



# Effects of Biaxial Birefringence on Polarization Reconstruction for the Askaryan Radio Array

Alan Salcedo Gomez for the ARA Collaboration

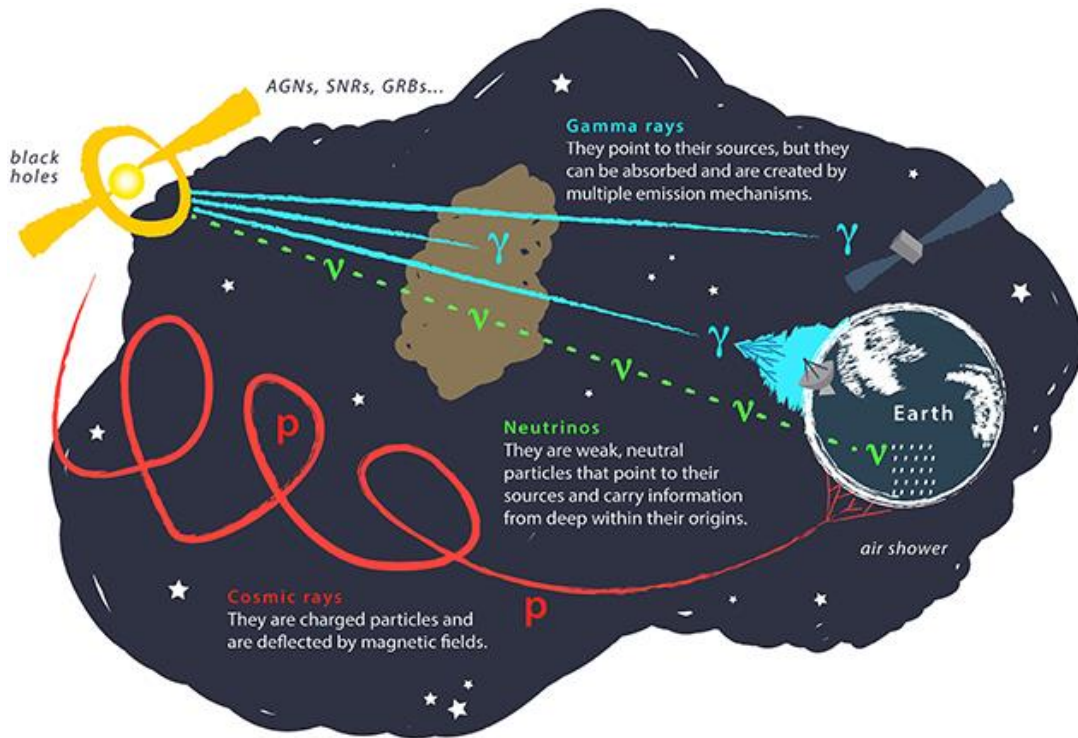
August 28<sup>th</sup>, 2024



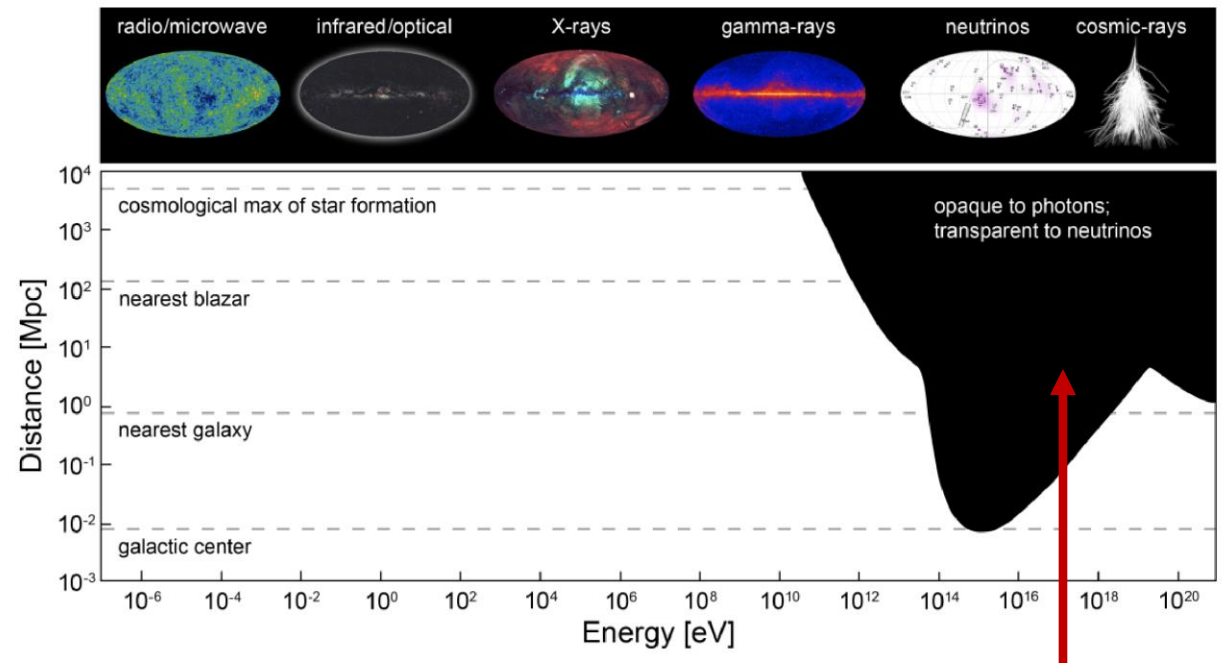
# Context

We want to expand the horizon of multi-messenger astrophysics

- Use neutrinos to study the most energetic and distant astrophysical sources in the Universe



Credit: IceCube Collaboration

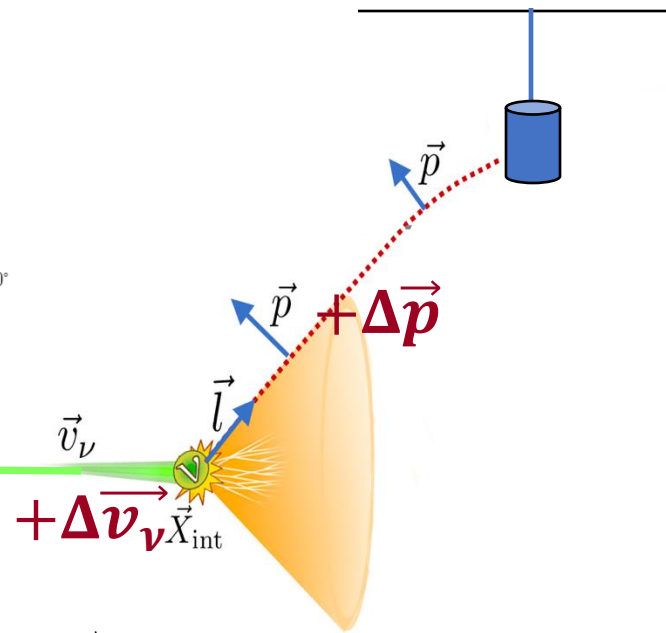
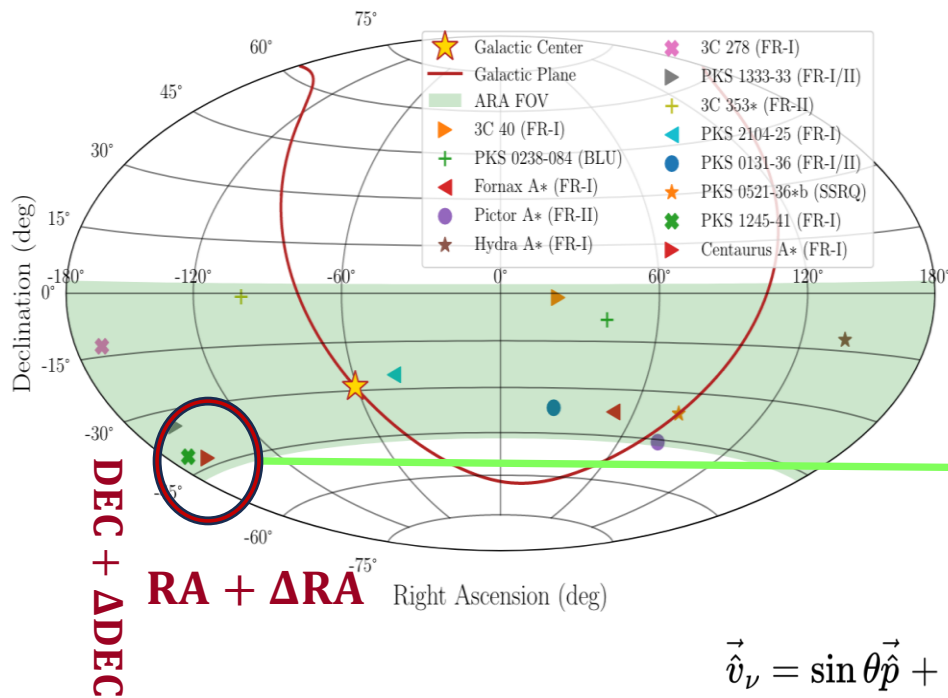


i.e. access this regime <sup>1</sup>

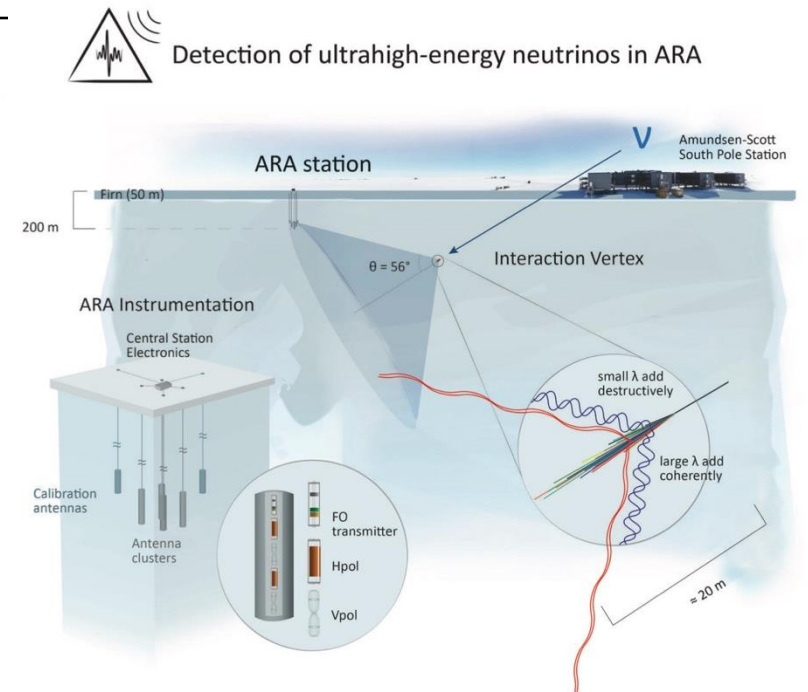
# Context

For this, we need to reconstruct the polarization of neutrino signals accurately and precisely

- **Uncertainties in polarization reconstruction propagate to uncertainties in the sky map**



$$\vec{v}_\nu = \sin\theta\vec{\hat{p}} + \cos\theta\vec{\hat{l}}$$

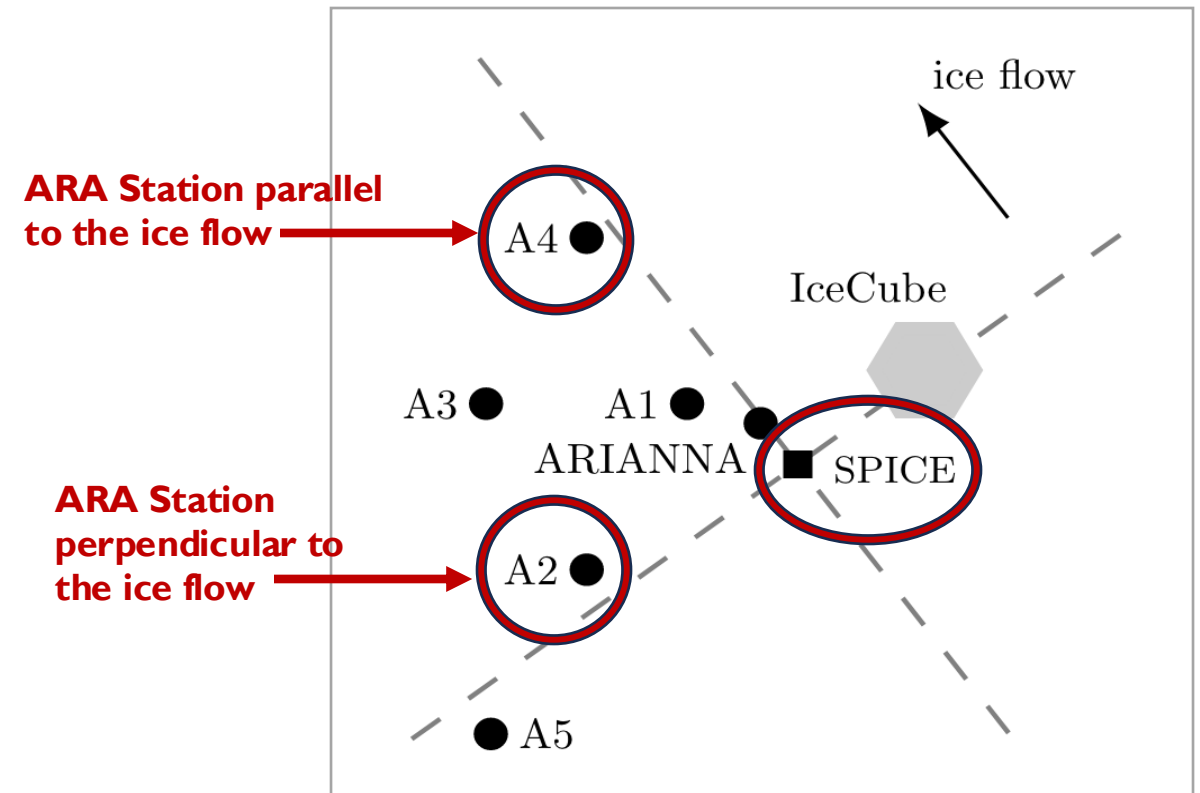


Modified from J. Torres (2020) and S. Barwick, C. Glaser (2023)

# SPICE Pulsar

The SPICE pulsing campaign provided a unique dataset of broadband radio pulses transmitted inside the ice

- The **South Pole Ice Core Experiment (SPICE)** drilled and recovered ice cores up to a depth of  $\sim 1700$  m
- **Broadband radio pulses were transmitted from inside the SPICE borehole** and received by ARA (A1 – A5) and ARIANNA over 1 - 5 km horizontal baselines
- This unique dataset been **important for calibrations and measurements of ice properties**

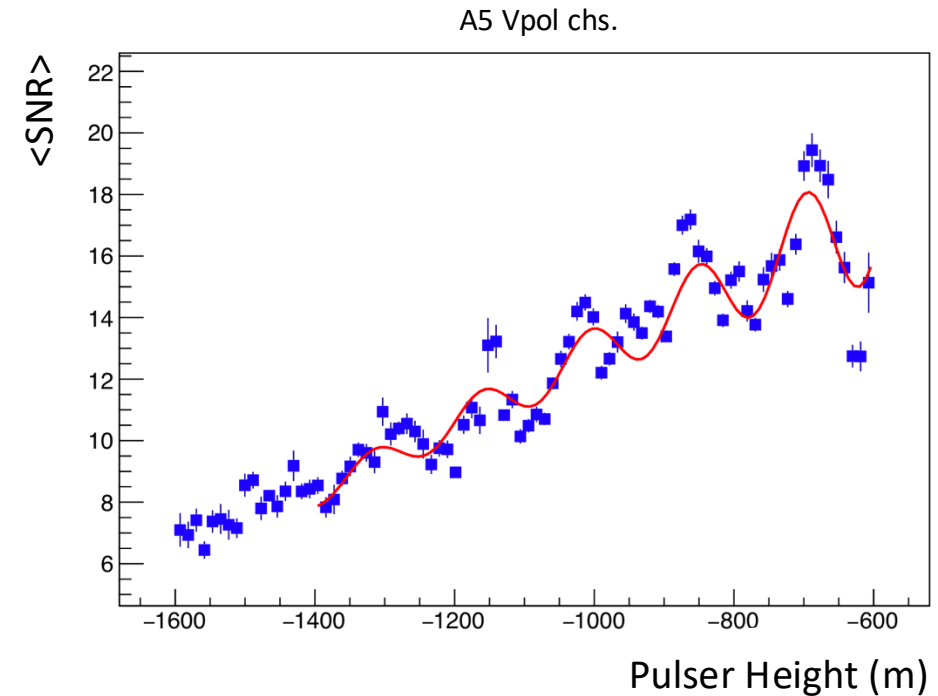
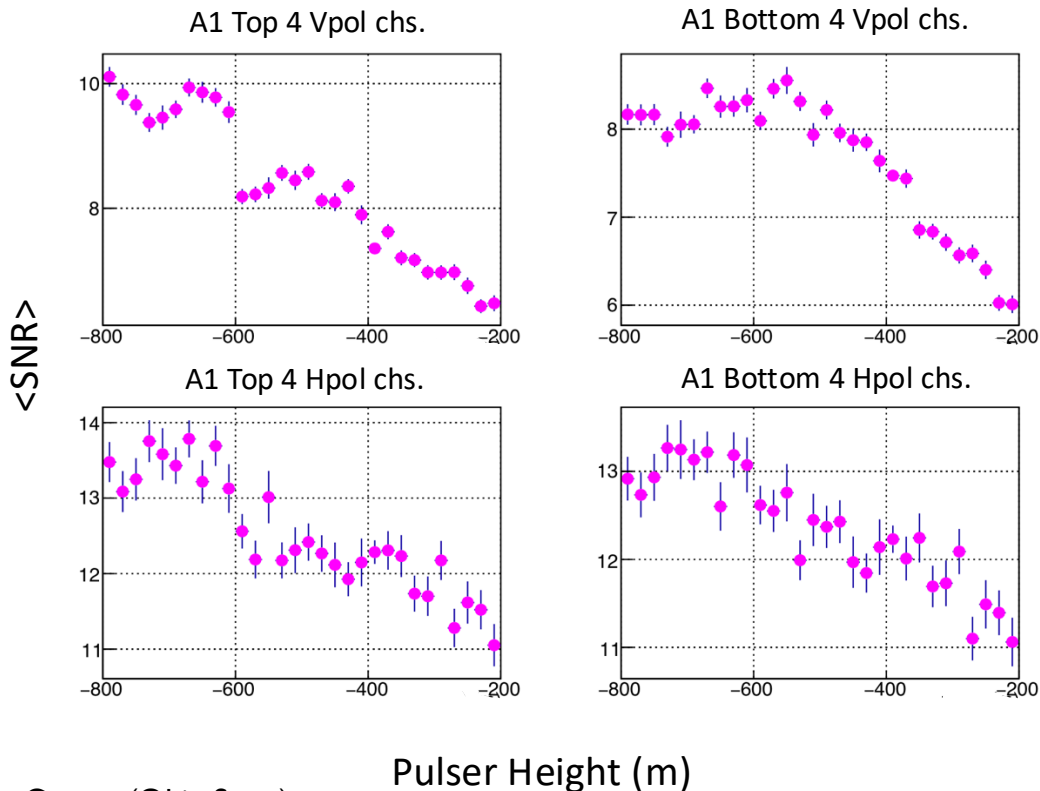


A. Connolly, Phys. Rev. D 105 (2022) 12, 123012

# SPICE Pulsar

## ARA observed an anomalous behavior of polarization from SPICE pulses

- Pulsars transmitted as Vpol were observed with higher Hpol power than expected, even larger in Hpol than Vpol
- Oscillatory behavior on signal-to-noise ratio

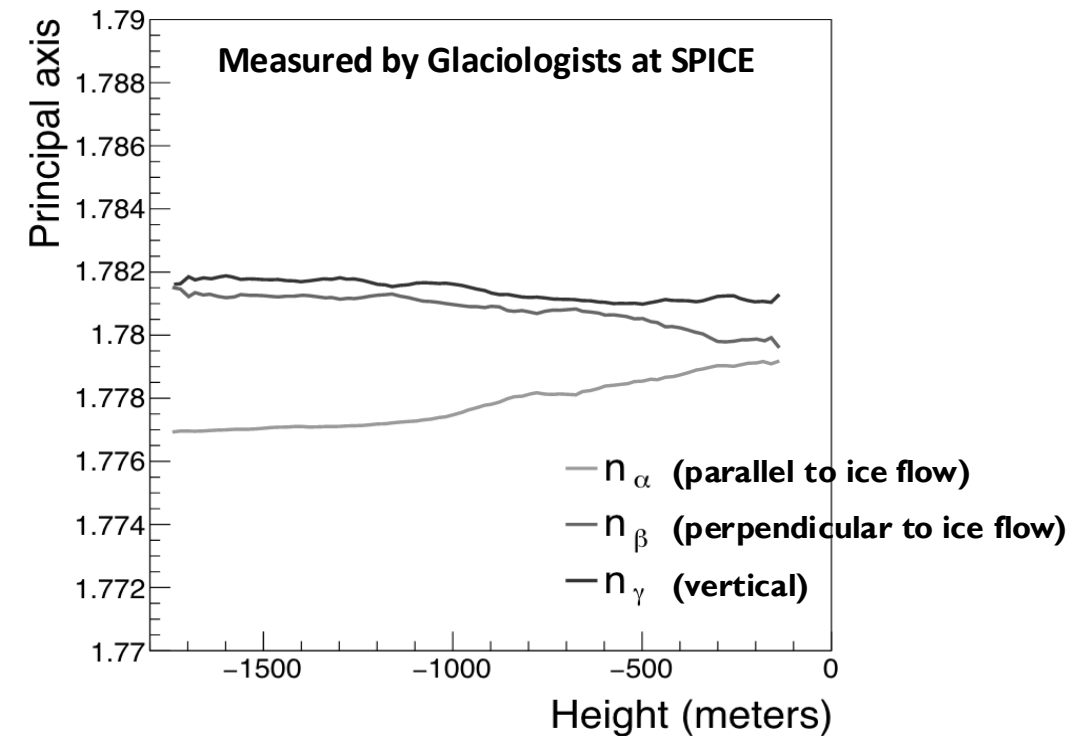


P.Allison et al, JCAP 12 (2020) 009

# Birefringence

Polar ice behaves as a biaxially birefringent medium at radio frequencies

- In birefringent media, the **propagation** of electromagnetic radiation **depends on its direction and polarization**
- Biaxial birefringent media are characterized by **three parameters** along three perpendicular axes, known as principal axes
- We are exploring **biaxial birefringence as a possible explanation of the anomalous behavior of polarization in SPICE events**

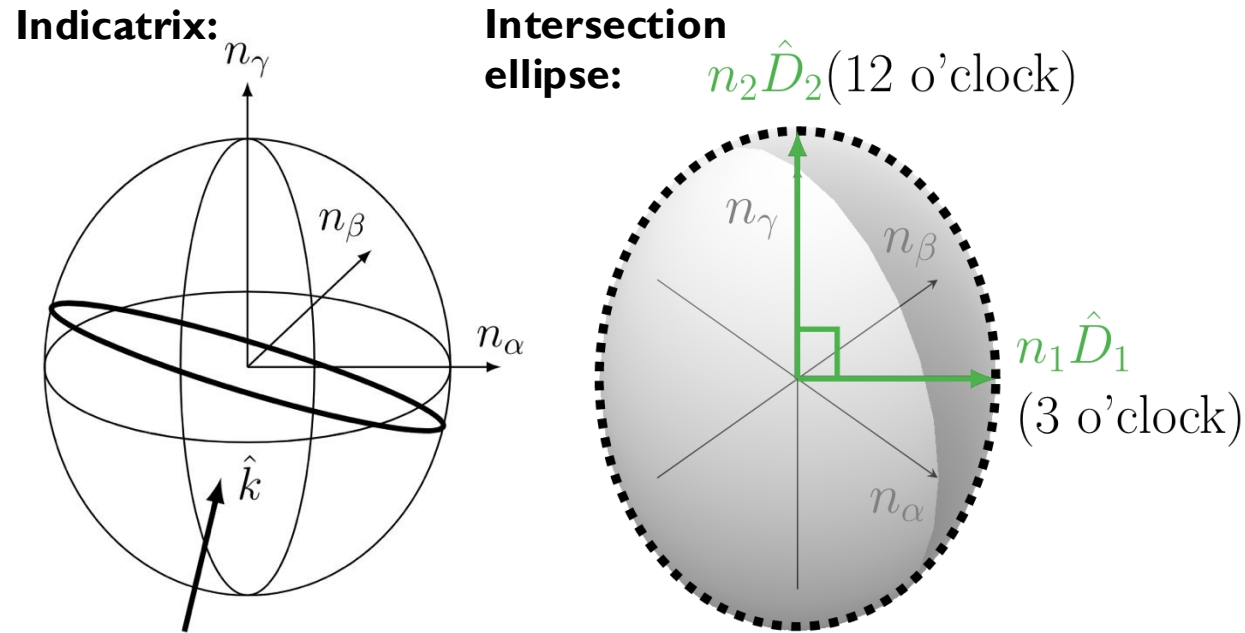


A. Connolly, Phys. Rev. D 105 (2022) 12, 123012

# Birefringence Model

The polarization vector is described by two eigenstates dependent on the principal axes

- Eigenstates are given by the axes of the intersection ellipse of an indicatrix and the signal's wavefront



- $n_\alpha, n_\beta, n_\gamma$  change with depth
- $n_1$  and  $n_2$  are different indices of refraction.  $\hat{D}_1$  and  $\hat{D}_2$  describe two separate rays

A. Connolly, Phys. Rev. D 105 (2022) 12, 123012

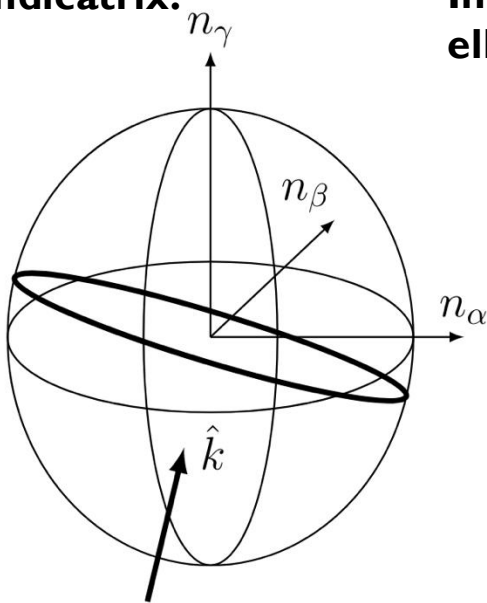


# Birefringence Model

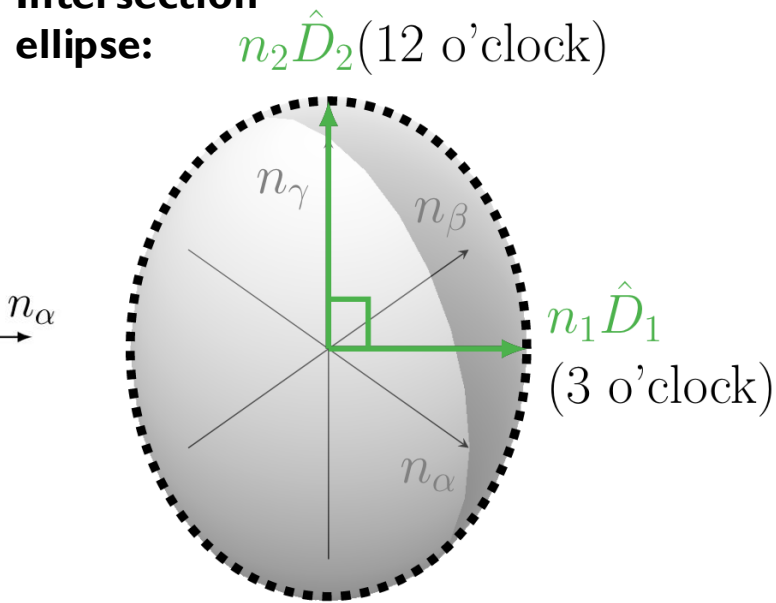
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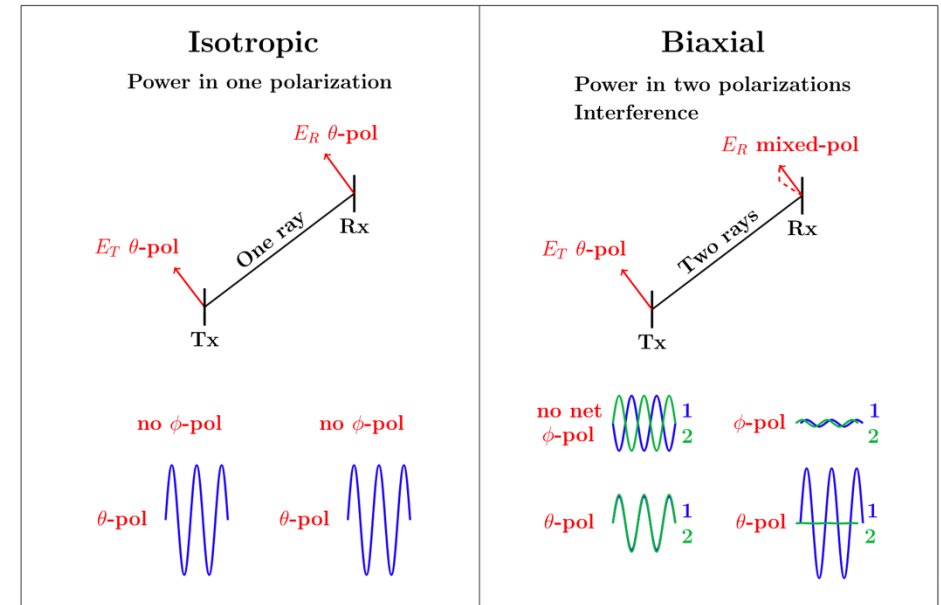
Indicatrix:



Intersection ellipse:



Polarization description before: | Polarization description now:



- $n_\alpha, n_\beta, n_\gamma$  change with depth
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A. Connolly, Phys. Rev. D 105 (2022) 12, 123012

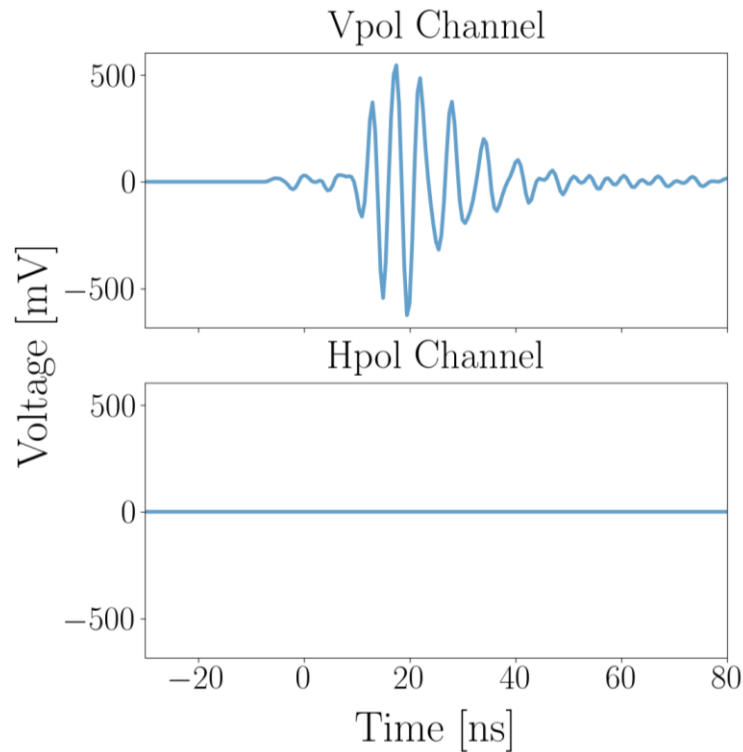


# Birefringence Model

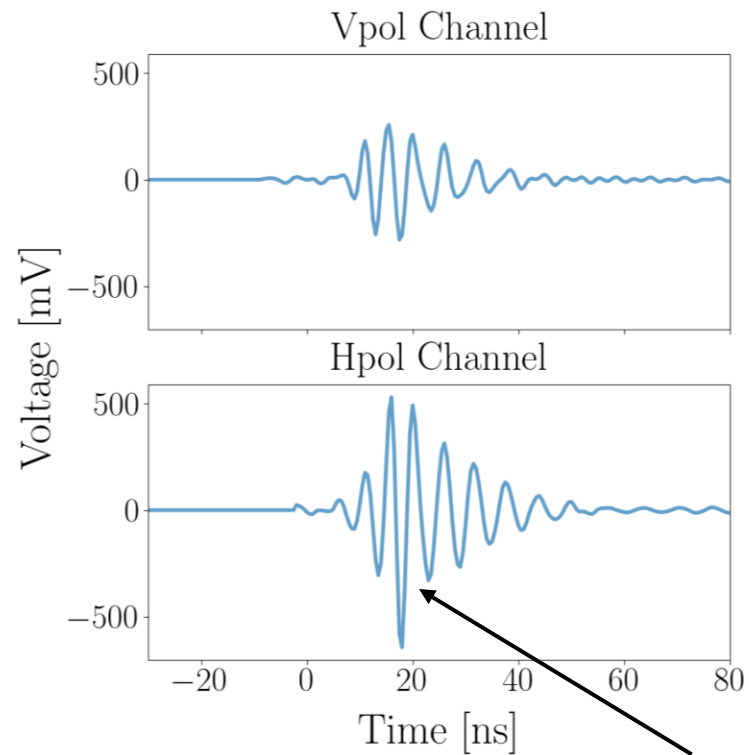
This birefringence model is now implemented in AraSim

**Simulation:** Pulser at SPICE location to **A4** from 1600 m depth

**Without birefringence**



**With biaxial birefringence:**



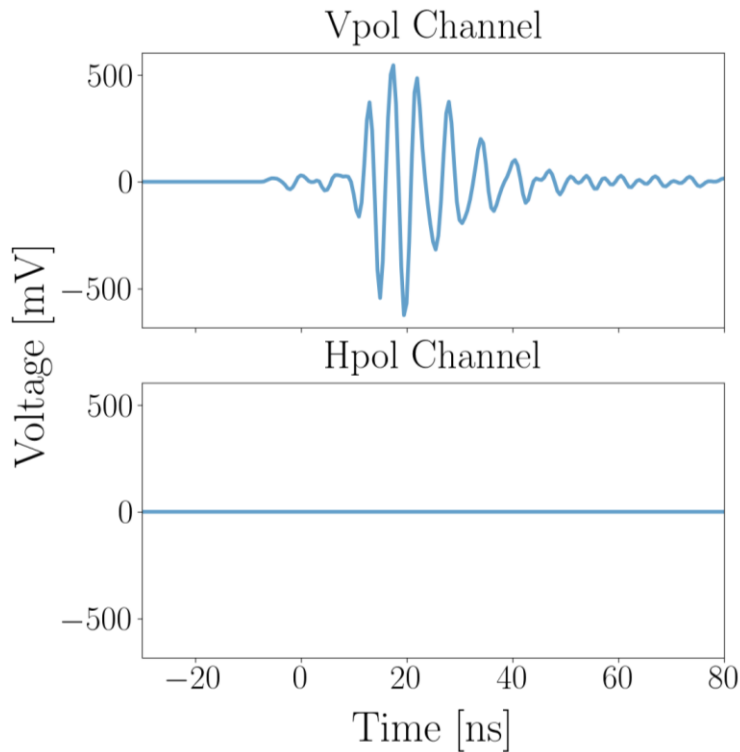
**Rotation**

# Birefringence Model

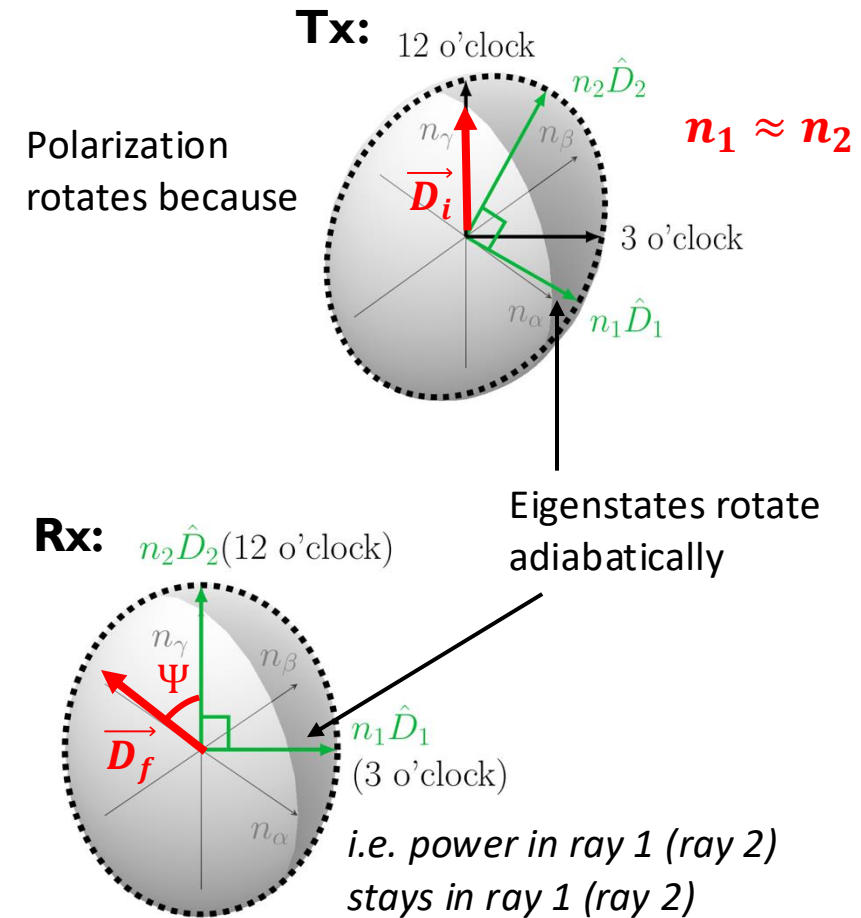
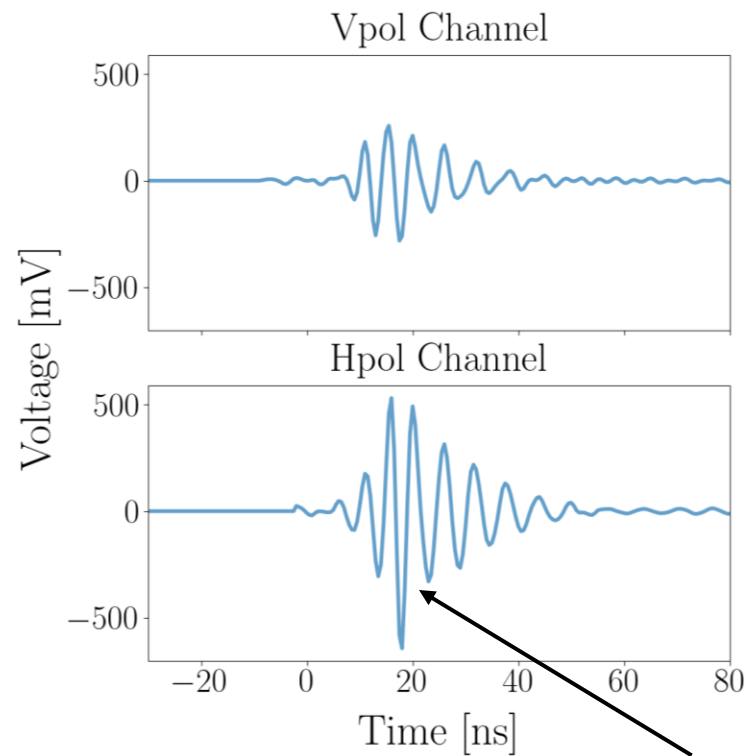
The **polarization** of a signal is **allowed to rotate** in this model

**Simulation:** Pulser at SPICE location to **A4** from 1600 m depth

**Without birefringence**



**With biaxial birefringence:**

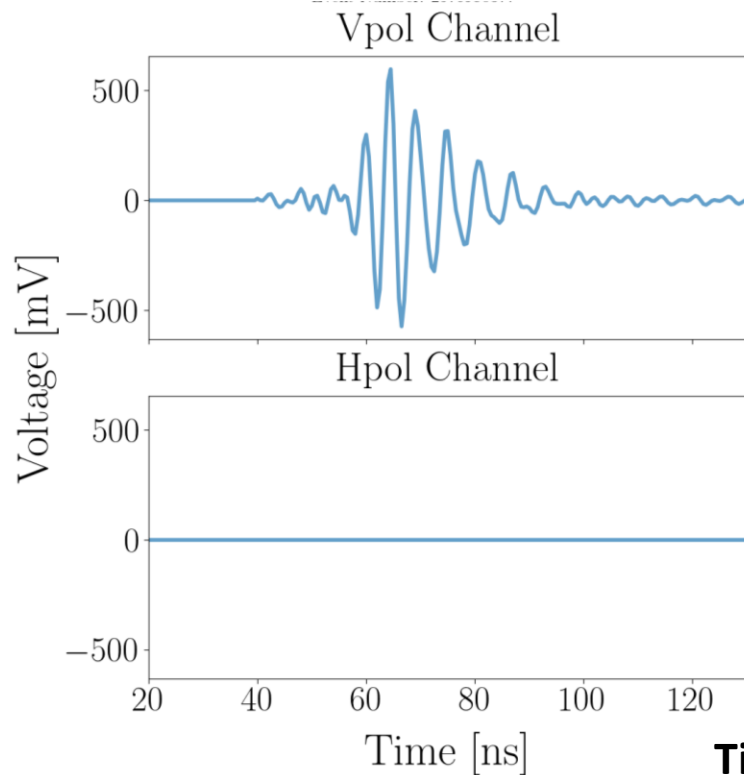


# Birefringence Model

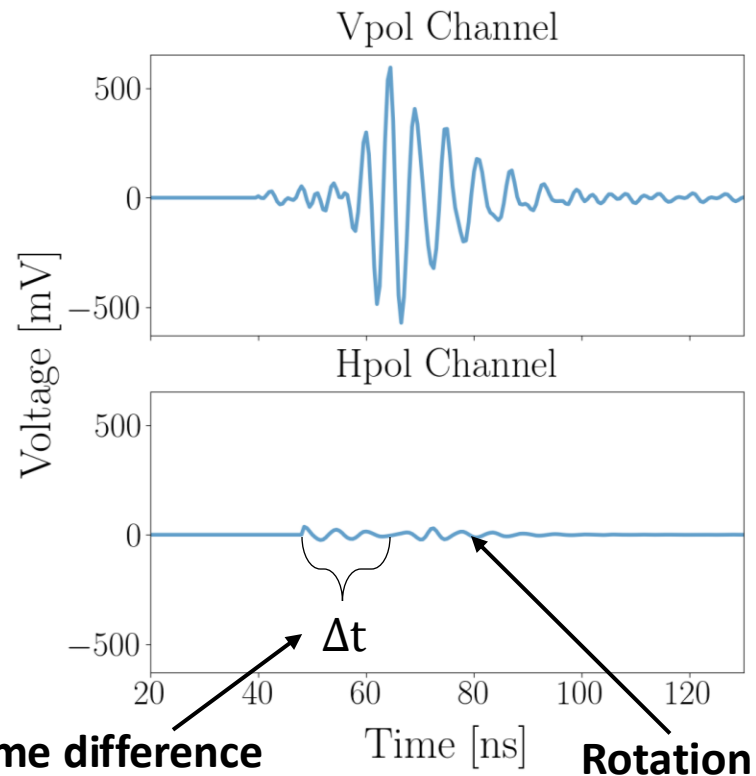
The polarization **eigenstates** are allowed to **arrive at different times**

**Simulation:** Pulser at SPICE location to **A2** from 1600 m depth

**Without birefringence:**



**With biaxial birefringence:**

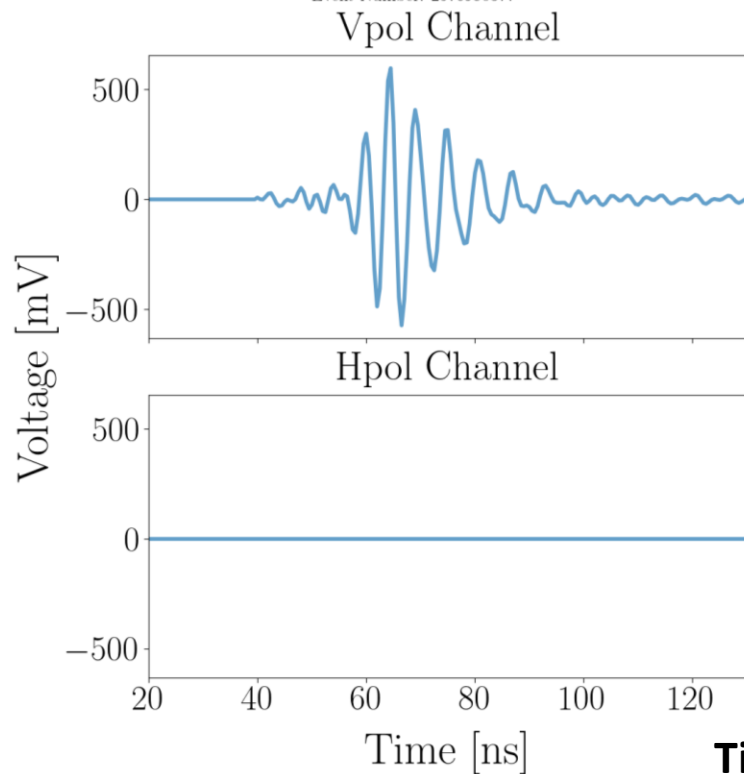


# Birefringence Model

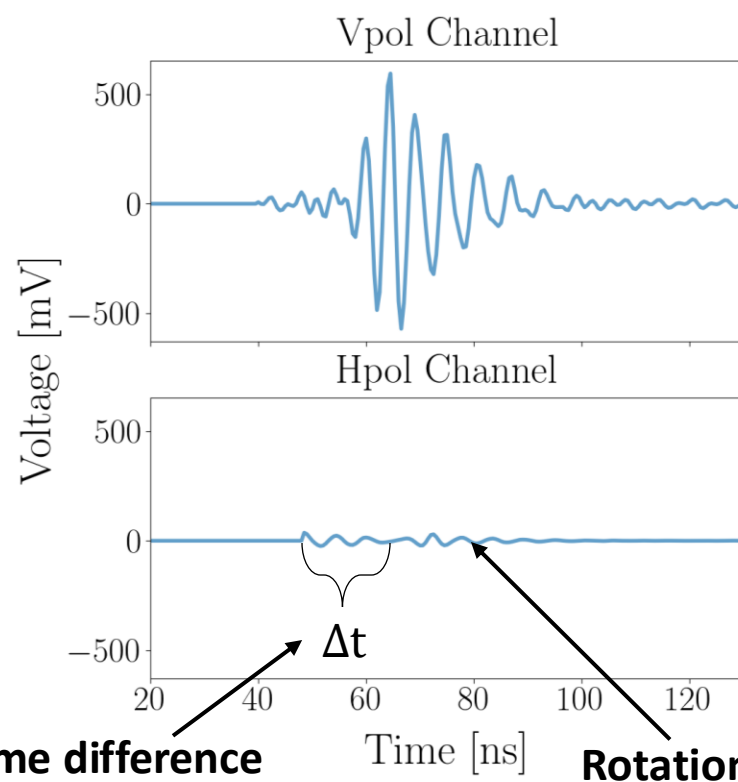
The polarization **eigenstates** are allowed to **arrive at different times**

**Simulation:** Pulser at SPICE location to **A2** from 1600 m depth

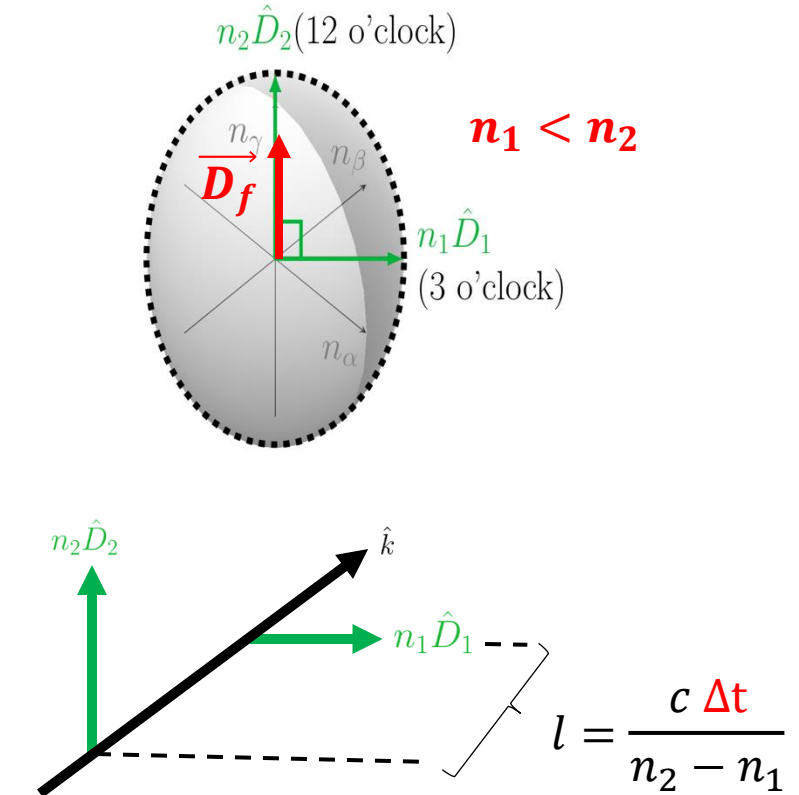
**Without birefringence:**



**With biaxial birefringence:**

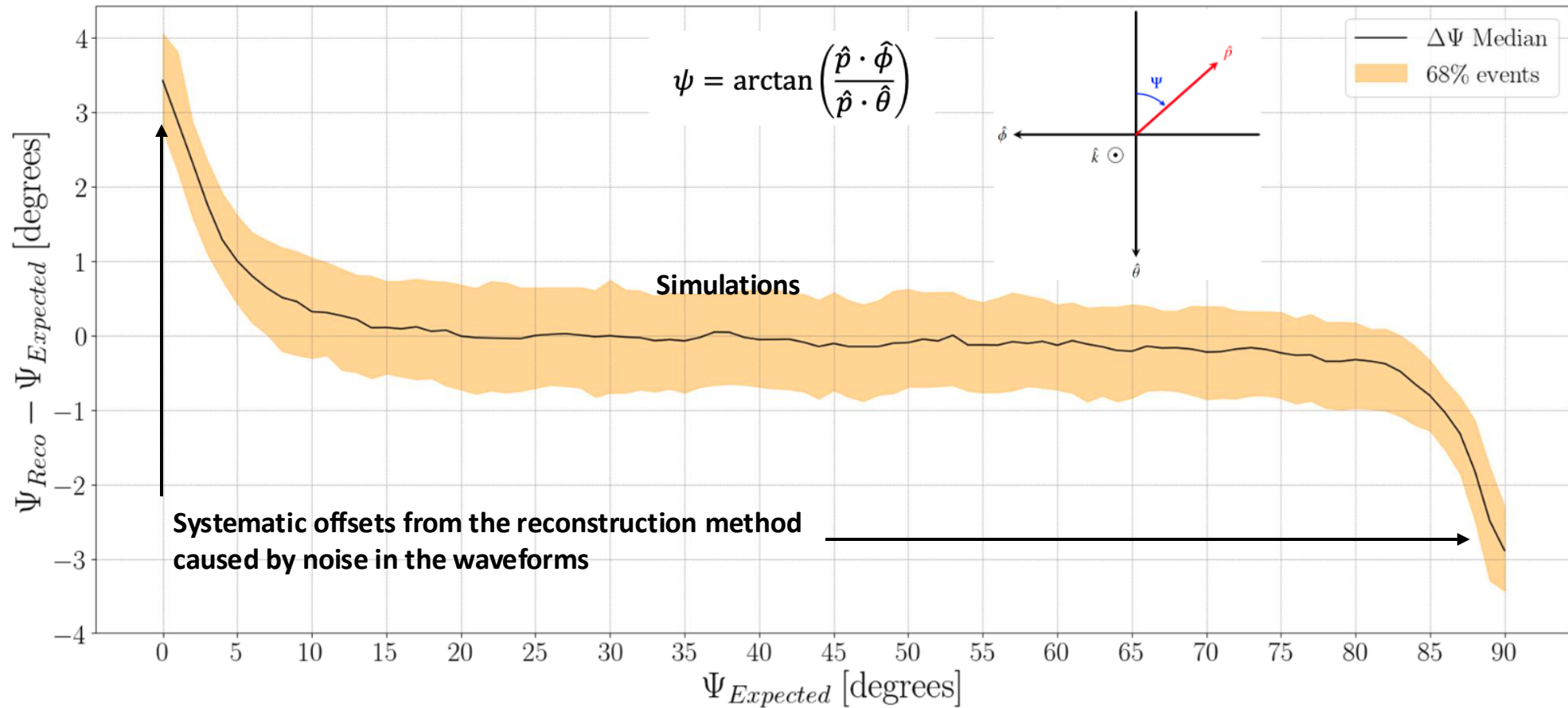


**Tx and Rx:**



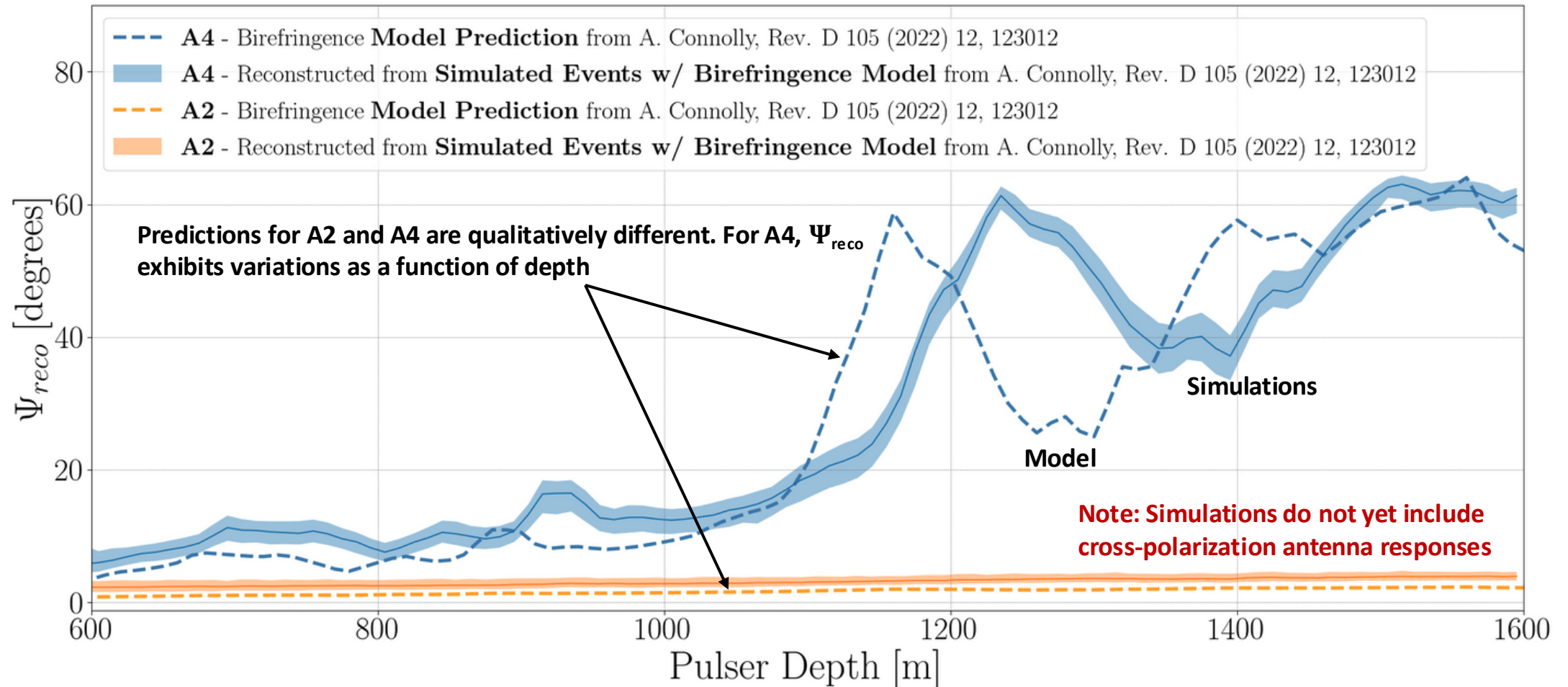
# Polarization Reconstruction

Reconstructing the polarization angle from ARA events is possible



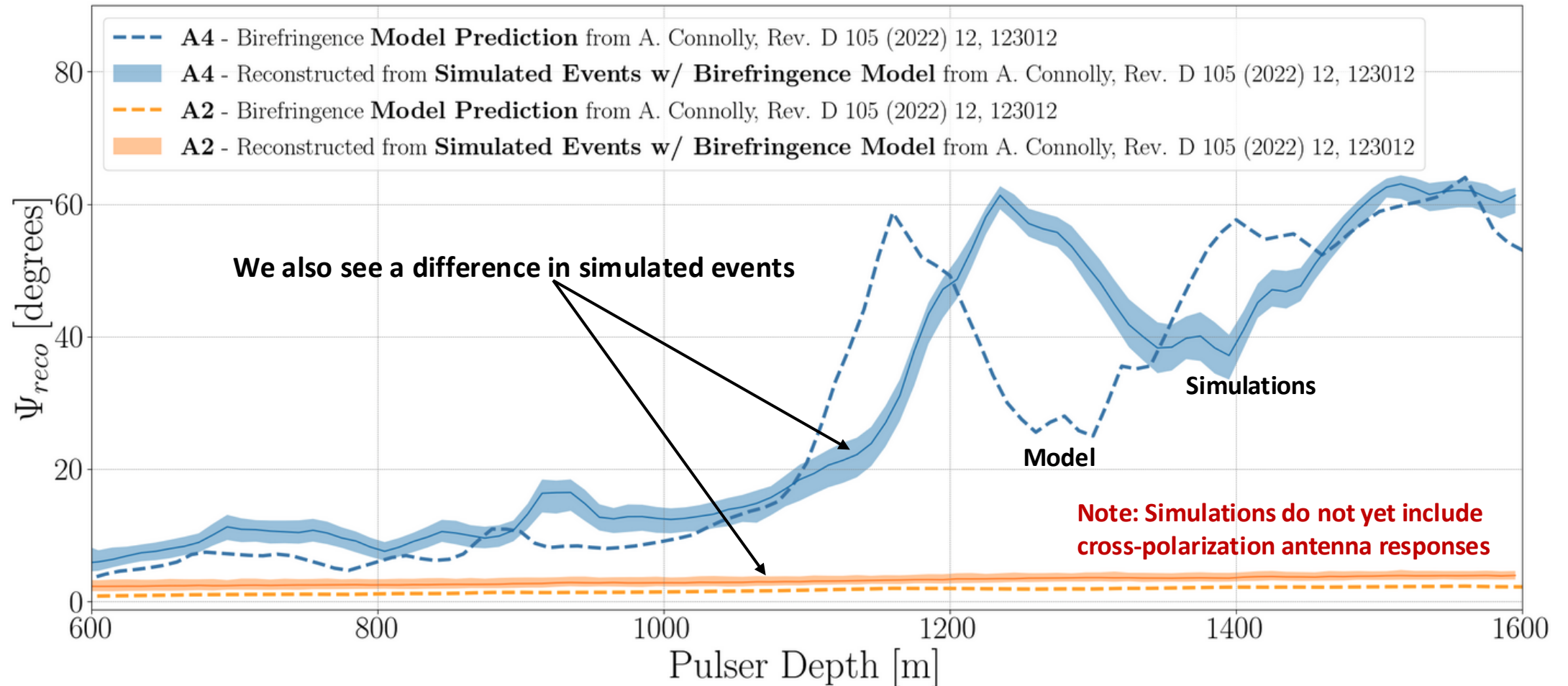
# Polarization Reconstruction

Polarization angle reconstruction on **A2** and **A4** from **simulated pulses at SPICE**



# Polarization Reconstruction

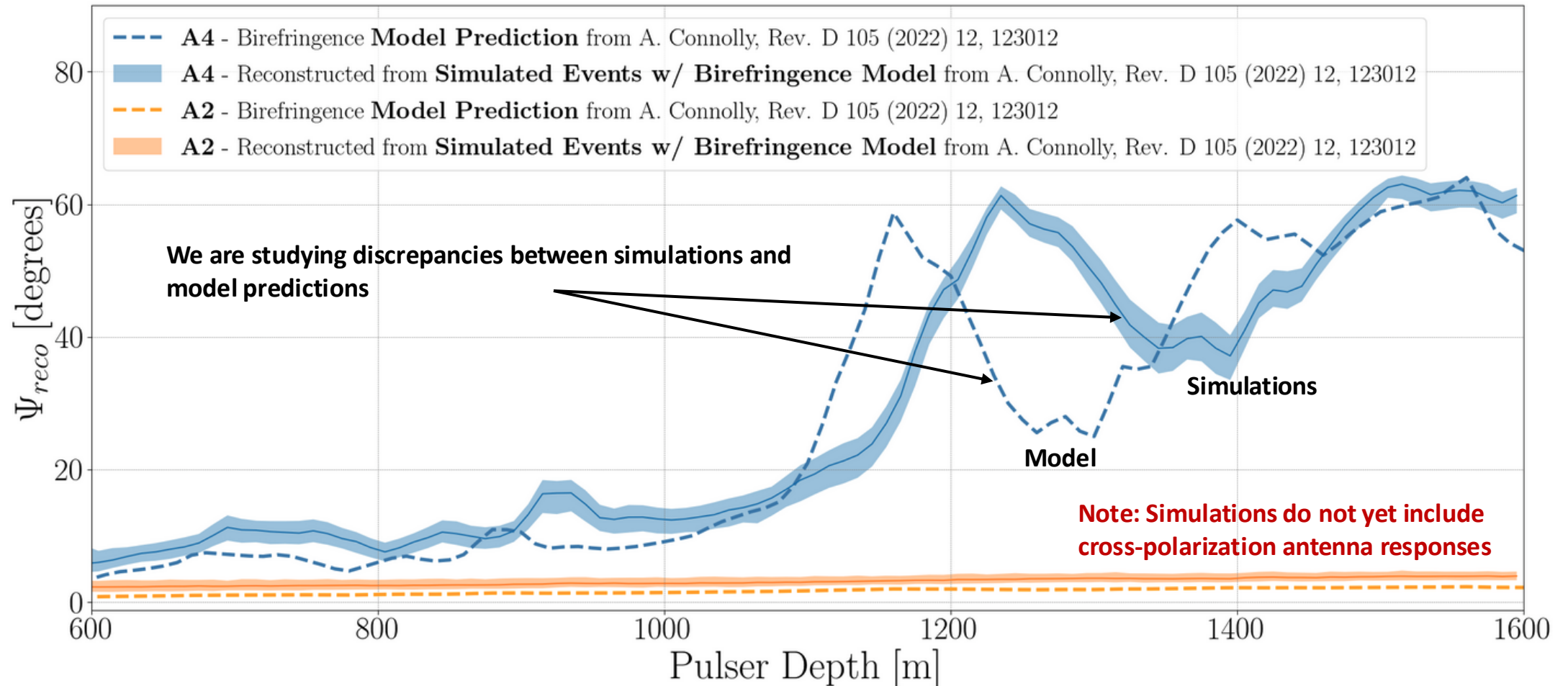
Polarization angle reconstruction on **A2** and **A4** from **simulated pulses at SPICE**





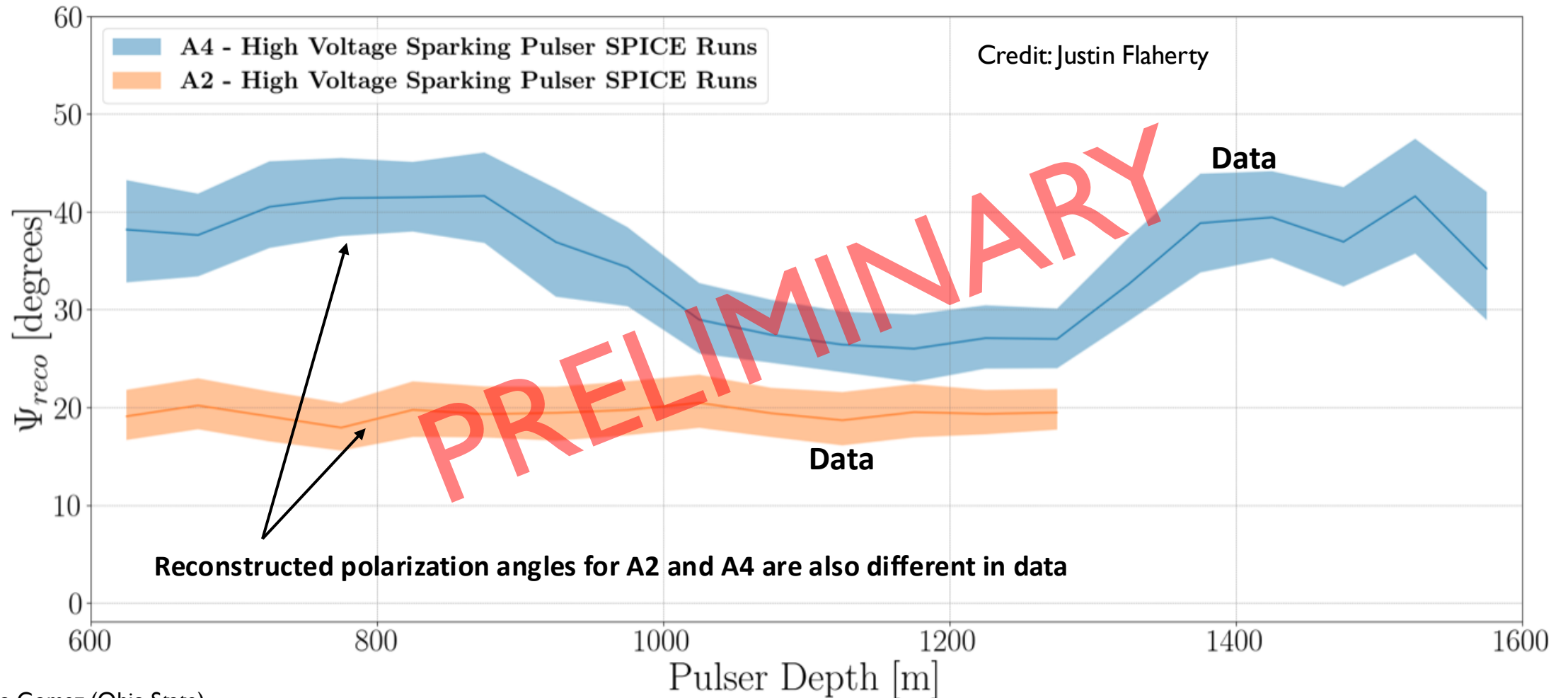
# Polarization Reconstruction

Polarization angle reconstruction on **A2** and **A4** from **simulated pulses at SPICE**



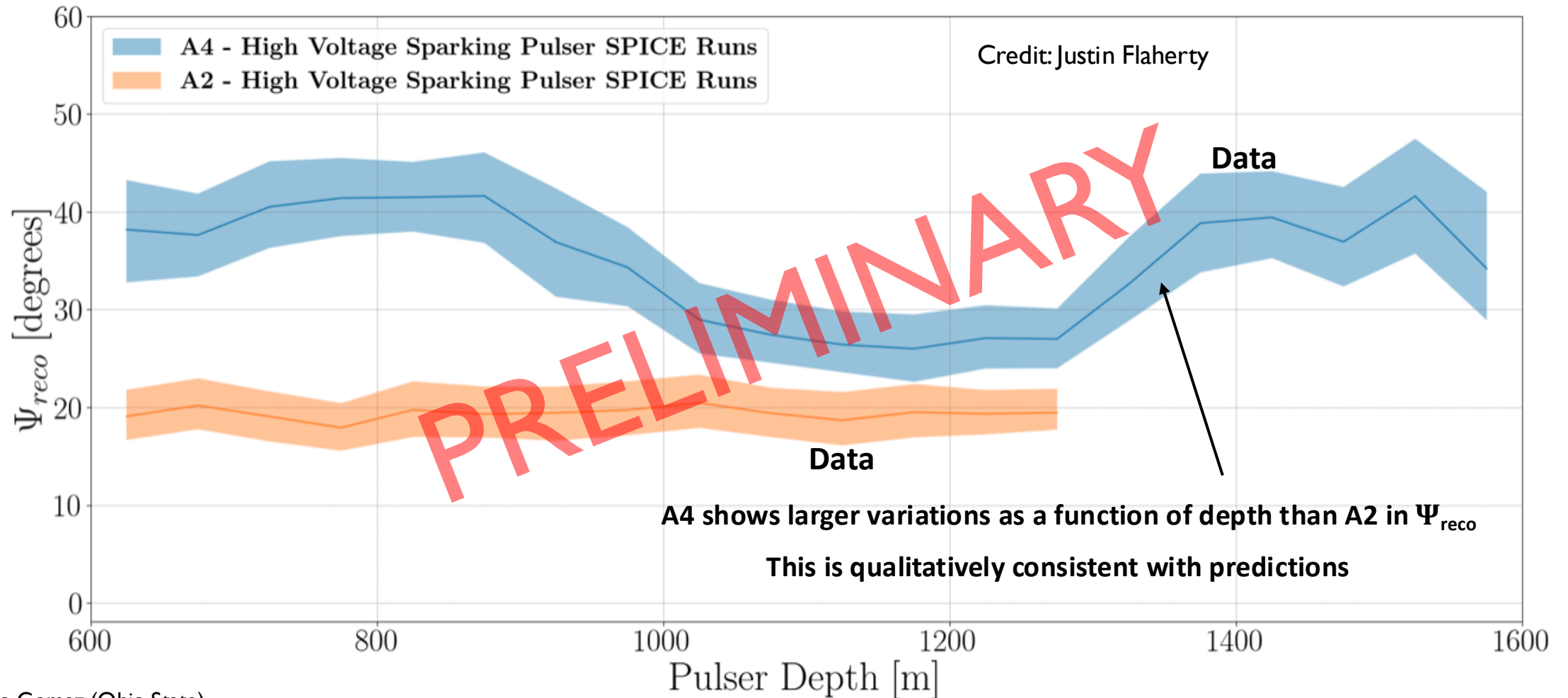
# Polarization Reconstruction

Polarization angle reconstruction on **A2** and **A4** from **SPICE** data



# Polarization Reconstruction

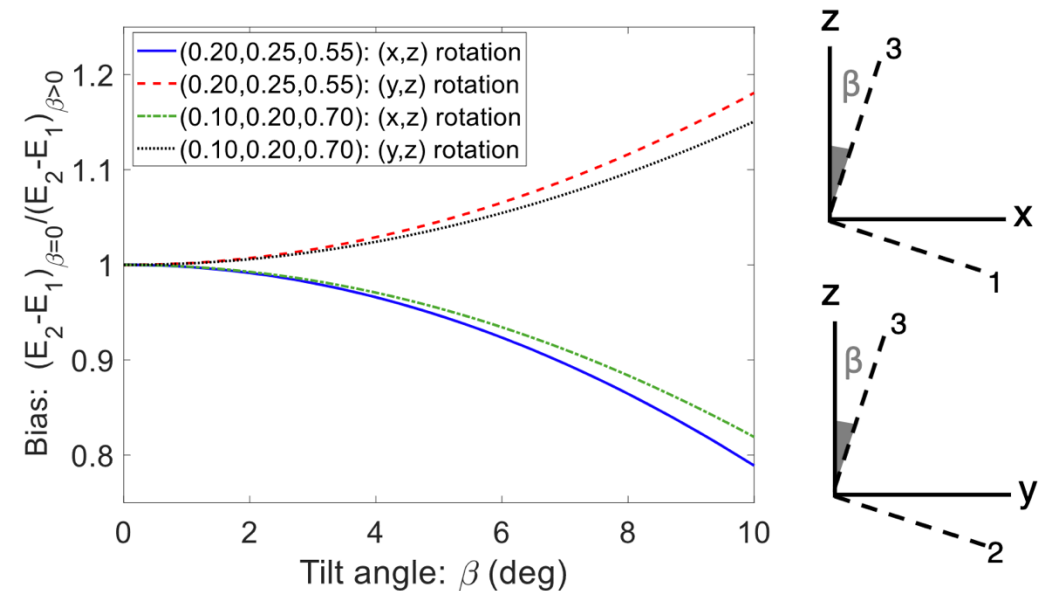
Polarization angle reconstruction on **A2** and **A4** from **SPICE** data



# Systematic Uncertainties

Uncertainties on the orientation of principal axes is not uncommon

- Theory assumes that indicatrix has  $\gamma$ -axis vertical and  $\alpha$ -axis along ice flow
- North Greenland Eemian Ice Drilling (**NEEM**):  $\alpha$ -axis as much as **25° from ice flow** (Jordan et al, 2020) and the  $\gamma$ -axis **9.6° from vertical** (J. Li, et al, 2018)
- At the South Pole, the tilt angle up to  $\sim 10^\circ$  (IceCube). Can lead to 20% uncertainties in  $n_\alpha - n_\beta$

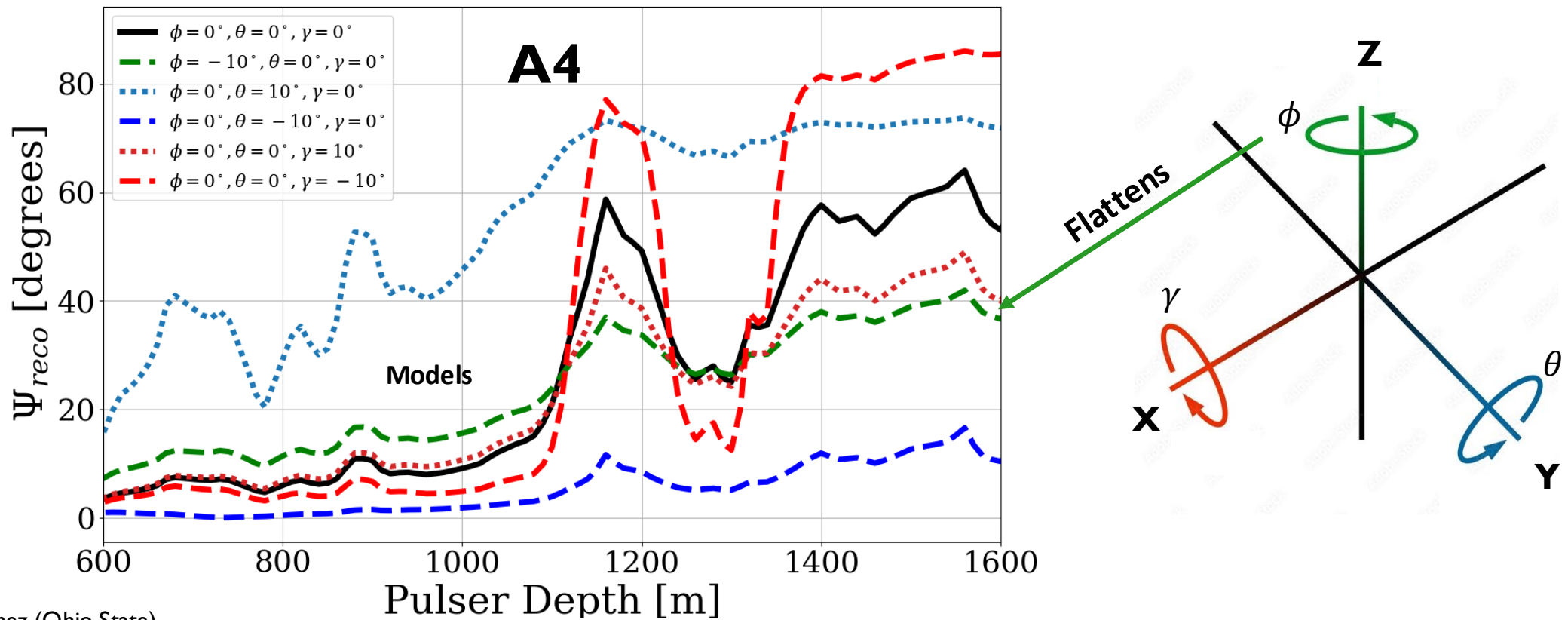


T. M. Jordan, . IEEE Transactions on Geoscience and Remote Sensing, 57 (2019) 11, 8641–8657

# Systematic Uncertainties

These can have a large effect on predictions for polarization reconstruction

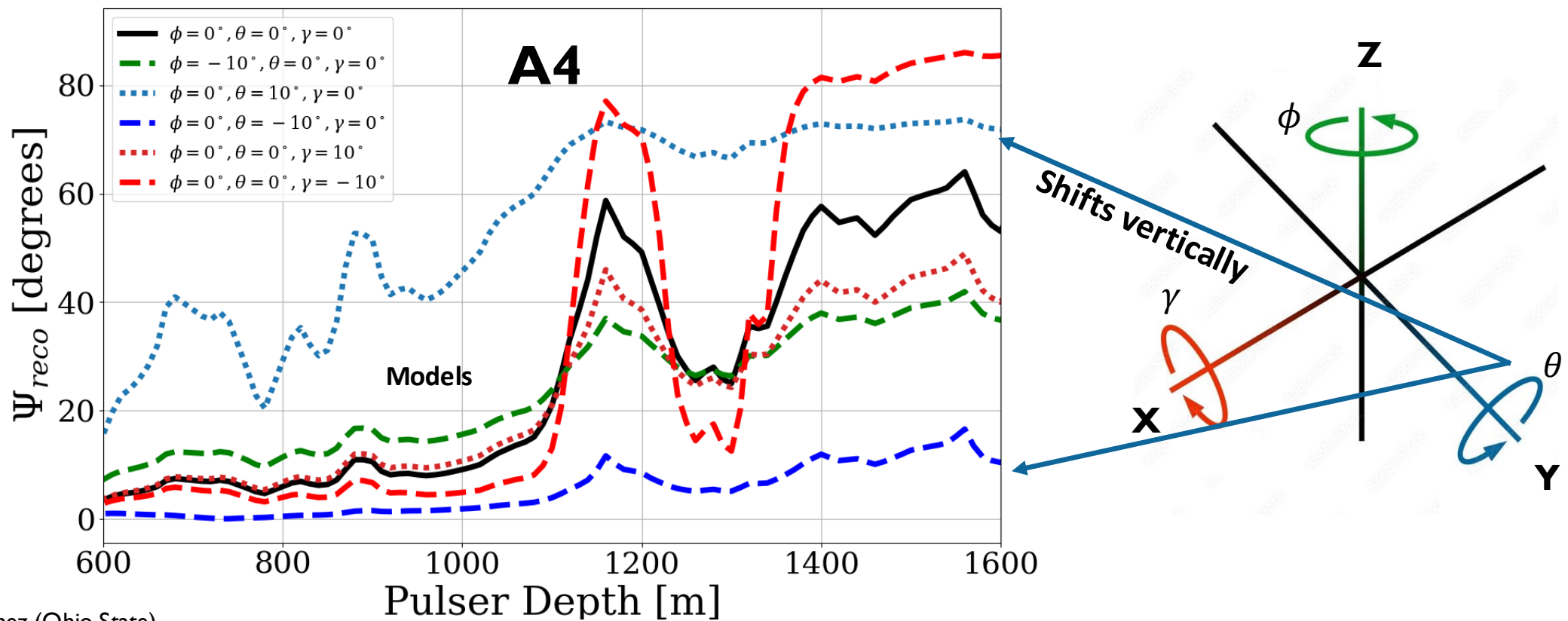
- Exploring effects of **rotating principal axes around each axis** on predictions for polarization reconstruction angles



# Systematic Uncertainties

These can have a large effect on predictions for polarization reconstruction

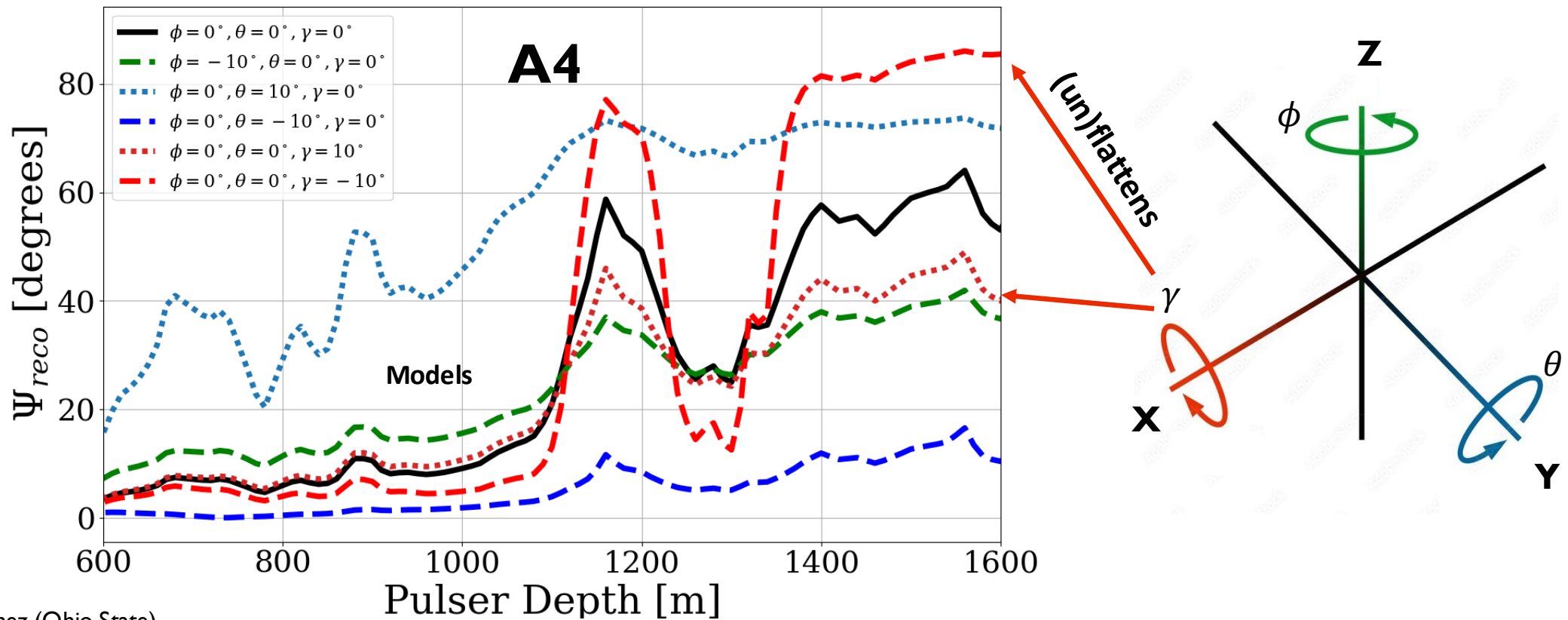
- Exploring effects of **rotating principal axes around each axis** on predictions for polarization reconstruction angles



# Systematic Uncertainties

These can have a large effect on predictions for polarization reconstruction

- Exploring effects of **rotating principal axes around each axis** on predictions for polarization reconstruction angles

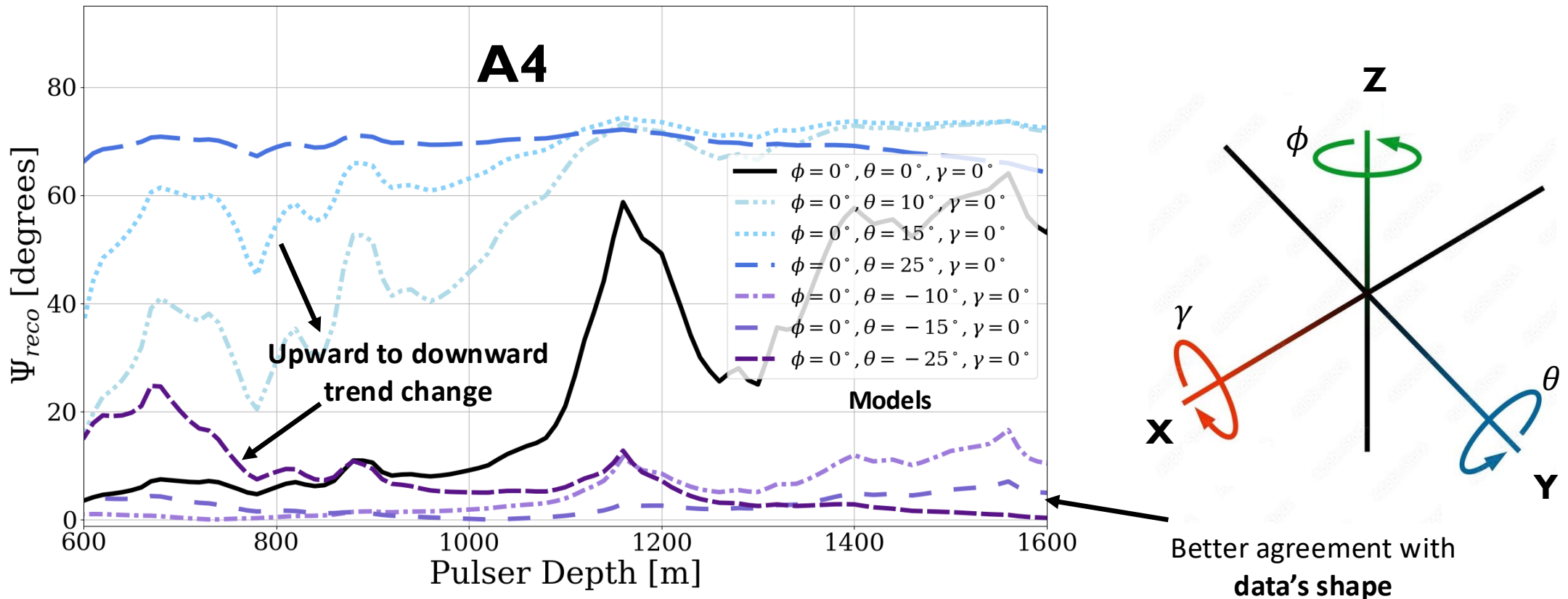




# Systematic Uncertainties

These can have a large effect on predictions for polarization reconstruction

- The qualitative shape of  $\Psi$  in data can be potentially obtained with a fit in  $(\phi, \theta, \gamma)$  across all five ARA stations

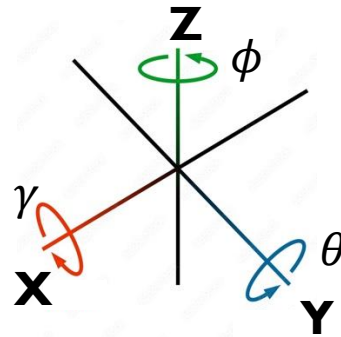


# Future Work

Biaxial birefringence effects may have implications for analysis and detector design

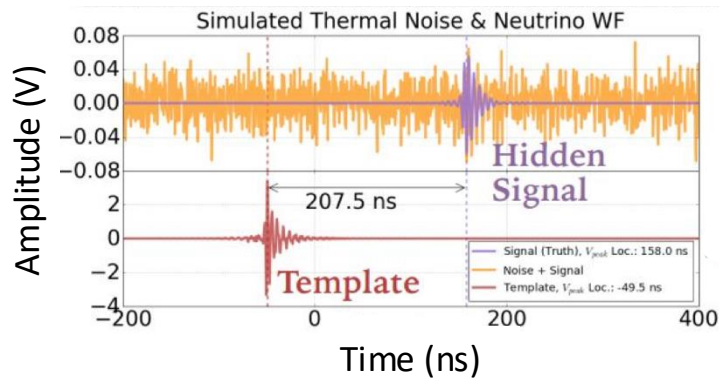
## Principal Axes Orientation Fit:

- Fit rotation angles on glaciology measurements of principal axes using SPICE data set across all ARA stations



## Neutrino Template Analysis:

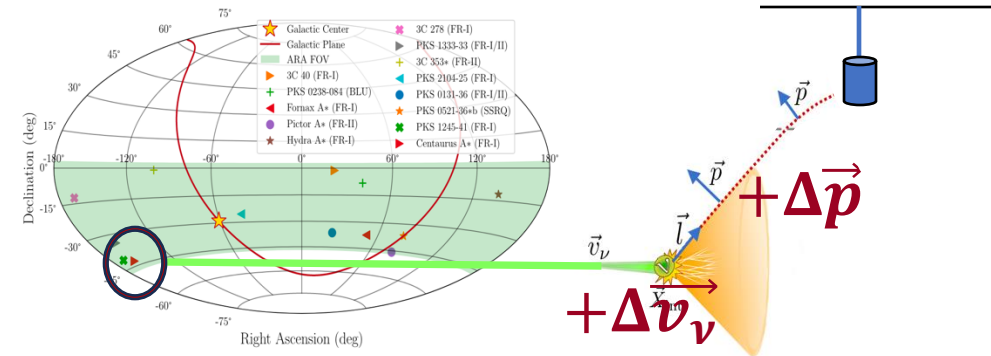
Credit: Myoungchul Kim



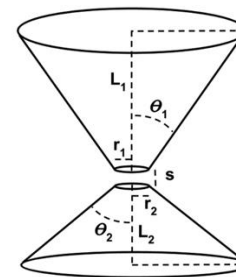
- Can design neutrino templates with birefringence effects

## Point Source Search:

Modified from J. Torres (2020) and S. Barwick, C. Glaser (2023)



- Birefringence should be taken into account in directional neutrino searches



## GENETIS is Optimizing Antenna and Array Designs:

- Exploring the optimization of antenna designs and detector array layouts accounting for birefringence effects

# Summary

- We are investigating **South Pole ice as a biaxial birefringent medium at radio frequencies.**
- Biaxial birefringence is expected to **cause rotations in polarization.**
- We are **using the unique SPICE pulser data set** across all five ARA stations **to fit for the parameters of the birefringence principal axes.**
- Biaxial birefringence **might need to be accounted for polarization reconstruction** and for performing point source searches of ultra-high energy neutrinos.
- **The effects of biaxial birefringence represent opportunities** to improve analysis and optimize detector designs.

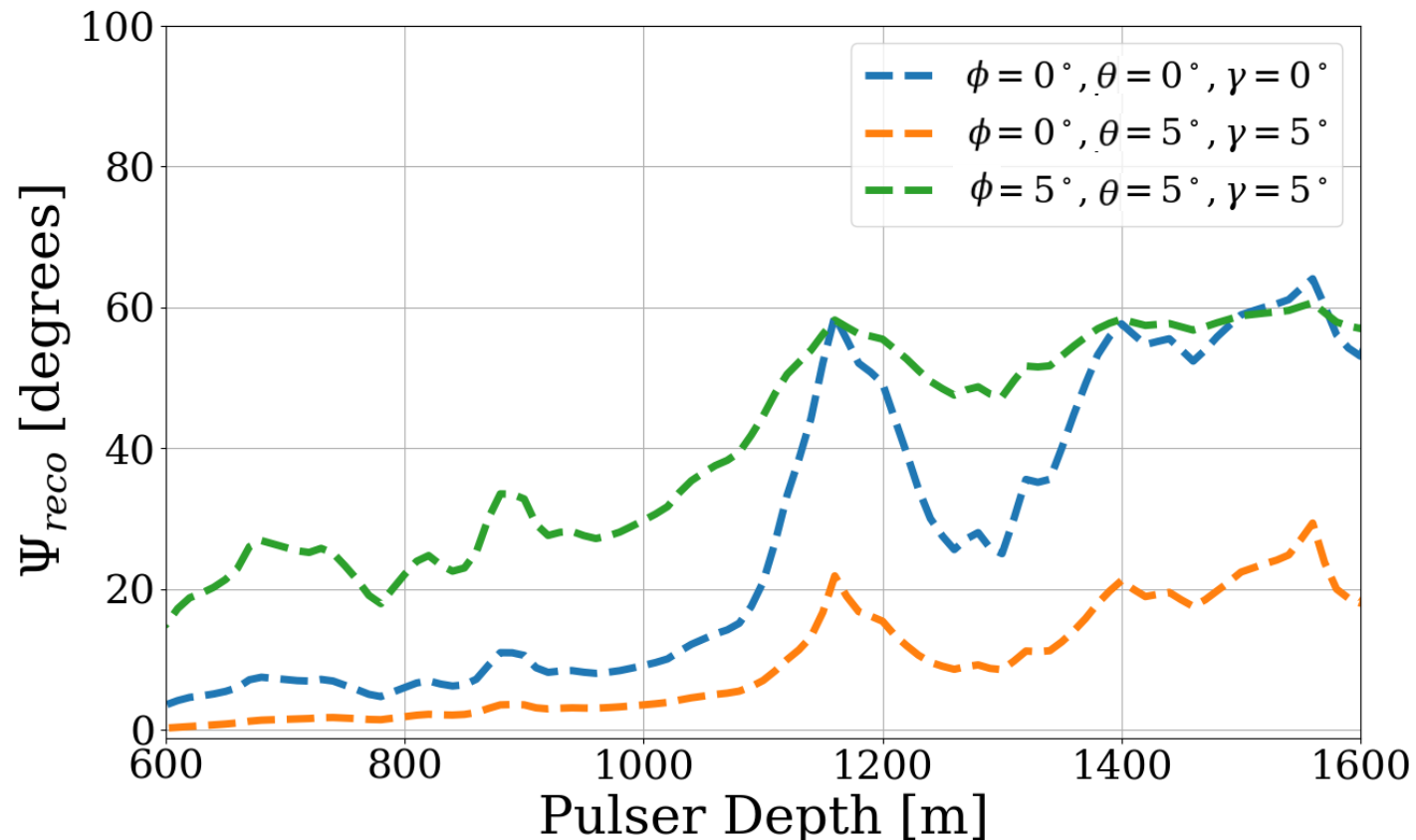
# Fin

- **Thank you!**

# BACKUP I: Systematic Uncertainties

Rotation of the COF can have a large effect on predictions for polarization reconstruction

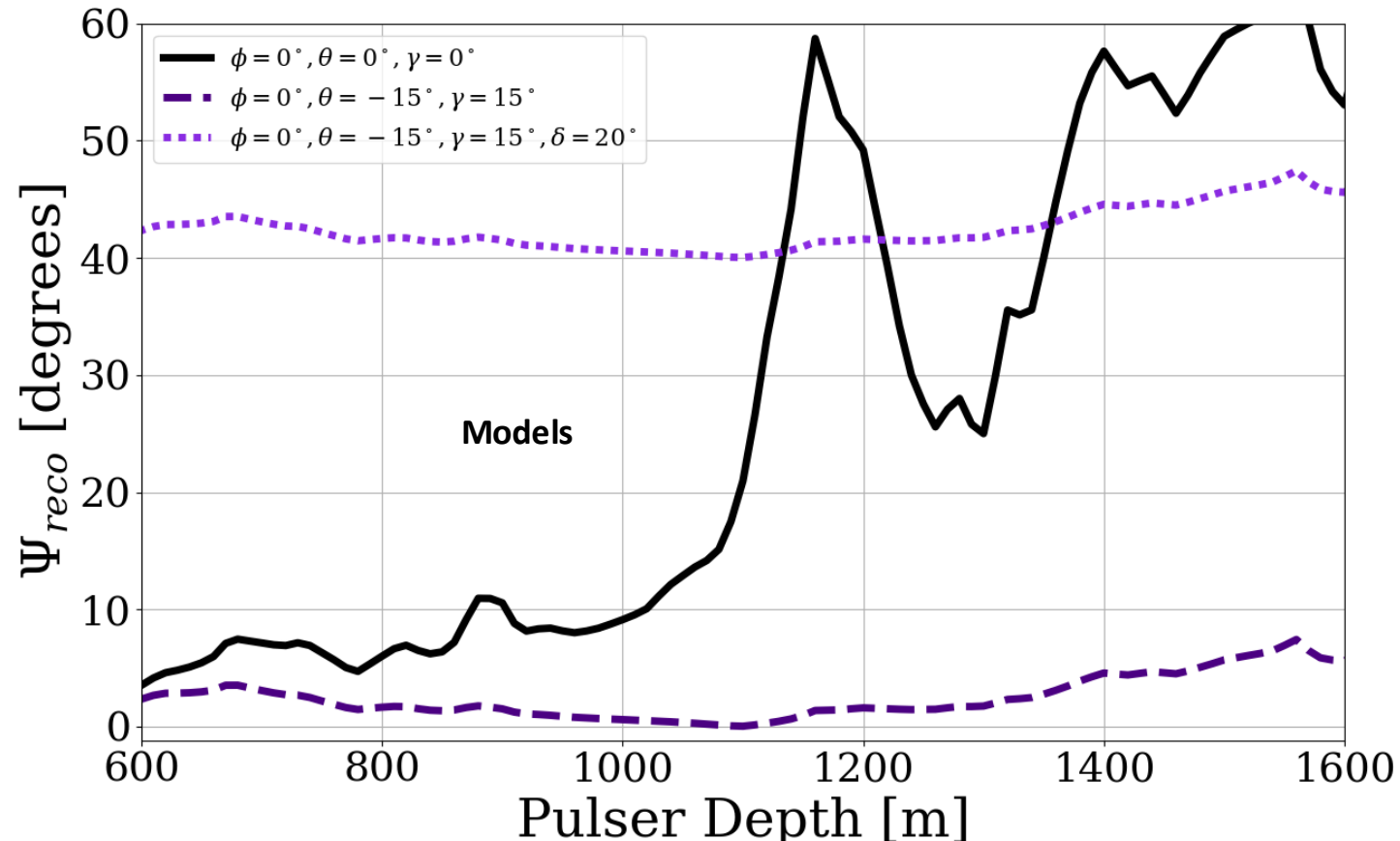
- Then, we calculate the effects on  $A_4$  by rotating the principal axes by  $5^\circ$  around **multiple axes at a time**



# BACKUP 2: Systematic Uncertainties

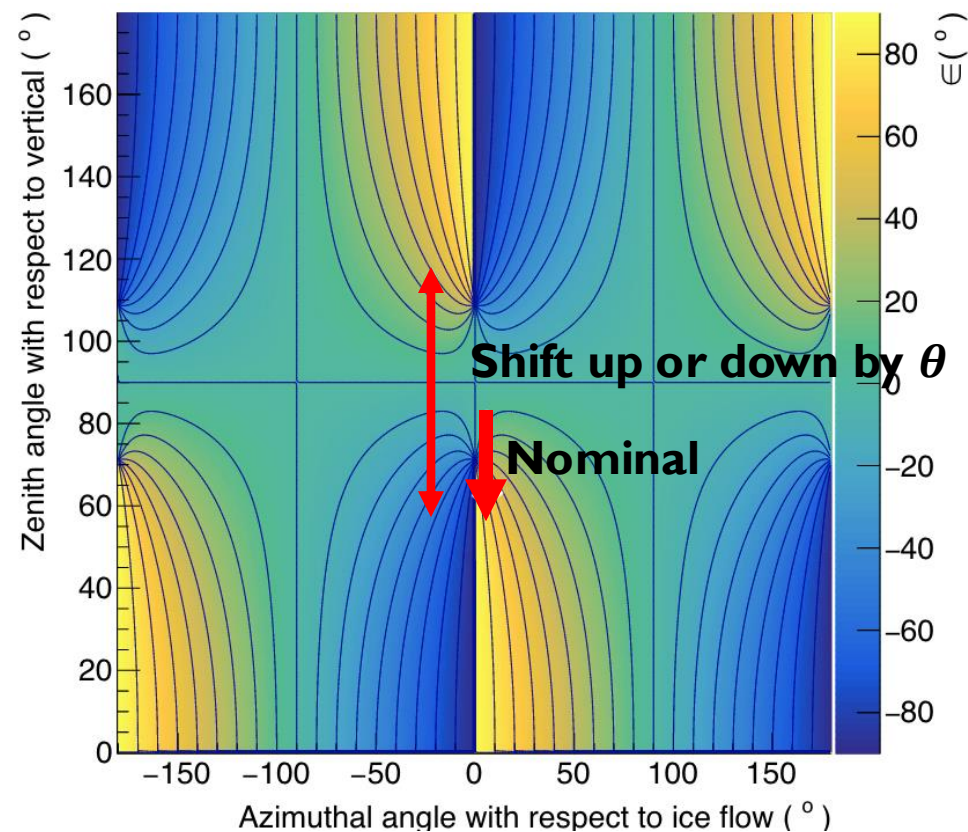
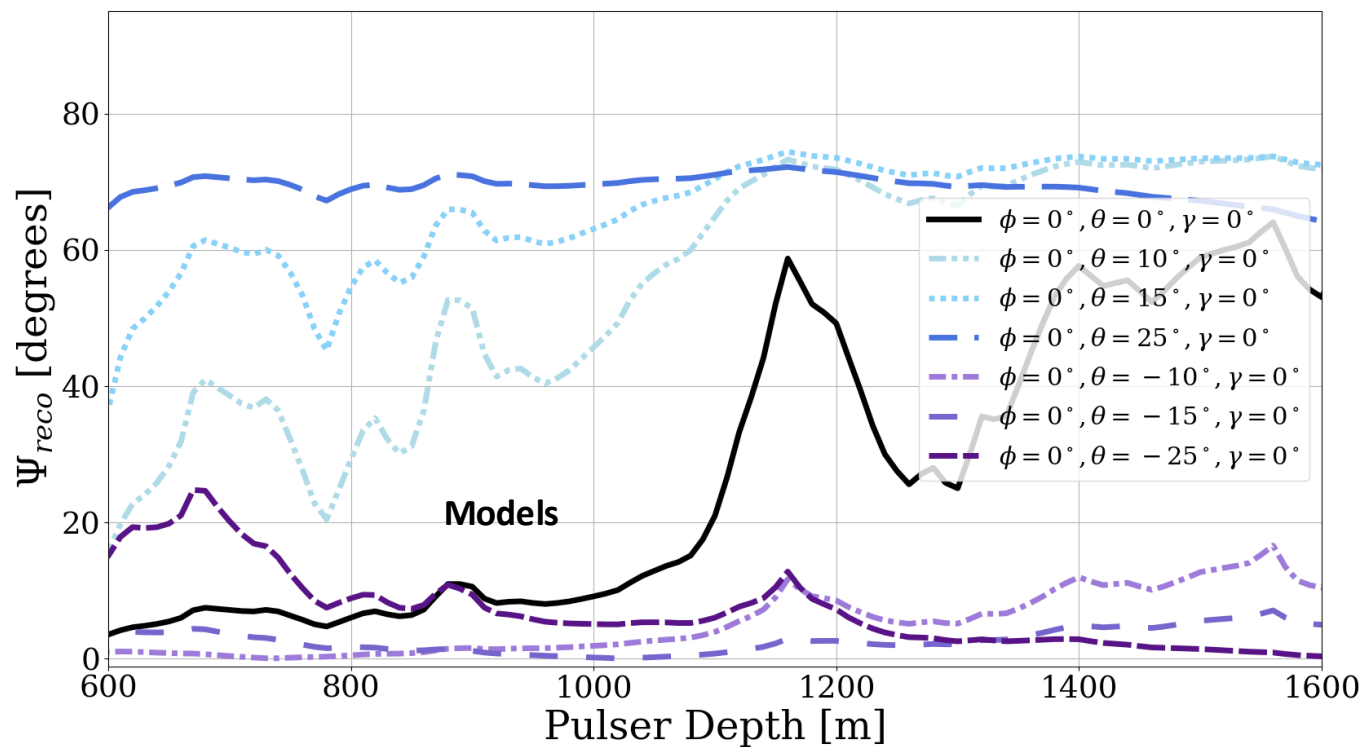
Rotation of the COF can have a large effect on predictions for polarization reconstruction

- Here we try reproducing the data's behavior with a simple model for cross-pol antenna response  $\delta$



# BACKUP 3: Systematic Uncertainties

Rotation of the COF can have a large effect on predictions for polarization reconstruction



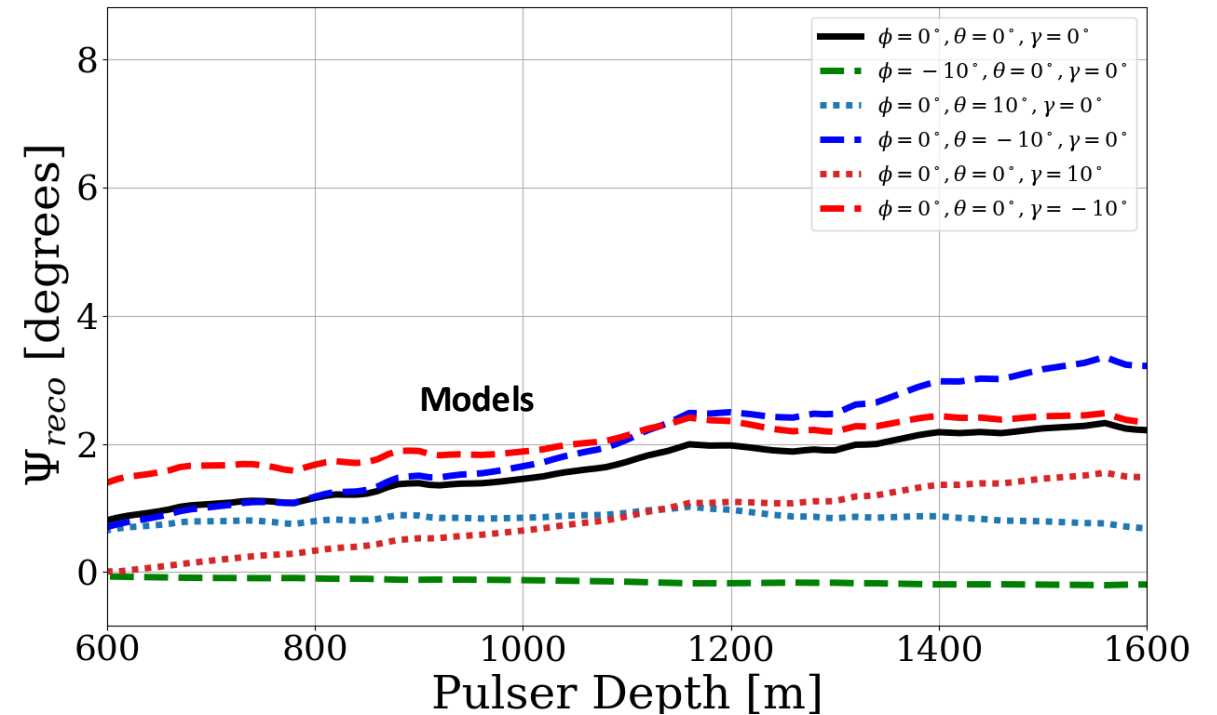
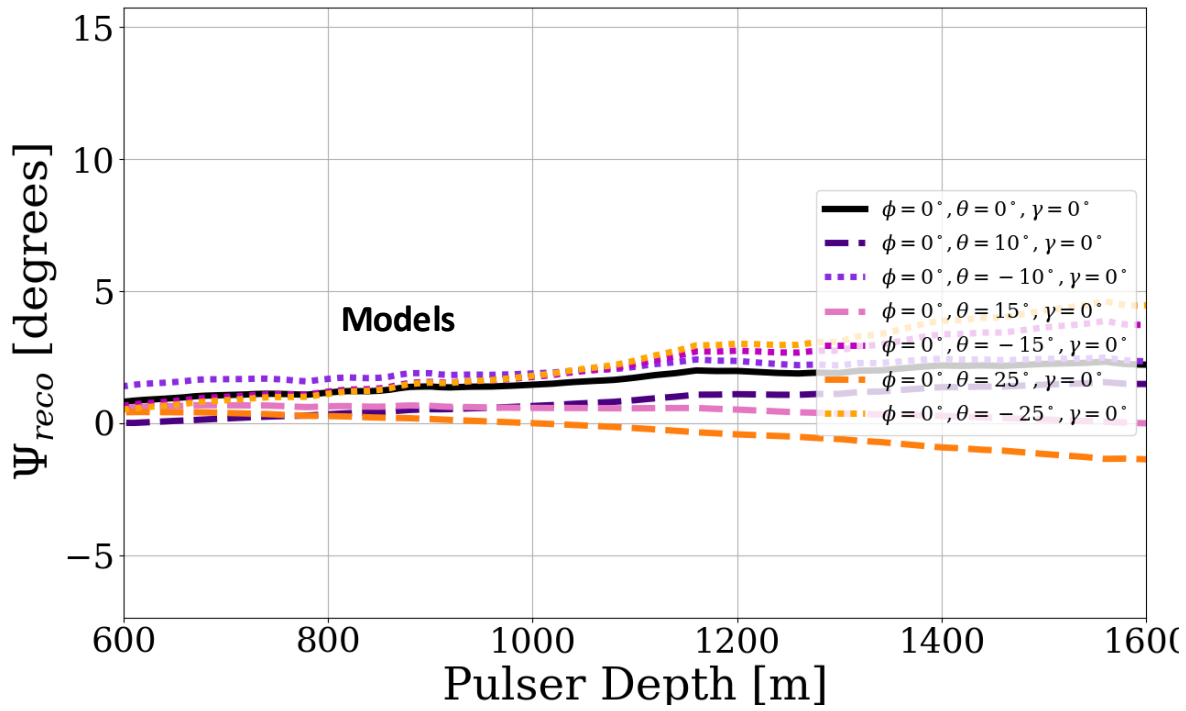
A. Connolly, Phys. Rev. D 105 (2022) 12, 123012



# BACKUP 4: Systematic Uncertainties

Rotation of the COF can have a large effect on predictions for polarization reconstruction

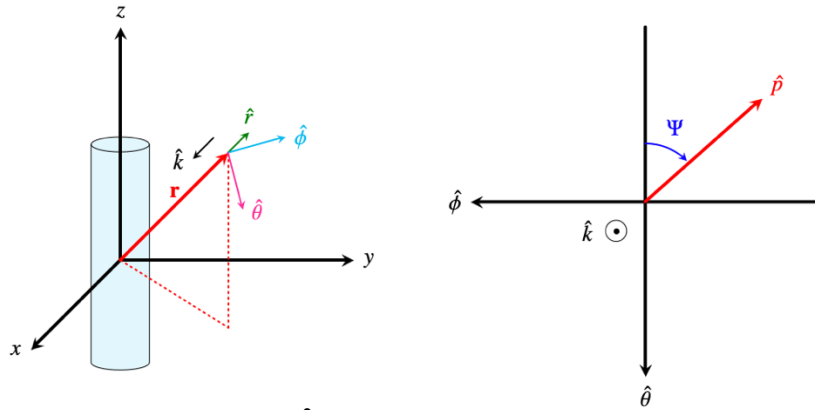
- We calculate the effects on **A2** by rotating the principal axes



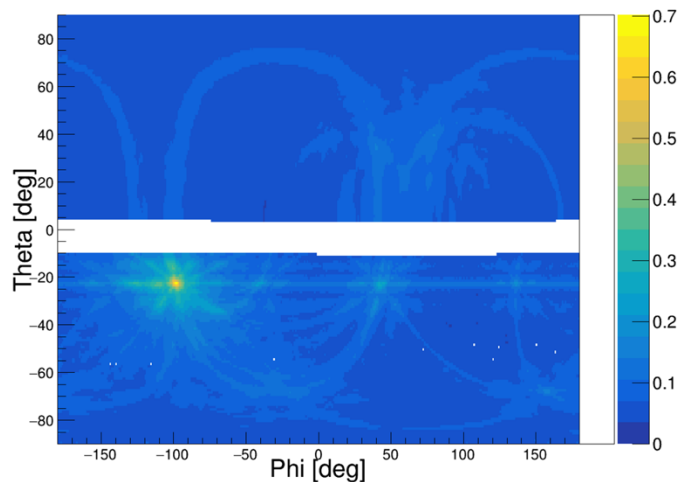
# BACKUP 5: Polarization Reconstruction

## Concepts for Polarization Reconstruction

### 1) Coordinates



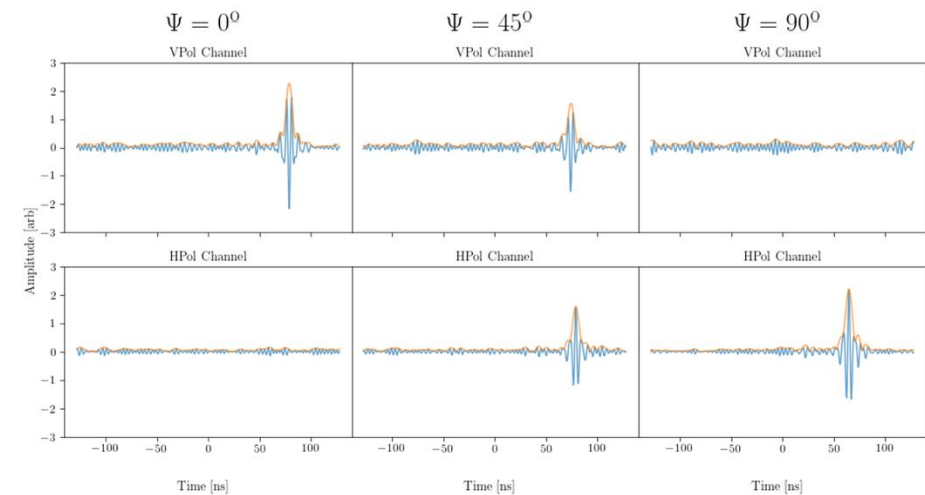
### 2) Vertex reconstruction



### 3) Deconvolution

$$\tilde{V}(\omega) = G_{\text{elec}} * G_{\text{ant}} * \tilde{E}(\omega) \rightarrow V(t)$$

### 4) Hilbert Peak



### 5) Polarization Reconstruction

$$\frac{V_{D,\text{HPol}}}{V_{D,\text{VPol}}} = \frac{P(\hat{p}, j=1) \cdot E(t)}{P(\hat{p}, j=0) \cdot E(t)} = \frac{\hat{p} \cdot \hat{\phi}}{\hat{p} \cdot \hat{\theta}} = \tan(\Psi)$$

# BACKUP 6: Polarization Reconstruction

Discrepancies between model and predictions for A4 may be due to the ray tracing algorithm used

