

# Proton-air interactions at ultra-high-energies in muon-depleted air showers with different depths

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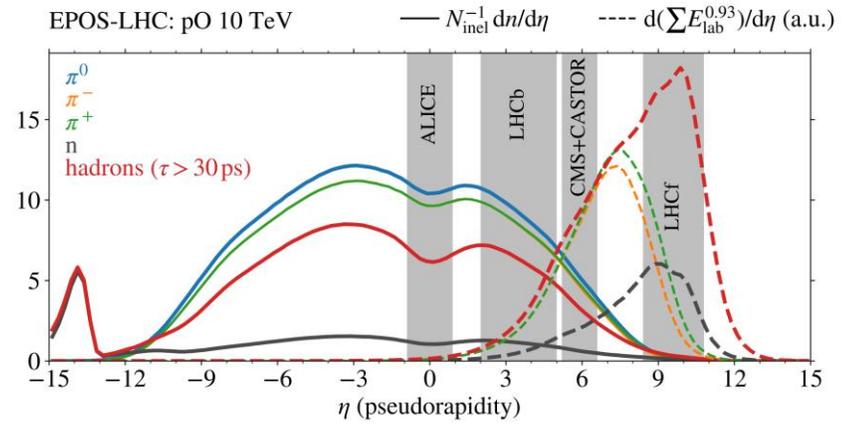
Fundación "la Caixa"

# Motivation

- Ultra-high energy cosmic rays ( $E_0 > 100 \text{ PeV}$ ) measured through extensive air showers  $\Rightarrow$  opportunity to probe hadronic interactions at center-of-mass energies and rapidity regions not covered by human-made accelerators.

## A degenerate problem:

- Unknown mass composition at highest energies;
- Lack of accelerator data in relevant kinematic phase space regions of CR-air interaction  $\Rightarrow$  hamper interpretation of mass composition.

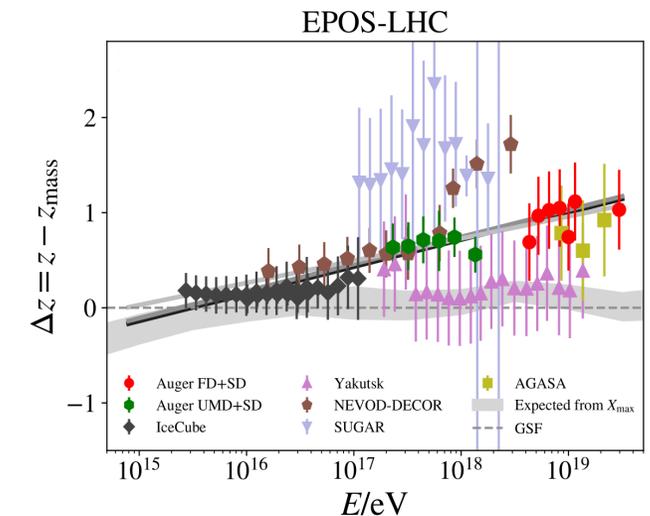


[Astrophys Space Sci 367, 27 \(2022\)](#)

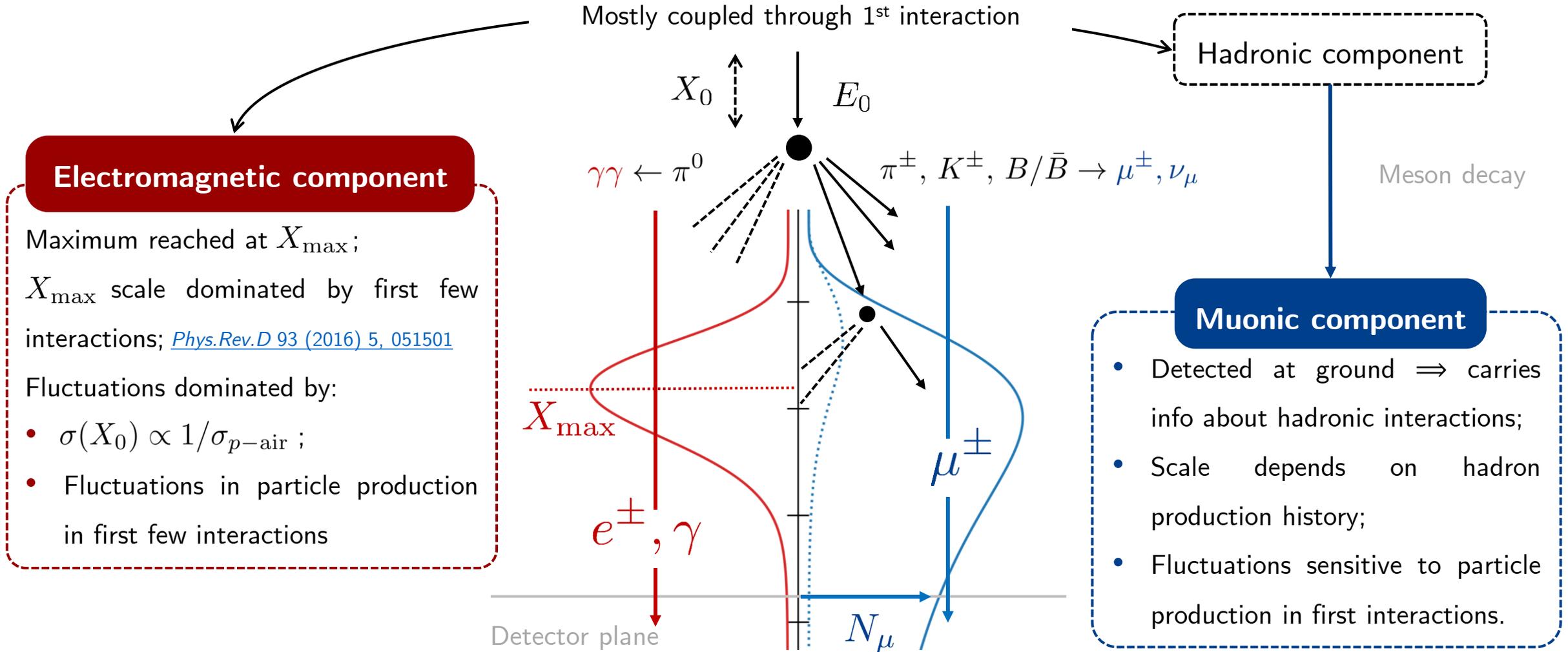
## A few current issues with air shower simulations:

- Muon puzzle: underestimation of muon scale in air shower simulations given mass composition from  $X_{\text{max}}$  (but fluctuations compatible!)
- Inconsistent description of electromagnetic and muonic components of EAS

Use full distributions of shower observables to probe particle production in model independent way from data!



# Cascade physics for fixed primary composition

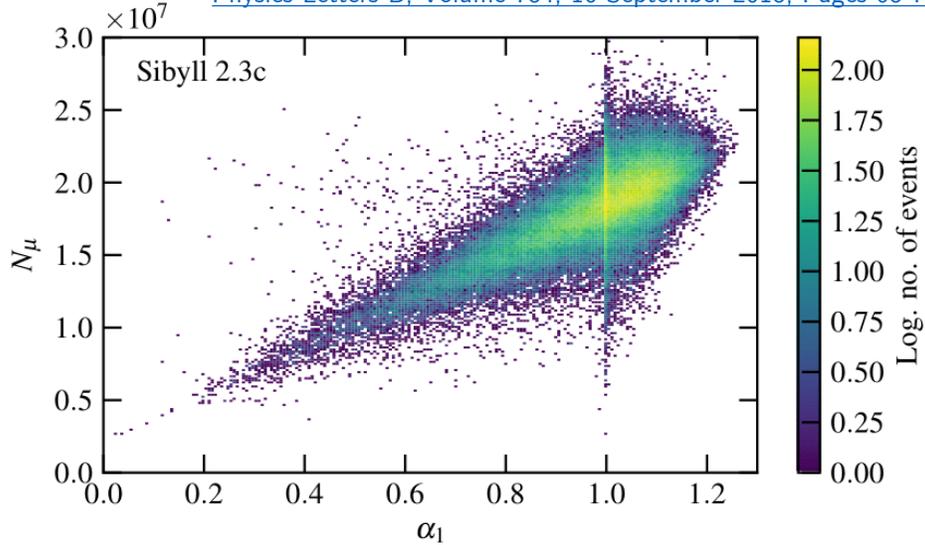


[Physics Letters B, Volume 784, 10 September 2018, Pages 68-76](#)

- Shower-to-shower distributions of  $X_{\max}$  and  $N_\mu$  sensitive to particle production at the highest energies.

# Hadronic physics from tail of distribution of $N_\mu$

Physics Letters B, Volume 784, 10 September 2018, Pages 68-76

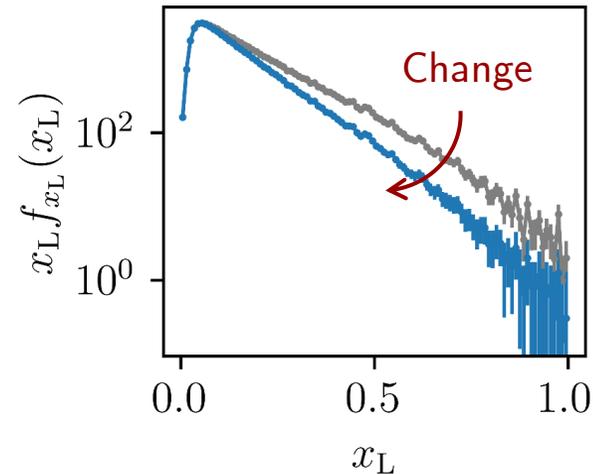


- $N_\mu$  highly correlated with fraction of primary energy in hadronic sector of the 1<sup>st</sup> CR-air interaction  $\alpha_1$ ;
- $\sigma(N_\mu)/N_\mu \simeq \sigma(\alpha_1)/\alpha_1$ ;
- Shape of distribution of  $N_\mu$  sensitive to hardness of energy spectrum of hadrons of 1<sup>st</sup> CR air interaction;

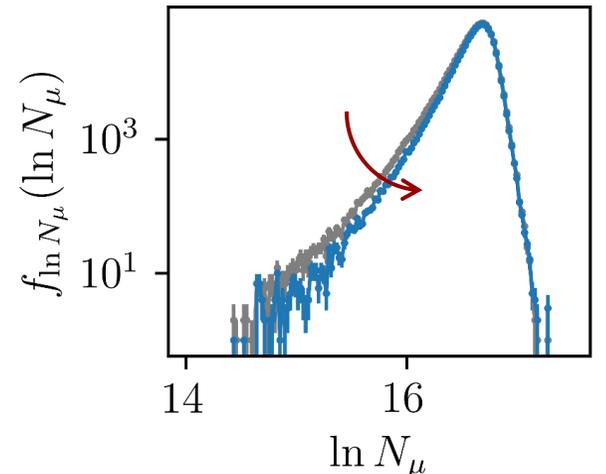
$$\alpha_1 = \sum_{\text{hadrons } i} \left( \frac{E_{\text{had } i}}{E_0} \right)^\beta$$

- Softer energy spectrum of  $\pi^0$  of 1<sup>st</sup> p-air interaction  $\Rightarrow$  steeper tail of  $N_\mu \Rightarrow$  probe production cross-section of  $\pi^0$  in p-air interactions above LHC through measurement of tail of distribution of  $N_\mu$

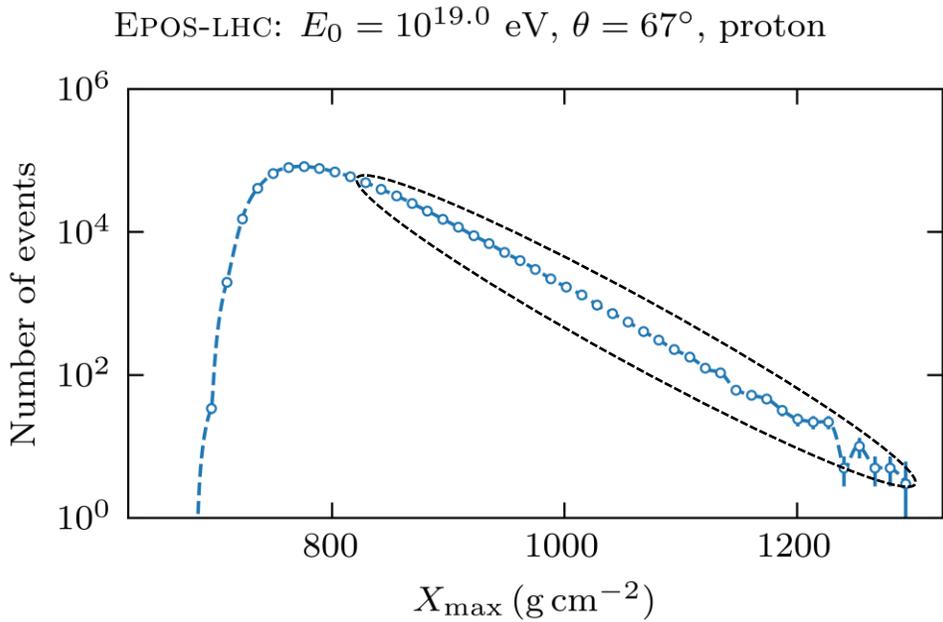
Energy spectrum of  $\pi^0$  of 1<sup>st</sup> p-air int.



[Phys.Rev.D 103 \(2021\) 2, 022001](https://arxiv.org/abs/2008.02201)



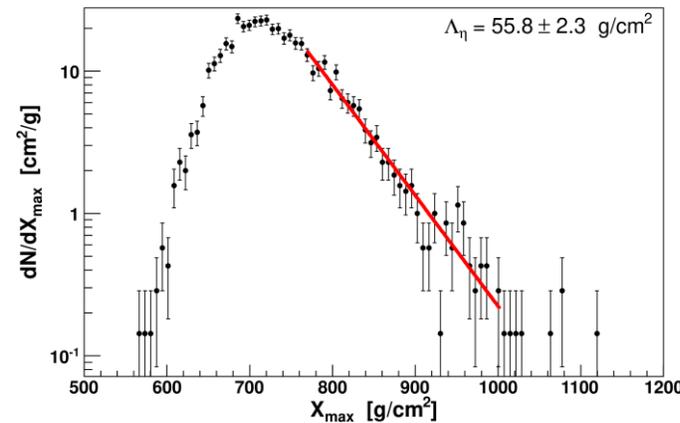
# Hadronic physics from tail of distribution of $X_{\max}$



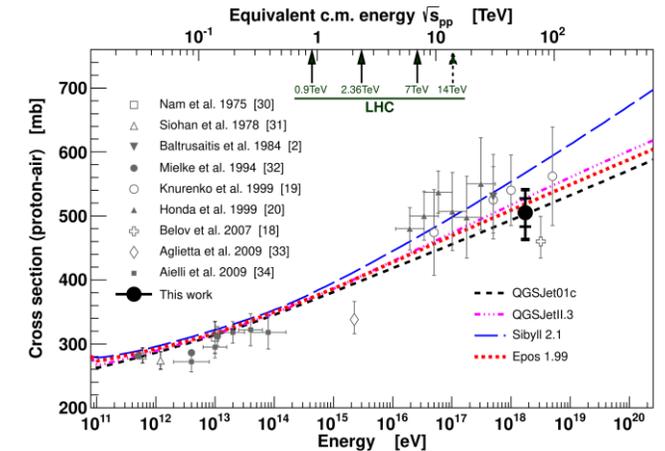
- Exponential tail from exponential distribution of depths of first interaction:

$$X_0 \sim \exp\left(-\frac{X_0}{\lambda_{p-\text{air}}}\right) \text{ with } \lambda_{p-\text{air}} \propto 1/\sigma_{p-\text{air}}$$

- Measurement of p-air cross-section with Auger at  $\sqrt{s} > 57$  TeV:



[Phys. Rev. Lett. 109, 062002](#)



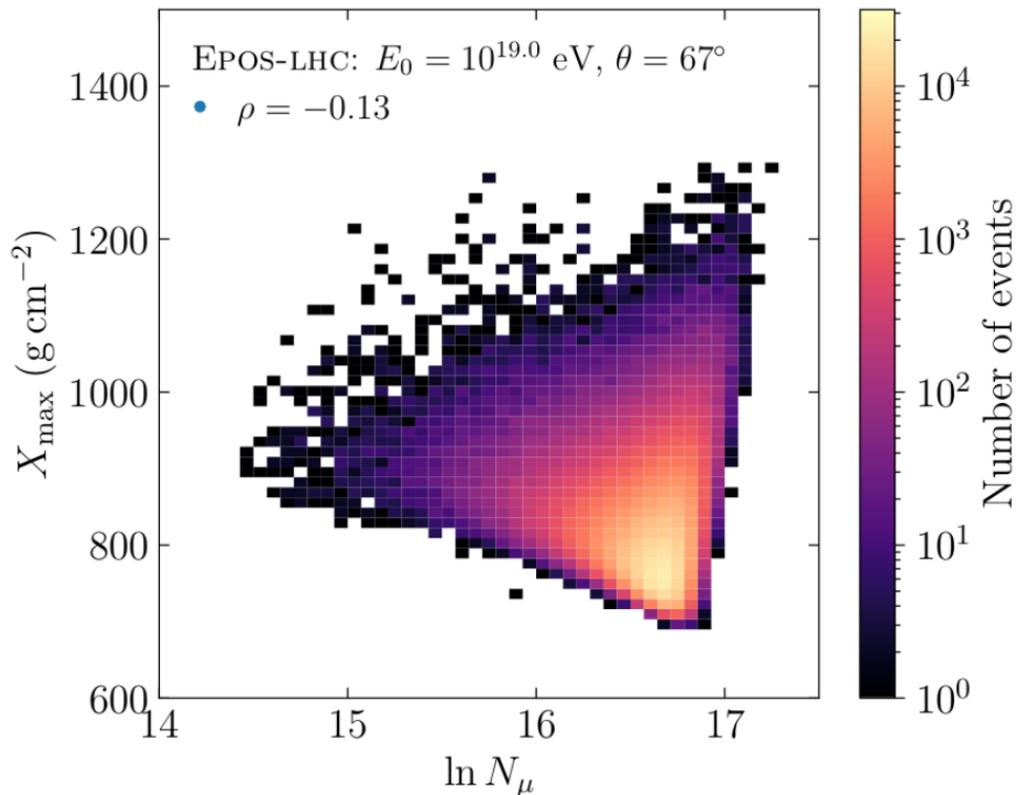
- Remaining fluctuations from fluctuations of  $\Delta X_{\max} = X_{\max} - X_0 \Rightarrow$  dominated by fluctuations in particle production in the highest energy interactions  $\Rightarrow$  possibility to probe such interactions above LHC energies.

# Hadronic physics from the $\ln N_\mu - X_{\max}$ plane

Proton primaries  $\Rightarrow$  mild anti-correlation between  $X_{\max}$  and  $N_\mu$  from highest energy interactions.

Anti-correlation decreased by:

- Fluctuations of depth of first interaction  $X_0$  uncorrelated with  $N_\mu$ ;
- Increased muon attenuation in shallower showers  $\Rightarrow$  positive correlation with  $X_{\max}$ ;



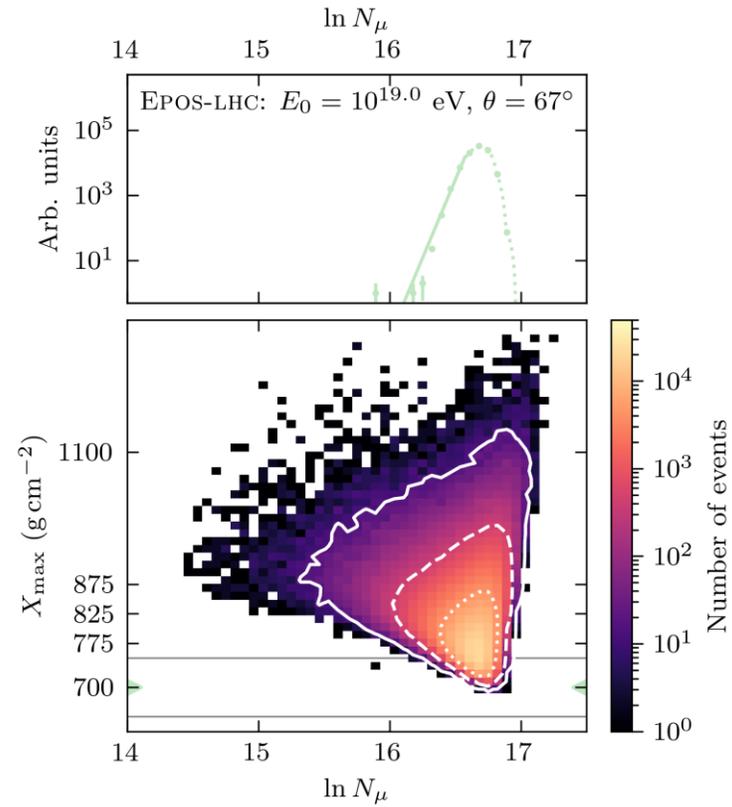
Conex simulations for  
proton primary!

**Objective:**

How much more information about 1<sup>st</sup> p-air interaction  
in joint distribution of  $N_\mu - X_{\max}$ ?

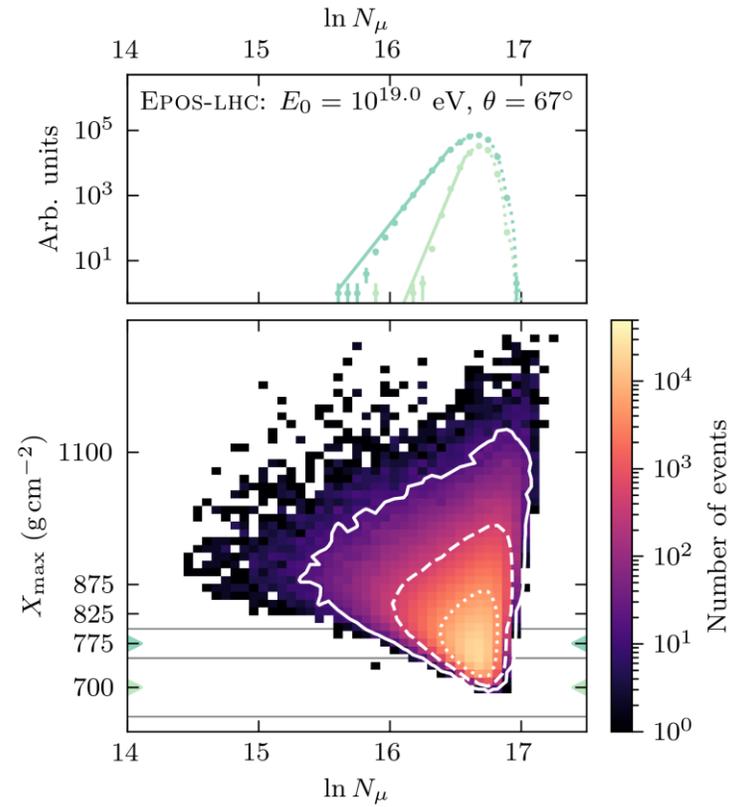
# Tail of muon number distribution as a function of $X_{\max}$

arXiv:2406.08620



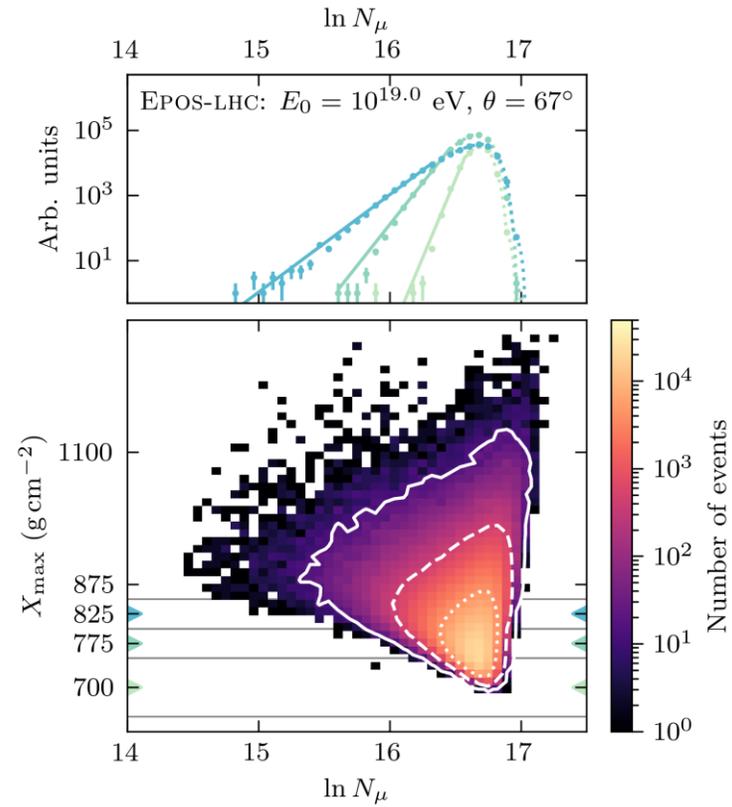
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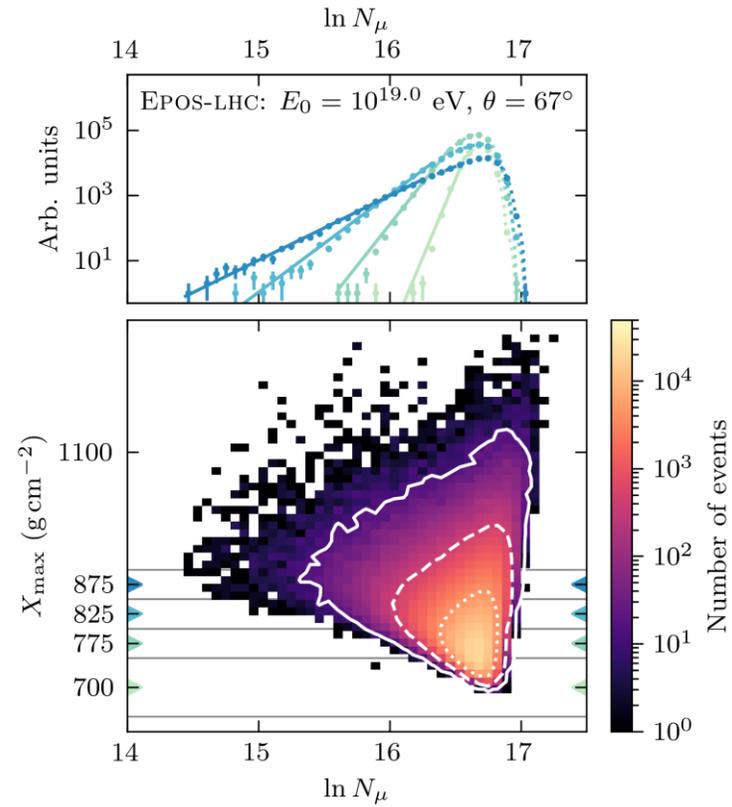


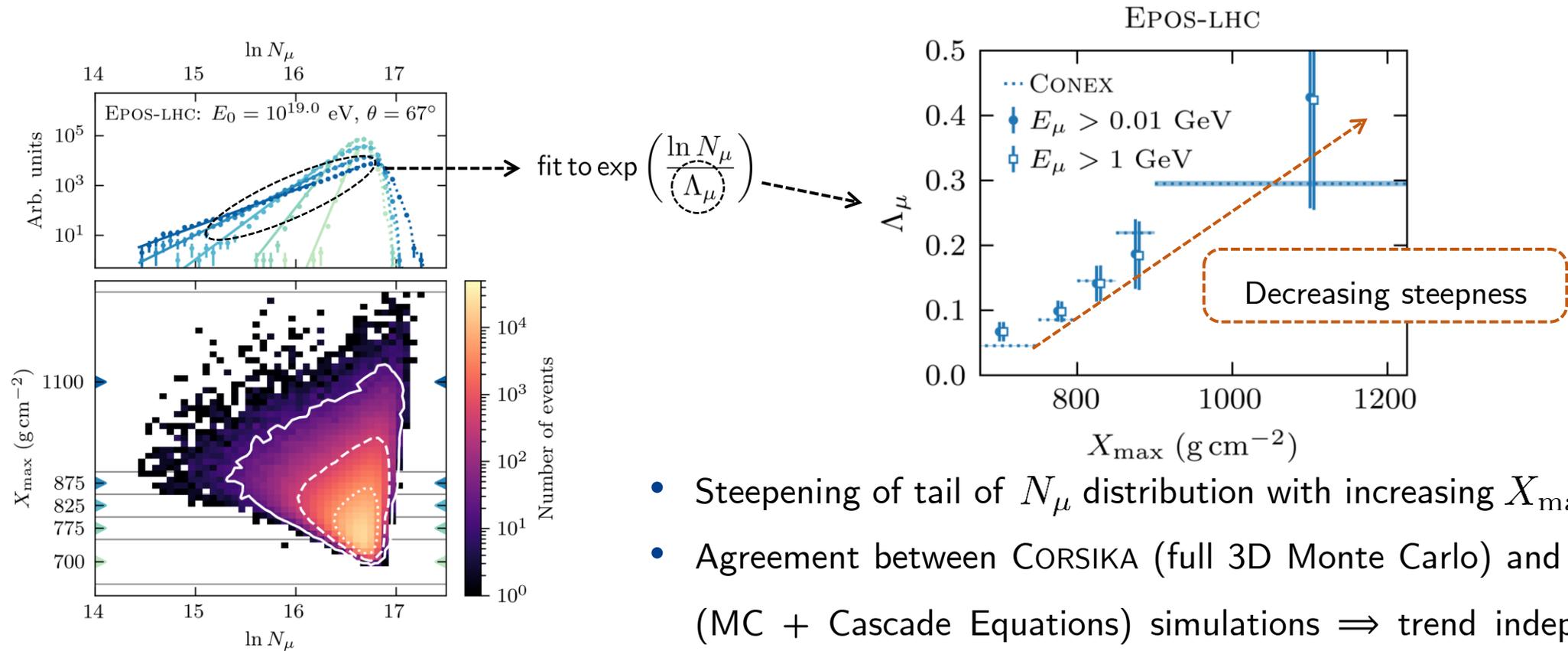
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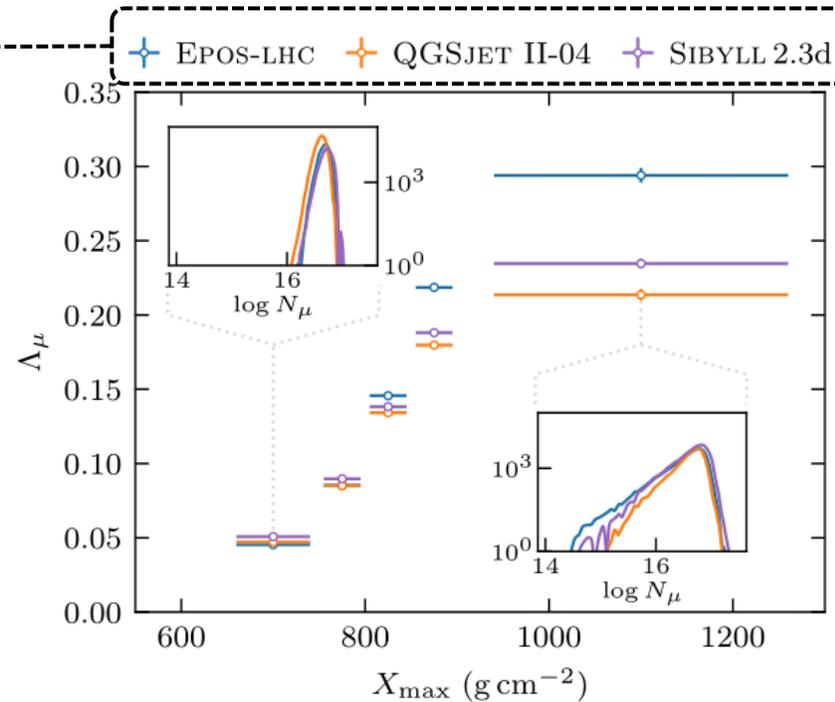


- Steepening of tail of  $N_\mu$  distribution with increasing  $X_{\max}$ ;
- Agreement between CORSIKA (full 3D Monte Carlo) and CONEX (MC + Cascade Equations) simulations  $\Rightarrow$  trend independent of energy threshold of muons.

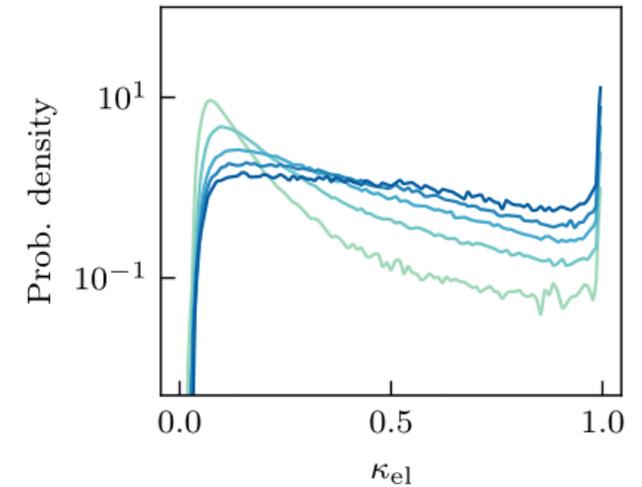
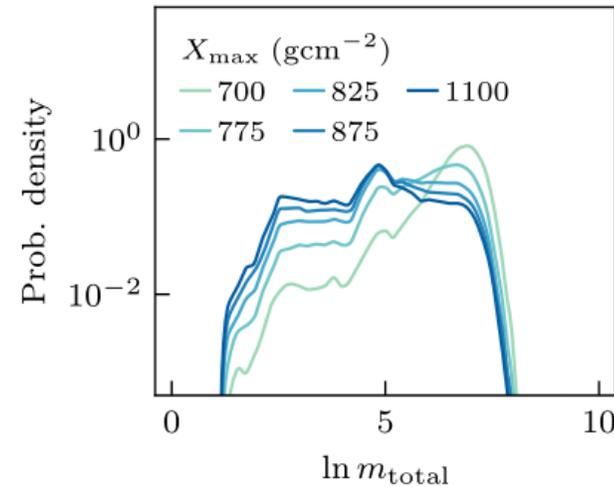
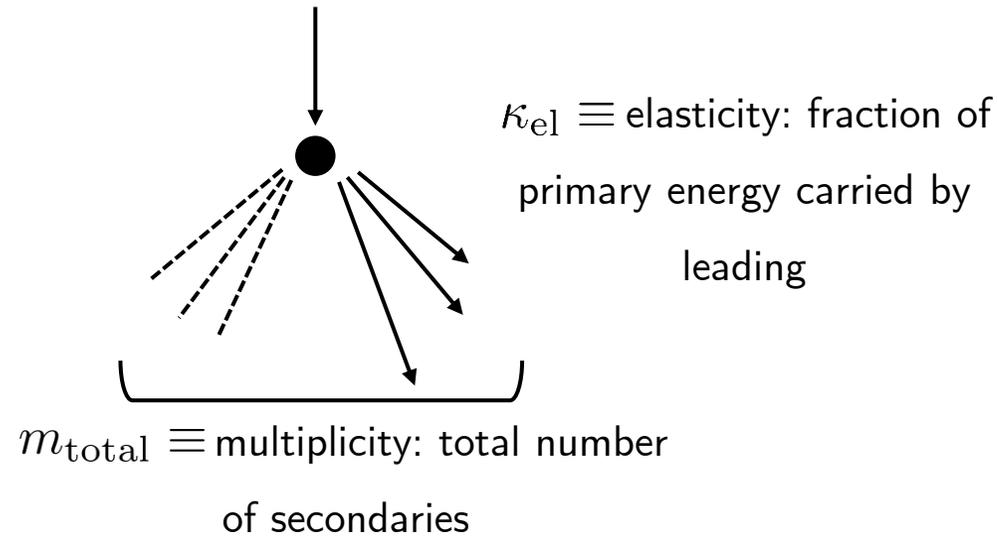
## Take home message

- Measuring evolution of  $\Lambda_\mu$  with  $X_{\max} \Rightarrow$  stronger constraints on particle production in the 1<sup>st</sup> p-air interaction

Different high energy  
hadronic interaction models



- $\Lambda_\mu$  evolution with  $X_{\max}$  is model dependent;
- Shallow showers: hadronic interaction model predictions are universal (< 10 % model dependence);
- Deep showers: enhanced model dependence of  $\Lambda_\mu$  reaching 30 %



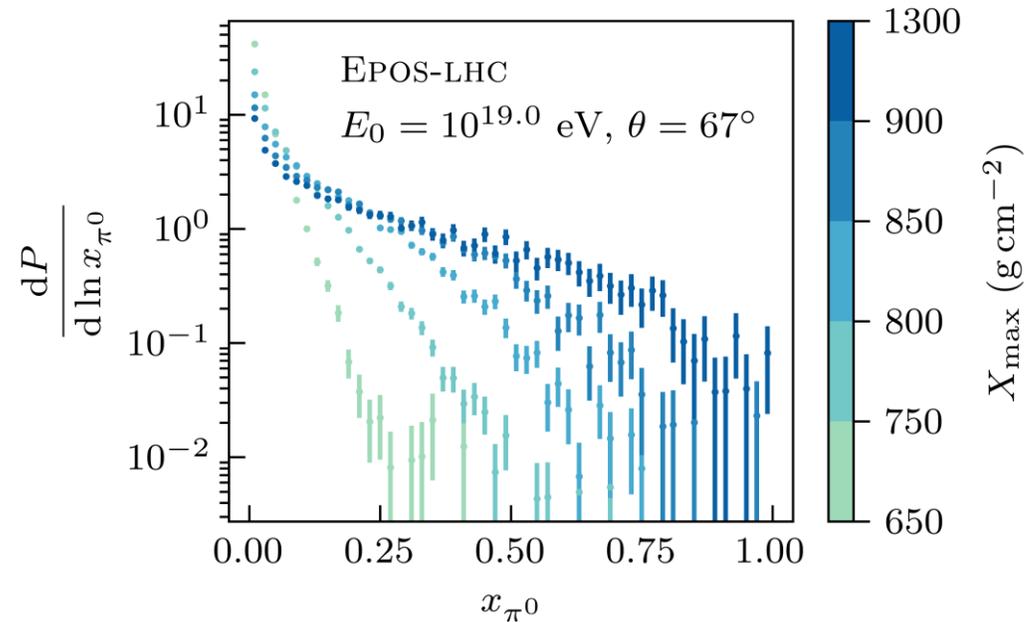
- Shallower showers: tendency for very inelastic 1<sup>st</sup> p-air interaction with high multiplicity (energy more evenly distributed among secondaries)  $\Rightarrow$  more hadronic activity  $\Rightarrow$  more universal tail.
- Deep showers: tendency for lower multiplicity + more elastic events  $\Rightarrow$  less hadronic activity

## Take home messages

- Binning in  $X_{\max} \Rightarrow$  probe continuously the hadronic activity of 1<sup>st</sup> interaction;
- $\Lambda_{\mu}(X_{\max})$  evolution constrains models in different regions of the kinematic phase-space of 1<sup>st</sup> interaction.

# Stronger constraints on neutral pion production cross section

Recall that  $\Lambda_\mu$  probes the hardness of the energy spectrum of neutral pions.



- Deep showers  $\Rightarrow$  events with fast  $\pi^0$  of the 1<sup>st</sup> int. more likely  $\Rightarrow$  less muons  $\Rightarrow$  flattening of the muon tail.

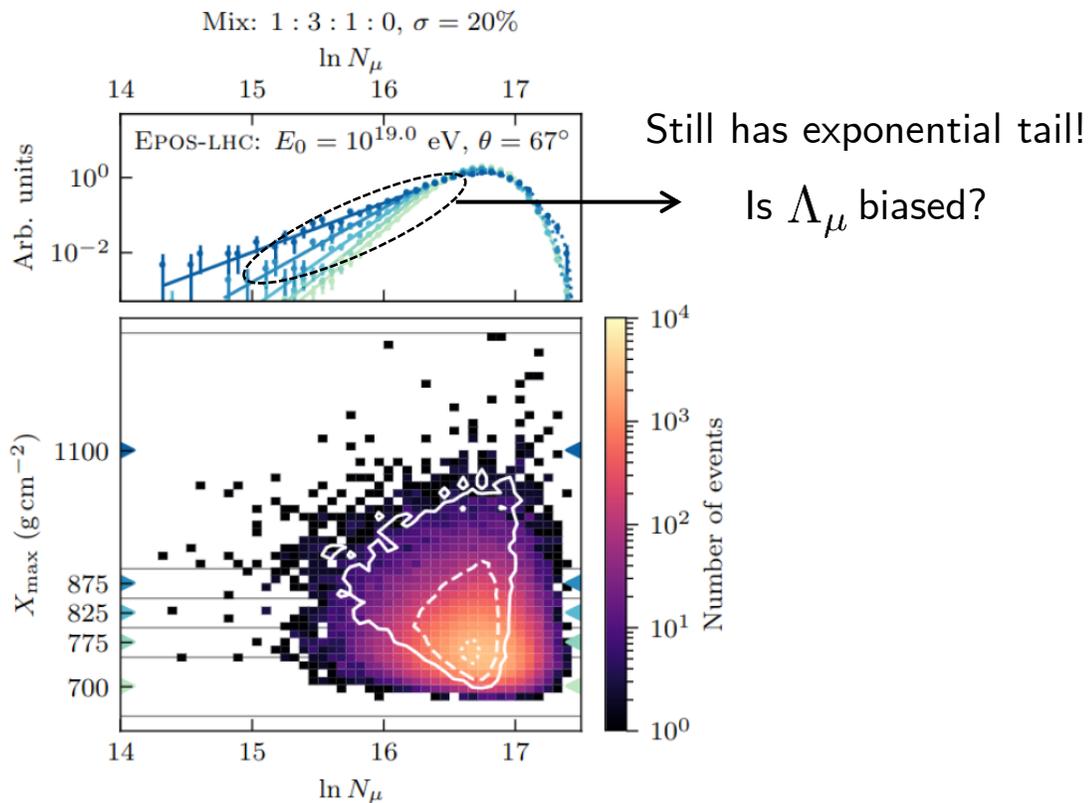
## Take home message:

- Can probe the production cross-section of neutral pions of the 1<sup>st</sup> p-air collision as a function of the hadronic activity outside phase-space covered by human-made accelerators!

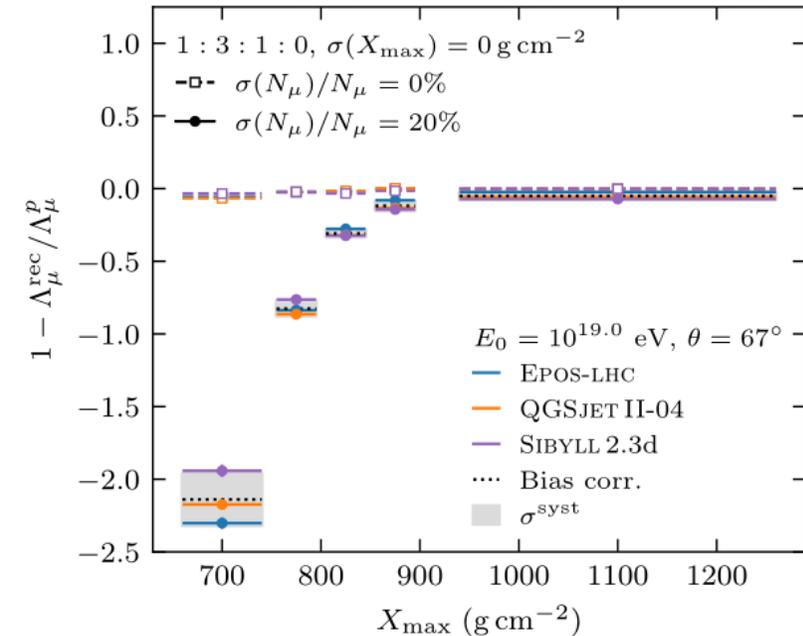
# Feasibility of measurement of $\Lambda_\mu$ : the case of Auger

Is it possible to measure  $\Lambda_\mu(X_{\max})$  with Auger, given:

- Mixed mass composition: p: He : N : Fe?
- Resolution in  $X_{\max}$ ,  $N_\mu$  and  $E_0$ ?

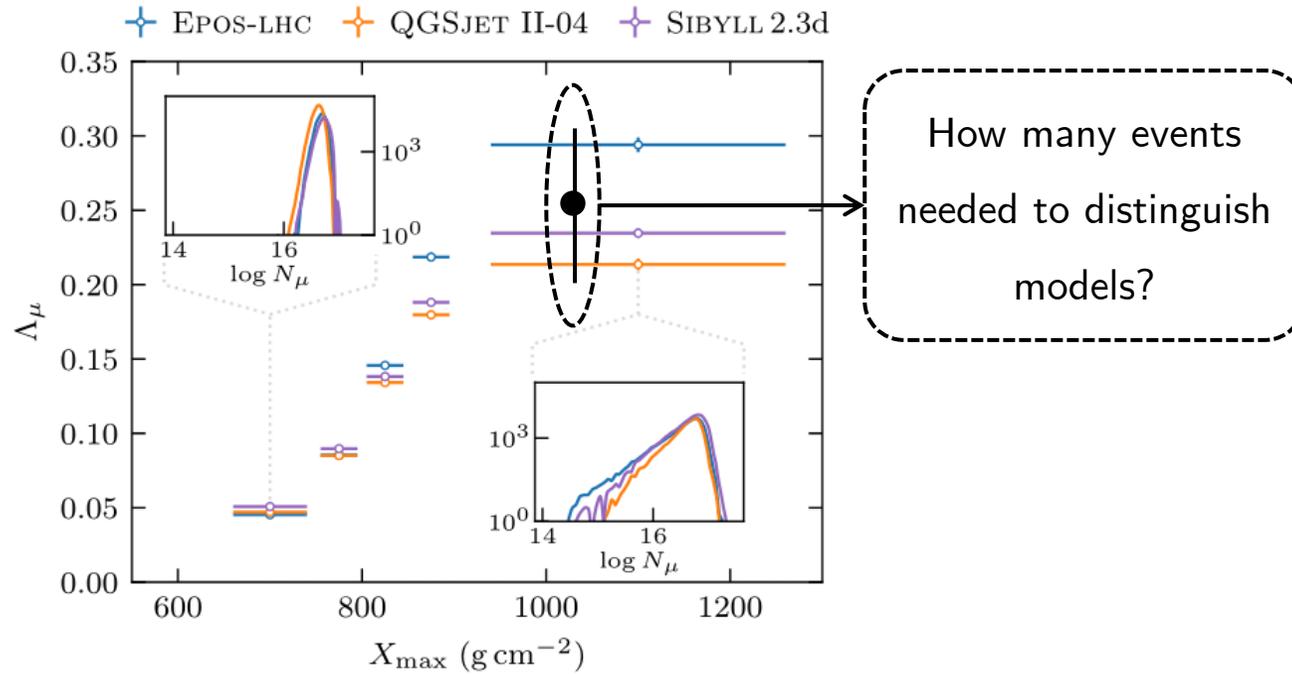


- Proton-rich and proton-poor composition scenarios estimated from Auger data with  $1 < E_0 < 3$  EeV



- Mixed mass comp. does not bias  $\Lambda_\mu$ , BUT resolution in  $N_\mu$  and  $X_{\max}$  does!
- Bias is model dependent  $\Rightarrow$  apply average bias correction and consider model systematic.

# Feasibility of measurement of $\Lambda_\mu$ : needed statistics



**Proton poor:** p :He: N = 1:3:1

$X_{\max}$ bin low edge	$n_{\min} (1 \sigma)$	$n_{\min} (3 \sigma)$
850	3 927	29 015
900	2 835	24 300

**Proton rich:** p :He: N = 7:1:2

$X_{\max}$ bin low edge	$n_{\min} (1 \sigma)$	$n_{\min} (3 \sigma)$
850	4 034	47 640
900	1 556	15 191

- Model distinction at 1 sigma possible with golden hybrids, regardless of the composition;
- AugerPrime and/or DNNs  $\implies$  able to exclude models with 3 sigma significance.

## Take home message:

- $\Lambda_\mu(X_{\max})$  measurement feasible with Auger statistics!

# Conclusions and outlook:

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## Conclusions:

- Model independent value of  $\Lambda_\mu$  for shallow showers but highly dependent for deep showers;
- Binning in  $X_{\max}$   $\Rightarrow$  continuously probe the hadronic activity of the first interaction;
- $\Lambda_\mu(X_{\max})$  evolution constrains models in different regions of the kinematic phase-space of 1<sup>st</sup> interaction  $\Rightarrow$  probe production cross-section of neutral pions in p-air interactions as a function of hadronic activity
- $\Lambda_\mu(X_{\max})$  measurement feasible with statistics of a typical UHECR observatory!
- Measuring  $\Lambda_\mu$  as a function of the primary energy by combining different experiments would probe the cross section for neutral pion production as a function of projectile energy  $\Rightarrow$  compare with/ extrapolate safely from accelerator data.
- More details in: [arXiv:2406.08620](https://arxiv.org/abs/2406.08620)

## Outlook:

- Fully explore the joint  $N_\mu - X_{\max}$  distribution to constrain particle production in the highest energies.