia, Bethany A. Suter, Ruo Xi Yang

2409.xxxxx

## Super-broad material exploration

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## **The Materials Project**

Harnessing the power of supercomputing and state-of-the-art methods, the Materials Project provides open web-based access to computed information on known and predicted materials as well as powerful analysis tools to inspire and design novel materials.

## Super-broad material exploration

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## $\left. \stackrel{\leftrightarrow}{\epsilon} \right|_{q=0}$ via DFT for **1,019 materials** (out of 154,718!)

## Recovering $\epsilon(q > 0)$

Materials Project only computes  $\overleftarrow{\epsilon}_{q=0}$ 

## Recovering $\epsilon(q > 0)$



Locate features in  $\operatorname{Re}(\epsilon)$  and fit analytical Lindhard functions

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Locate features in  $\operatorname{Re}(\epsilon)$  and fit analytical Lindhard functions

$$\epsilon_{\rm fit}(\mathbf{q},\omega) = \frac{1}{\sum_k h_k} \sum_{k=1}^{n_{\rm peaks}} h_k \epsilon_{\rm L}(\omega_{{\rm p},k},\Gamma_{{\rm p},k},E;\mathbf{q},\omega)$$

#### Three most sensitive materials per half-decade



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#### Three most sensitive materials per half-decade



Now evaluating these new materials for use

# [2/3] Extra sensitivity from detector geometry

Laura Baudis, Alexander Bismark, Noah Brugger, Chiara Capelli, Ilya Charaev, Jose Cuenca, Guy Daniel Hadas, Yonit Hochberg, Benjamin Kilminster, **BVL**, Severin Nägeli, Titus Neupert, Bjoern Penning, Diego Ramirez, Andreas Schilling (QROCODILE collaboration)

2410.xxxxx

(See also: Lasenby & Prabhu 2110.01587, Hochberg+ & BVL 2110.01586)



8



8



8



#### Real detectors: SNSPDs

Superconducting Nanowire Single-Photon Detector

#### Superconducting Nanowire Single-Photon Detector



Thin-layer geometry

9 Hochberg+ & **BVL** 2110.01586

Quantum Resolution-Optimized Cryogenic Observatory for Dark matter Incident at Low Energy

Next-generation SNSPD demonstrator (11 µm threshold)



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Quantum Resolution-Optimized Cryogenic Observatory for Dark matter Incident at Low Energy

Next-generation SNSPD demonstrator (11 µm threshold)

- Geometry matters for  $q \leq 1/(2 \text{ nm}) \approx 100 \text{ eV}$
- $\implies$  nontrivial effect for  $m_{\rm DM} \lesssim 100 \, \rm keV$



## Geometric enhancement



#### QROCODILE & BVL 2410.xxxxx

## [3/3] *Nuclear* recoils in electronic detectors

Sinéad M. Griffin, Guy Daniel Hadas, Yonit Hochberg, Katherine Inzani, BVL

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## Nature of the excitations

"Broken Cooper pairs"

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#### "Broken Cooper pairs"





Below  $T_C$ , transition to superconducting vacuum  $|0_{BCS}\rangle$ , with a condensate of Cooper pairs:  $\langle c_{-\mathbf{k}\downarrow}c_{\mathbf{k}\uparrow}\rangle \neq 0$ .

$$c_{-k\downarrow}$$
 (phonons)  $e^{-}$   $c_{k\uparrow}$ 

Below  $T_C$ , transition to superconducting vacuum  $|0_{BCS}\rangle$ , with a condensate of Cooper pairs:  $\langle c_{-\mathbf{k}\downarrow}c_{\mathbf{k}\uparrow}\rangle \neq 0$ .

$$\mathcal{H} = \sum_{\mathbf{k}\sigma} \xi_{\mathbf{k}} c_{\mathbf{k}\sigma}^* c_{\mathbf{k}\sigma} + \sum_{\mathbf{k}\ell} V_{\mathbf{k}\ell} \left( c_{\mathbf{k}\uparrow}^* c_{-\mathbf{k}\downarrow}^* b_{\ell} + b_{\mathbf{k}}^* c_{-\ell\downarrow} c_{\ell\uparrow} - b_{\mathbf{k}}^* b_{\ell} \right)$$

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Diagonalize  $\mathcal{H}$  with 
$$\begin{cases} c_{\mathbf{k}\uparrow} = u_{\mathbf{k}}^* \gamma_{\mathbf{k}0} + v_{\mathbf{k}} \gamma_{\mathbf{k}1} \\ c_{-\mathbf{k}\downarrow}^* = -v_{\mathbf{k}}^* \gamma_{\mathbf{k}0} + u_{\mathbf{k}} \gamma_{\mathbf{k}1}^* \end{cases}$$

Below  $T_{\rm C}$ , transition to superconducting vacuum  $|0_{\rm BCS}\rangle$ , with a condensate of Cooper pairs:  $\langle c_{-\mathbf{k}|} c_{\mathbf{k}\uparrow} \rangle \neq 0$ .

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"Electron recoils":  $|\chi\rangle|0_{BCS}\rangle \longrightarrow |\chi\rangle|QP_1, QP_2\rangle$ 

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Final state is insensitive to initial excitation type

#### New constraints on scattering



Griffin+ & **BVL** 2409.xxxxx

#### New constraints on scattering





#### Data-driven material discovery



Data-driven material discovery





Geometric enhancement



Data-driven material discovery





Geometric enhancement



Nuclear recoils in superconductors

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