

# MARES: A MACROSCOPIC APPROACH TO THE RADAR ECHO SCATTER FROM HIGH-ENERGY PARTICLE CASCADES

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ON BEHALF OF THE RADAR ECHO TELESCOPE  
COLLABORATION

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CHICAGO



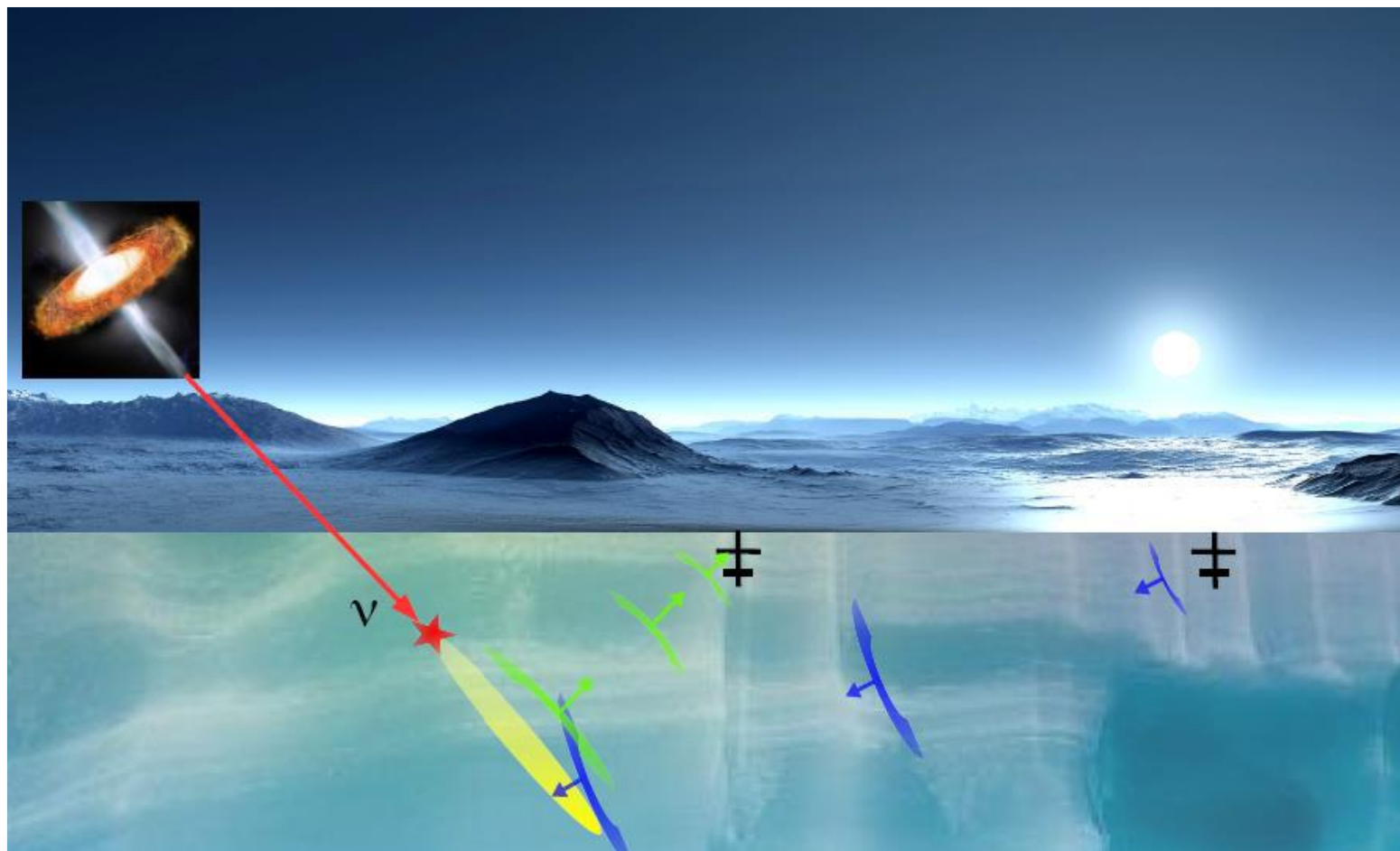
PennState



National  
Taiwan  
University

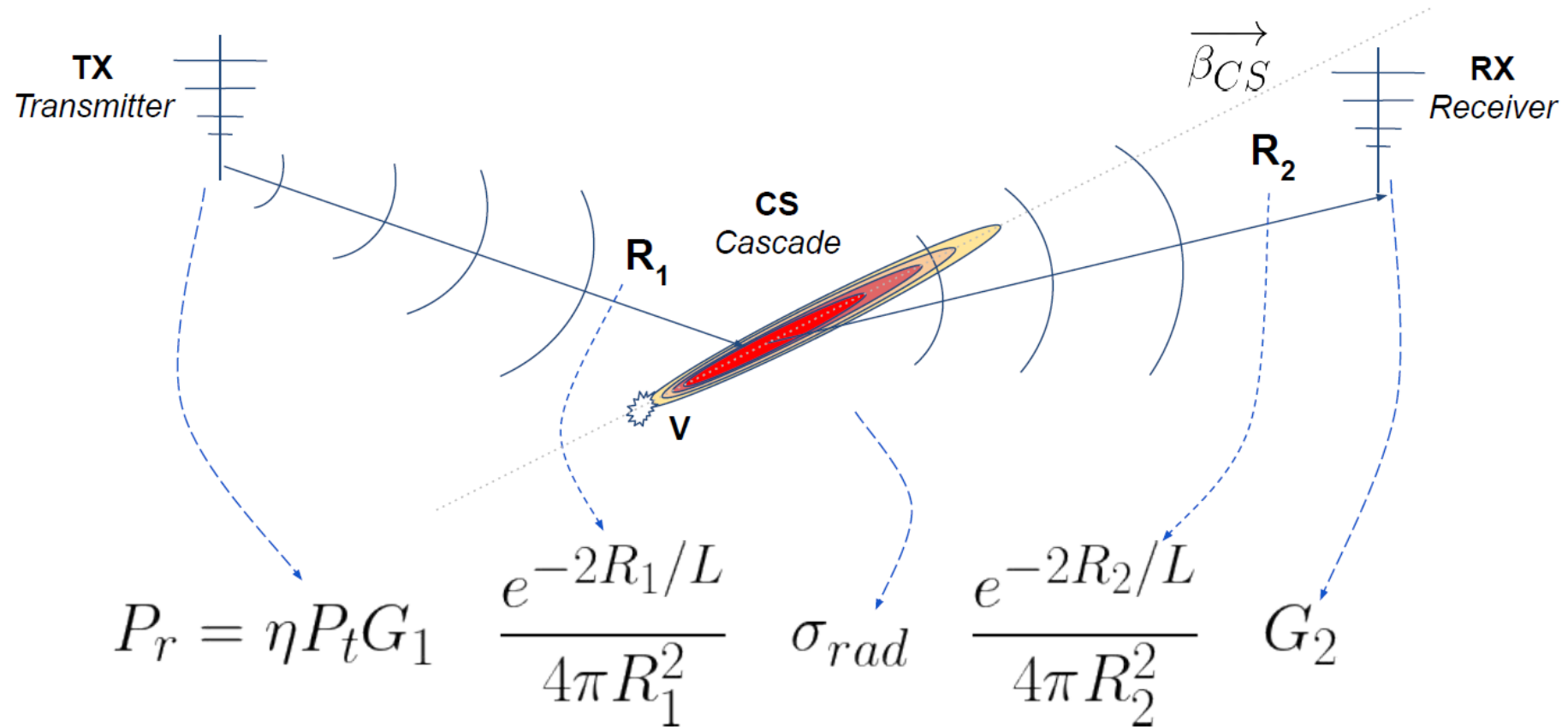
# RADAR DETECTION OF HIGH-ENERGY PARTICLE CASCADES IN ICE

## THE MAIN IDEA



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## THE RADAR RANGE EQUATION



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## THE CASCADE

(1) Relativistic cascade front

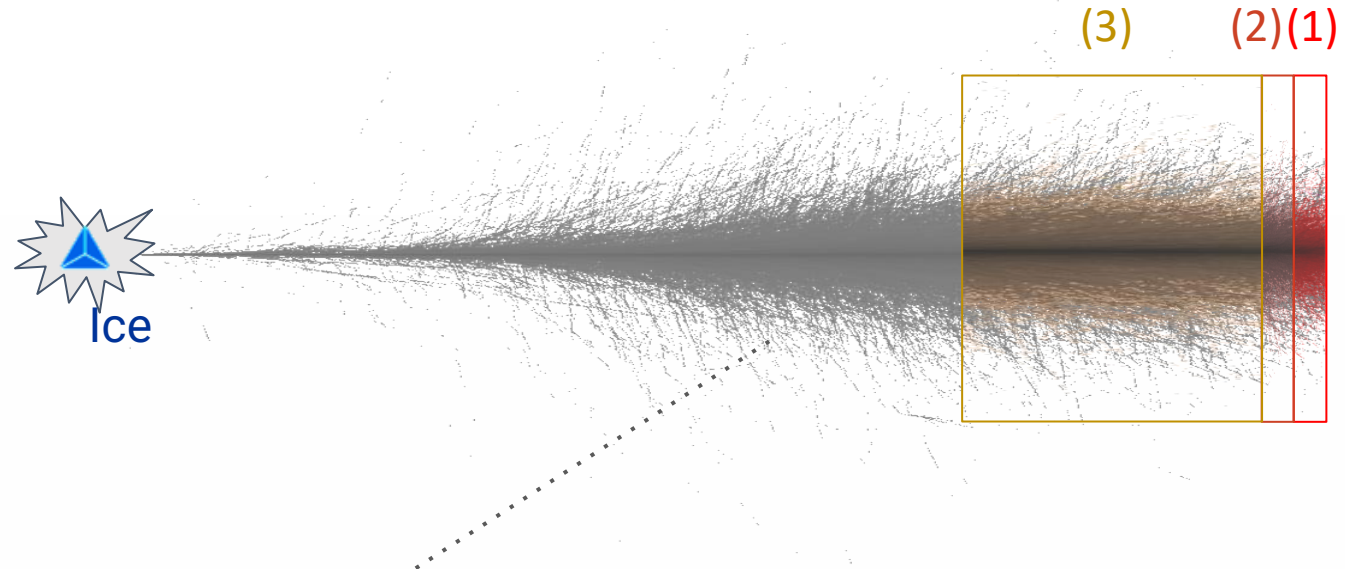
$$E_p > E_{front} > E_{rel} \sim O(1 \text{ MeV})$$

(2) Auger secondaries

$$E_{rel} > E_{trail} > E_{ion}$$

(3) Cascade trail

$\tau (e^- \text{ ionisation}) \sim O(10) \text{ ns}$ .  
Long-lived electron plasma

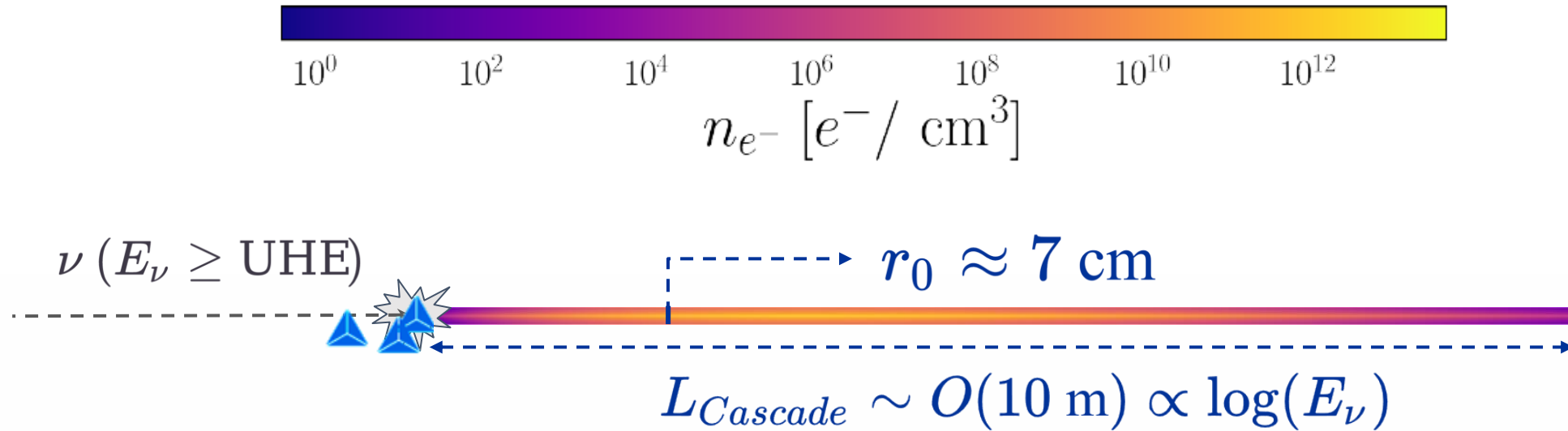


$$\max(n_{e^-}, Trail) \sim 10^{10} \left[ \frac{e^-}{\text{cm}^3} \right] \log \left( \frac{E_p}{10 \text{ PeV}} \right) \ll N_{Avogadro}$$

4

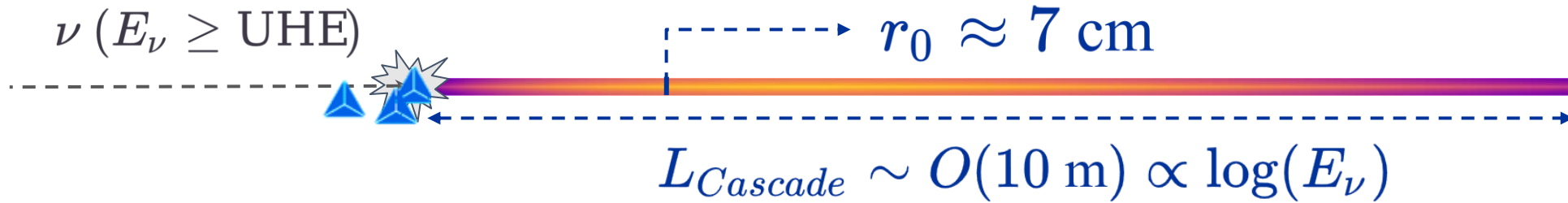
# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## MARES: THE CASCADE



$$\max(n_{e^-}, \text{Trail}) \sim 10^{10} \left[ \frac{e^-}{\text{cm}^3} \right] \log\left(\frac{E_p}{10 \text{ PeV}}\right) \ll N_{\text{Avogadro}}$$

## MARES: THE CASCADE SEGMENTATION



**Cascade shape very “line-like” → Allows integration along radial dimension and considering line-segments:**



**Take segments small enough to preserve coherence**

**MARES:**  
**arXiv:2310.06731**  
**Phys. Rev. D 109, 083012 (2024)**

## MARES: THE RADAR ECHO CROSS-SECTION

$$\left[ 6.65 \cdot 10^{-25} \text{ cm}^2 \right] \left[ 10^{-10} \rightarrow 10^{-14} \right] \left[ \frac{3}{2} \sin^2(\theta) \right]$$

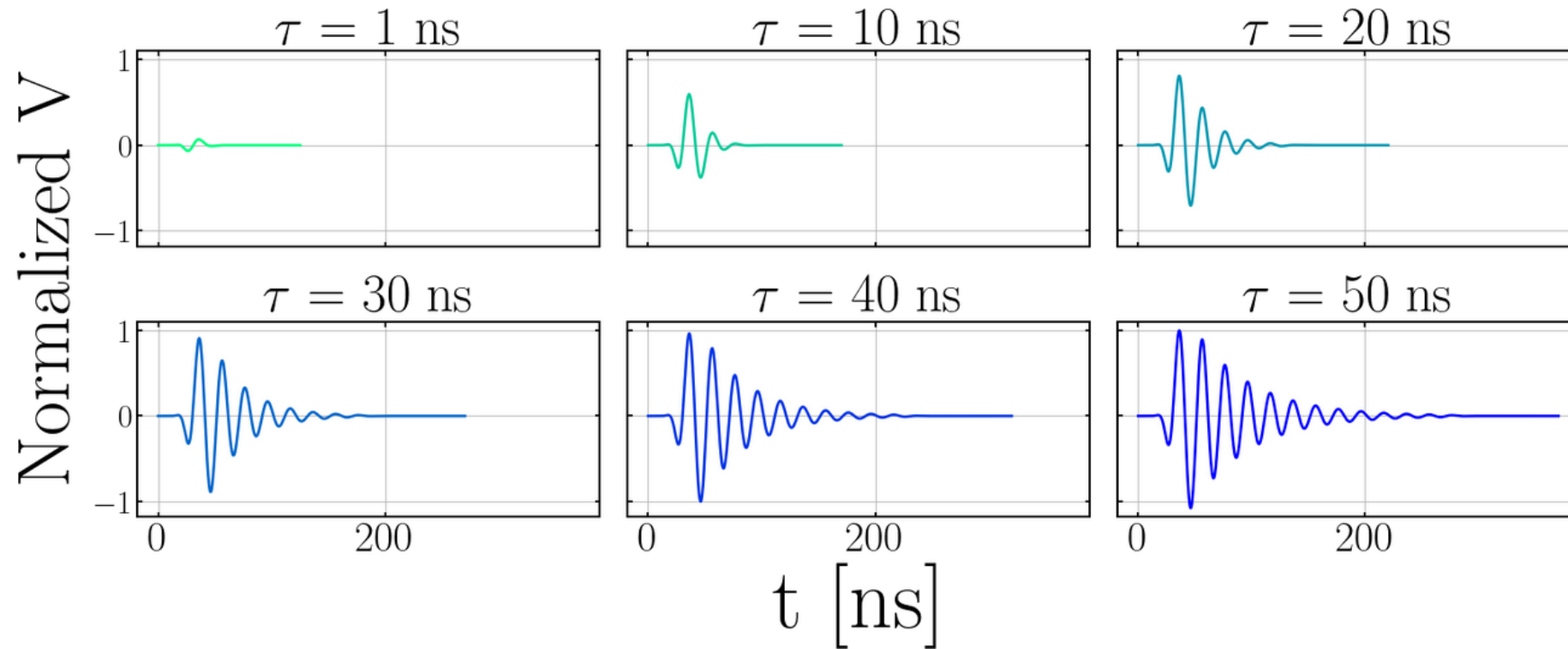
$$\sigma_{RCS,e^-} \simeq \sigma_{Thomson} \cdot \left( \frac{\omega}{\nu_c} \right)^2 \cdot G_{Hertz}$$

$$\sigma_{RCS,dV} = \sigma_{RCS,e^-} \cdot N_e^2 \cdot \mathcal{I} \cdot \left[ \Theta(t - t_0) e^{-2t/\tau_e} \right]_{t=t_{ret}}$$



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: LIFETIME

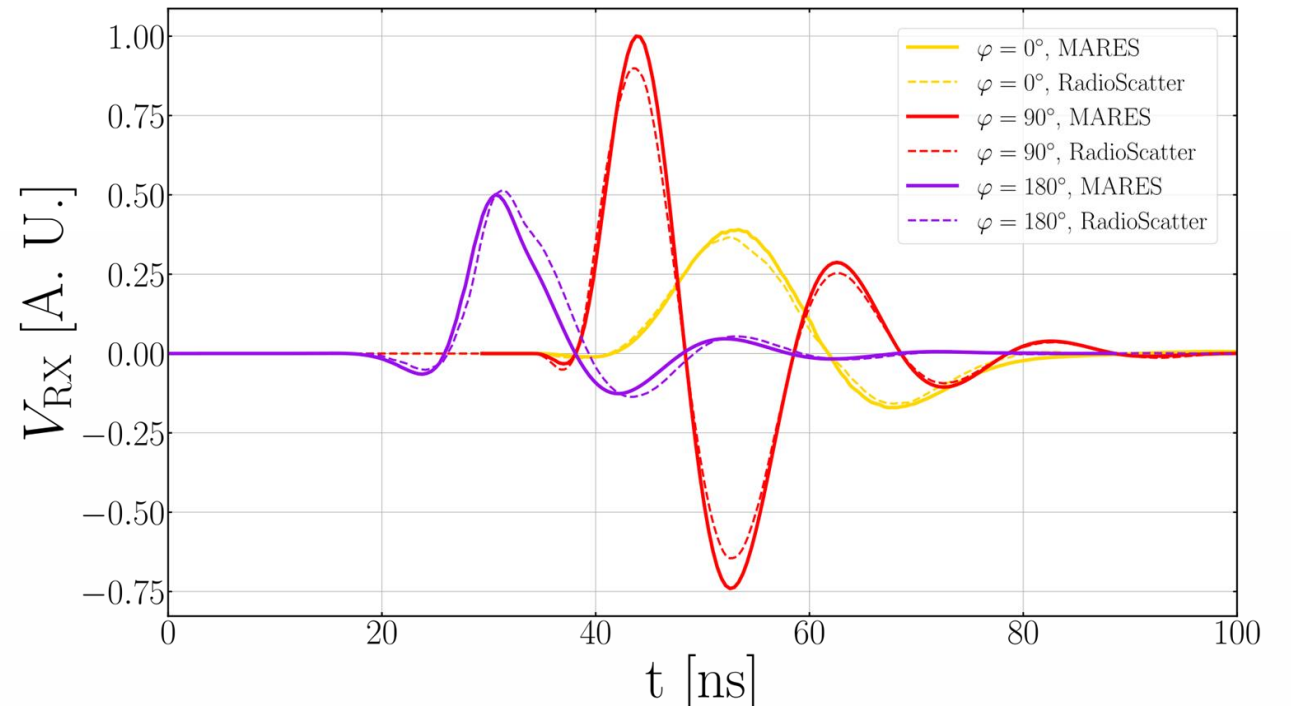
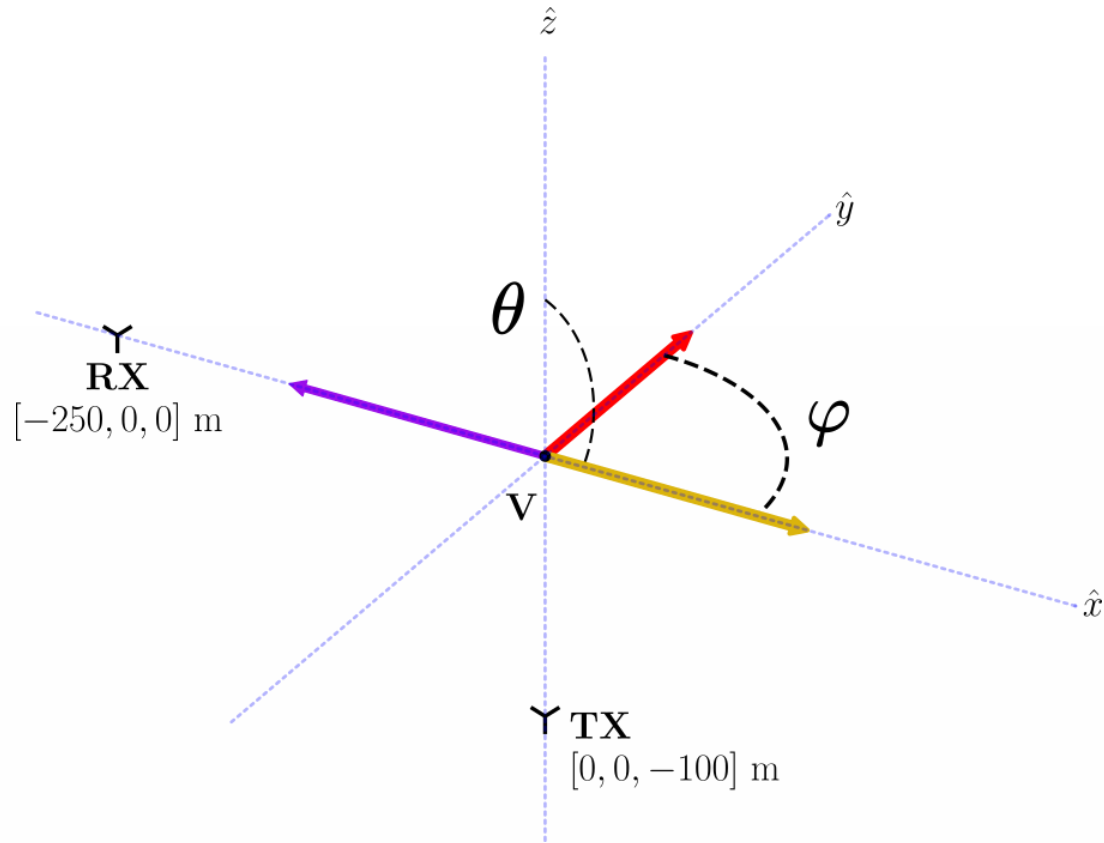


**MARES:**  
**arXiv:2310.06731**  
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# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: PULSE SHAPE



Excellent agreement between **RadioScatter + GEANT4** **Microscopic Monte-Carlo** simulation and **MARES** **Macroscopic deterministic** RET simulation codes

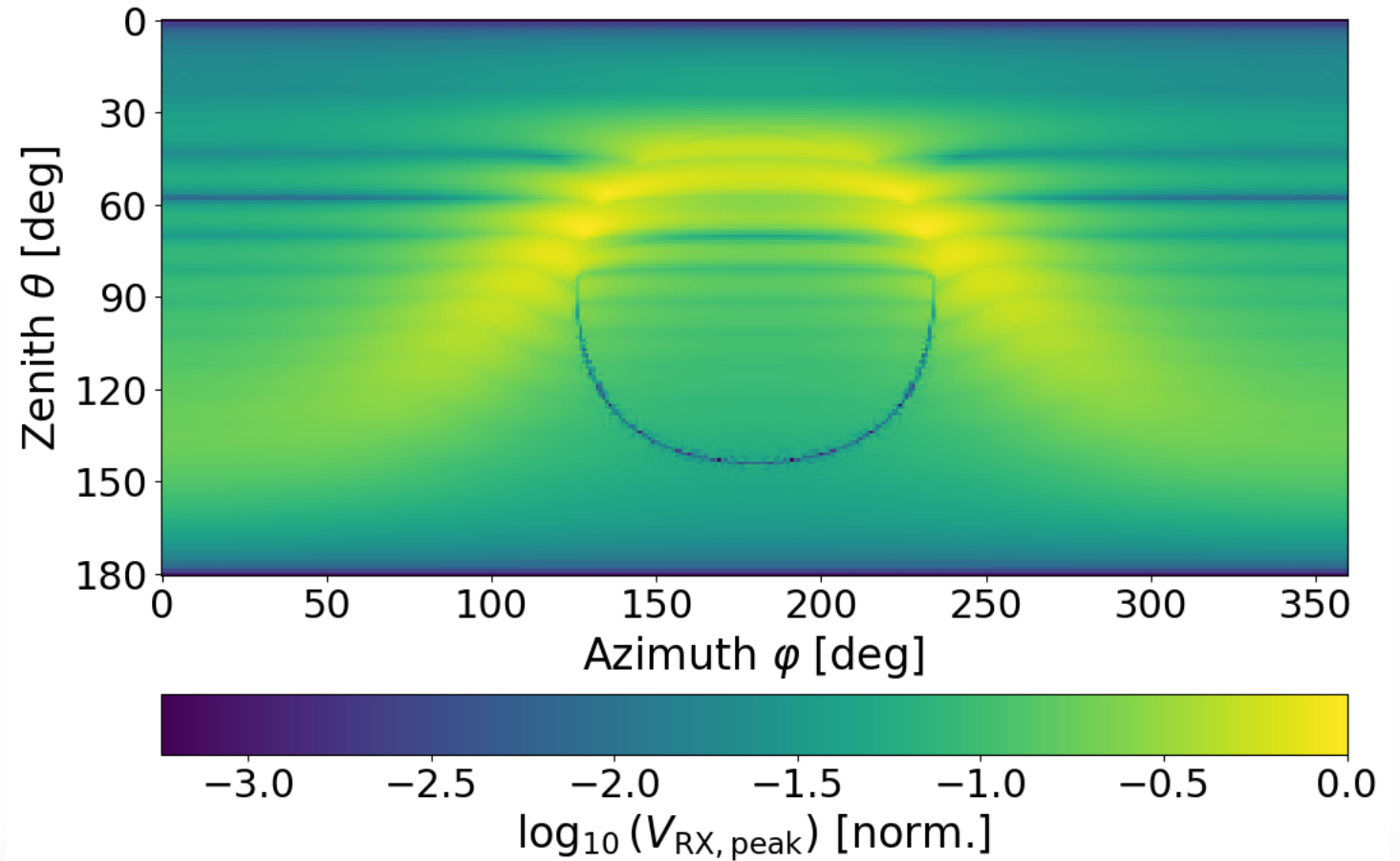
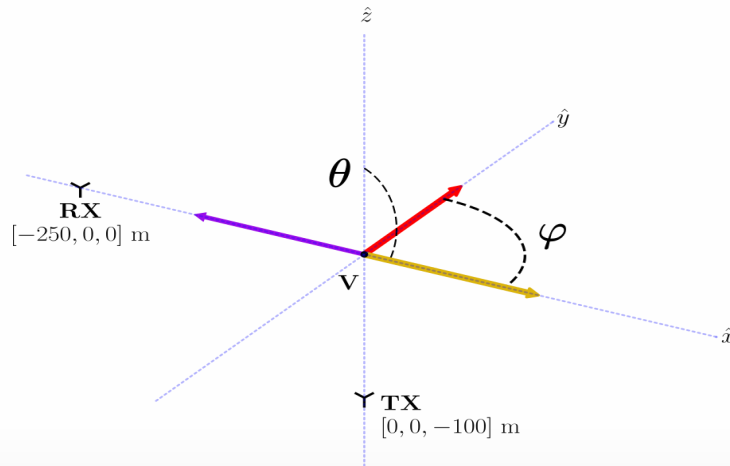
**RadioScatter:** arXiv:1710.02883 ; NIM-A 922 (2019) 161-170  
**MARES:** arXiv:2310.06731 ; Phys. Rev. D 109, 083012 (2024)

# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: INTENSITY

### Features:

- 1) Cherenkov-like effect
- 2) Diffraction bands
- 3) High-intensity swirl



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

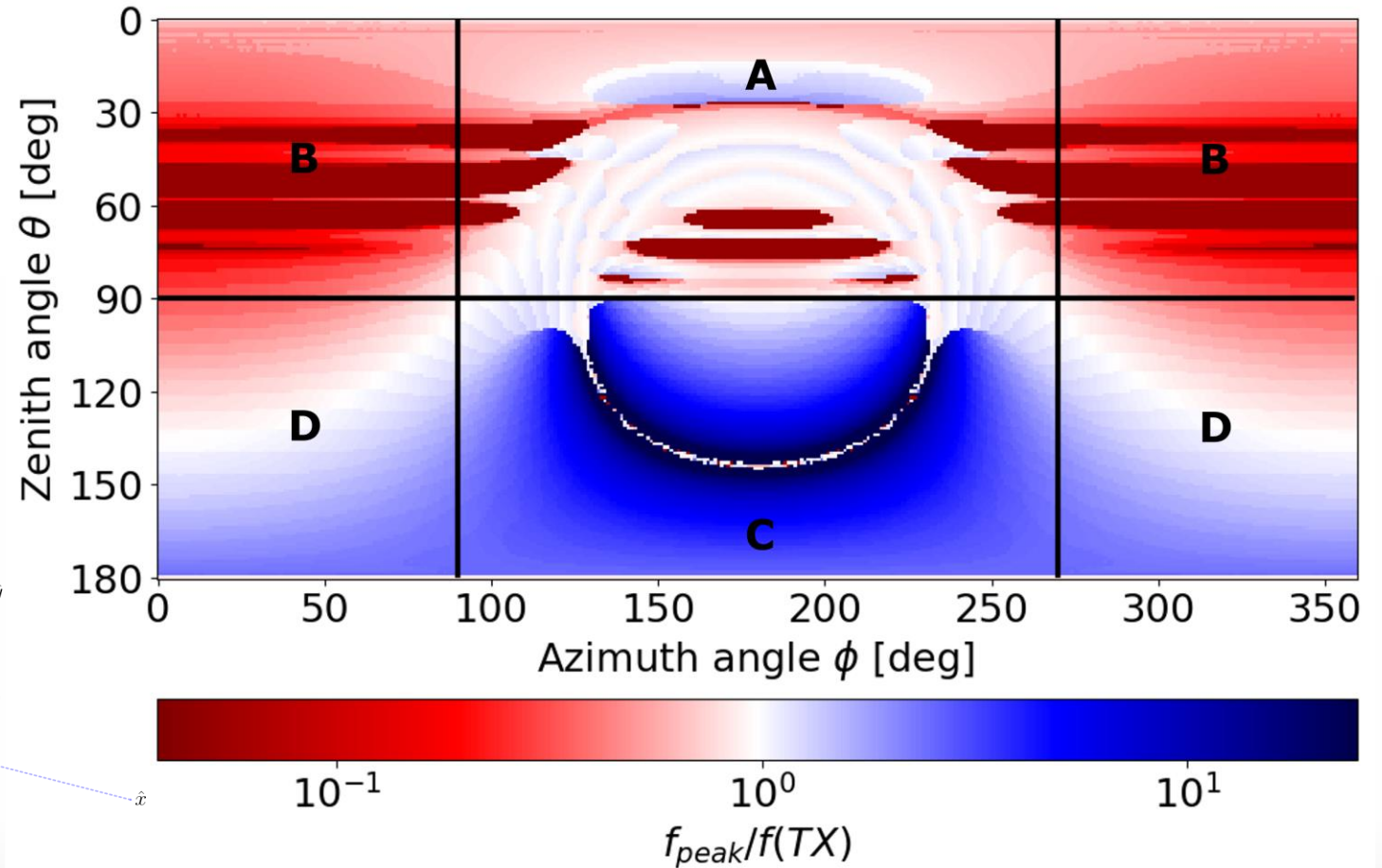
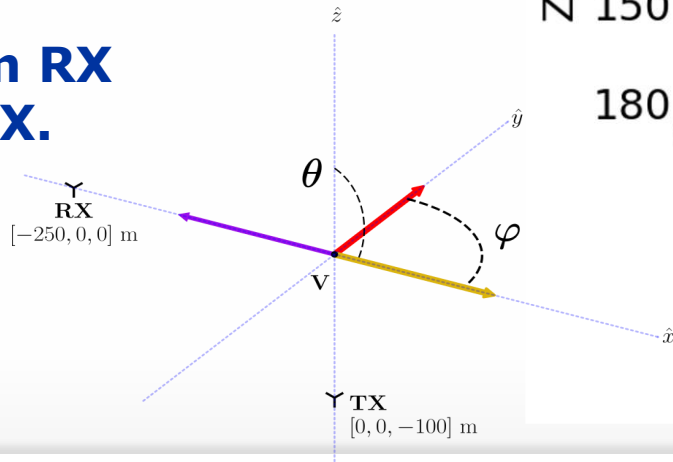
## SIGNAL PROPERTIES: FREQUENCY

**A:** Towards RX,  
Away from TX.

**B:** Away from RX  
Away from TX.

**C:** Towards RX  
Towards TX.

**D:** Away from RX  
Towards TX.



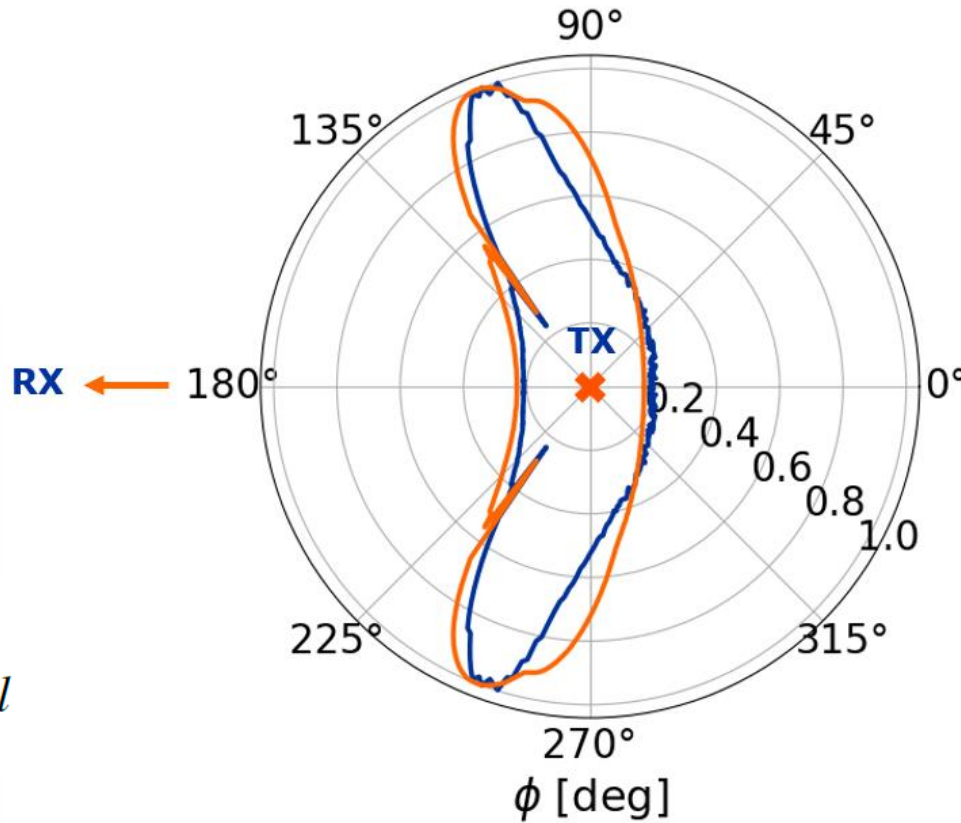
# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: PHASE ALIGNMENT

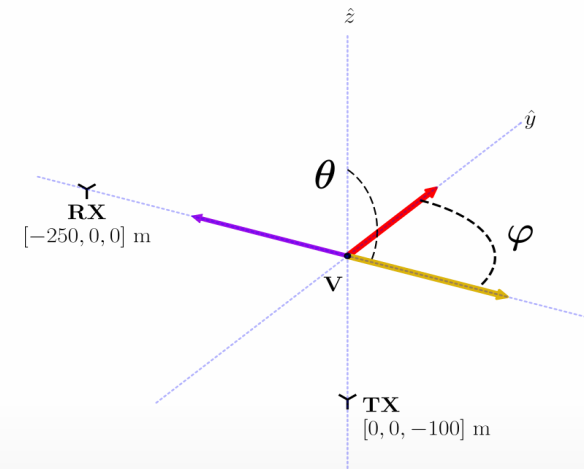
**Orange:** Simulation at fixed zenith angle of 90 degrees

**Blue:** Phase alignment measure:

$$C = \int \left( \cos(\varphi) \cdot \frac{n_{e^-}}{n_{max}} \right)_{norm} dl$$



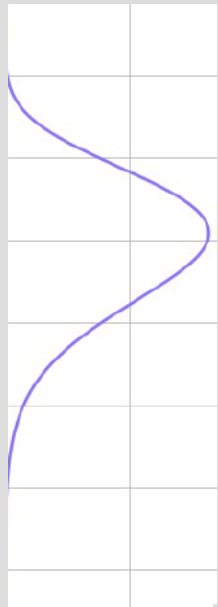
**PRELIMINARY**



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: PHASE ALIGNMENT

RET-CR geometry  
PRELIMINARY

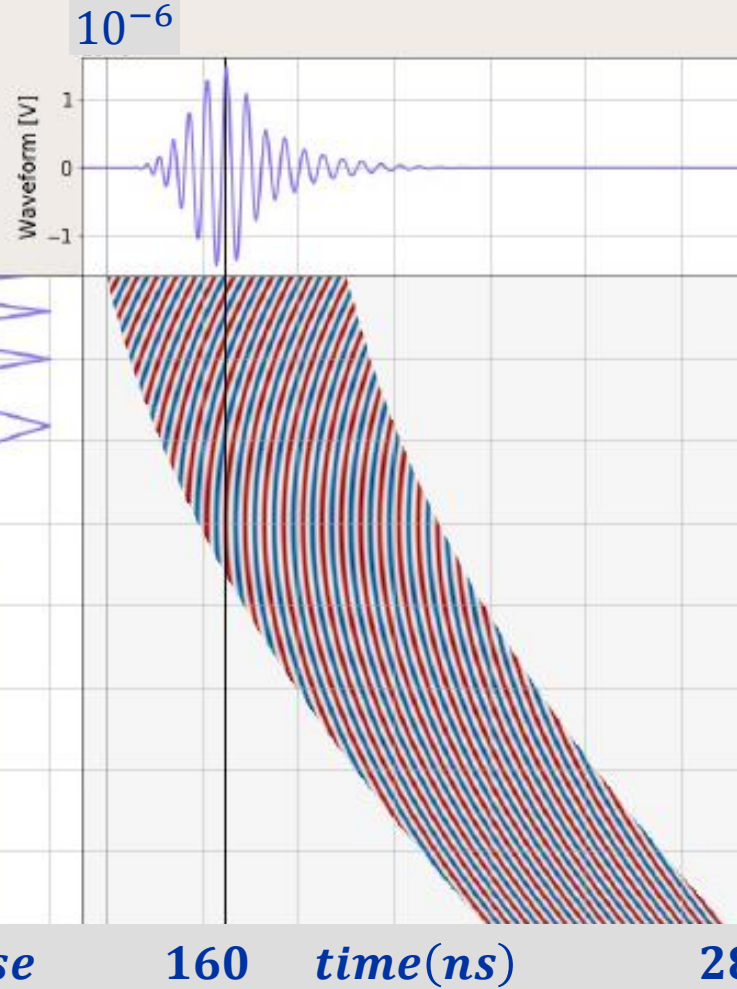


$N_e(10^{12})$

length(m)

0.0

20.0



Waveform [V]

$10^{-6}$

1

0

-1

phase

160

time(ns)

280

Phase /  $\pi$

1.0

0.8

0.6

0.4

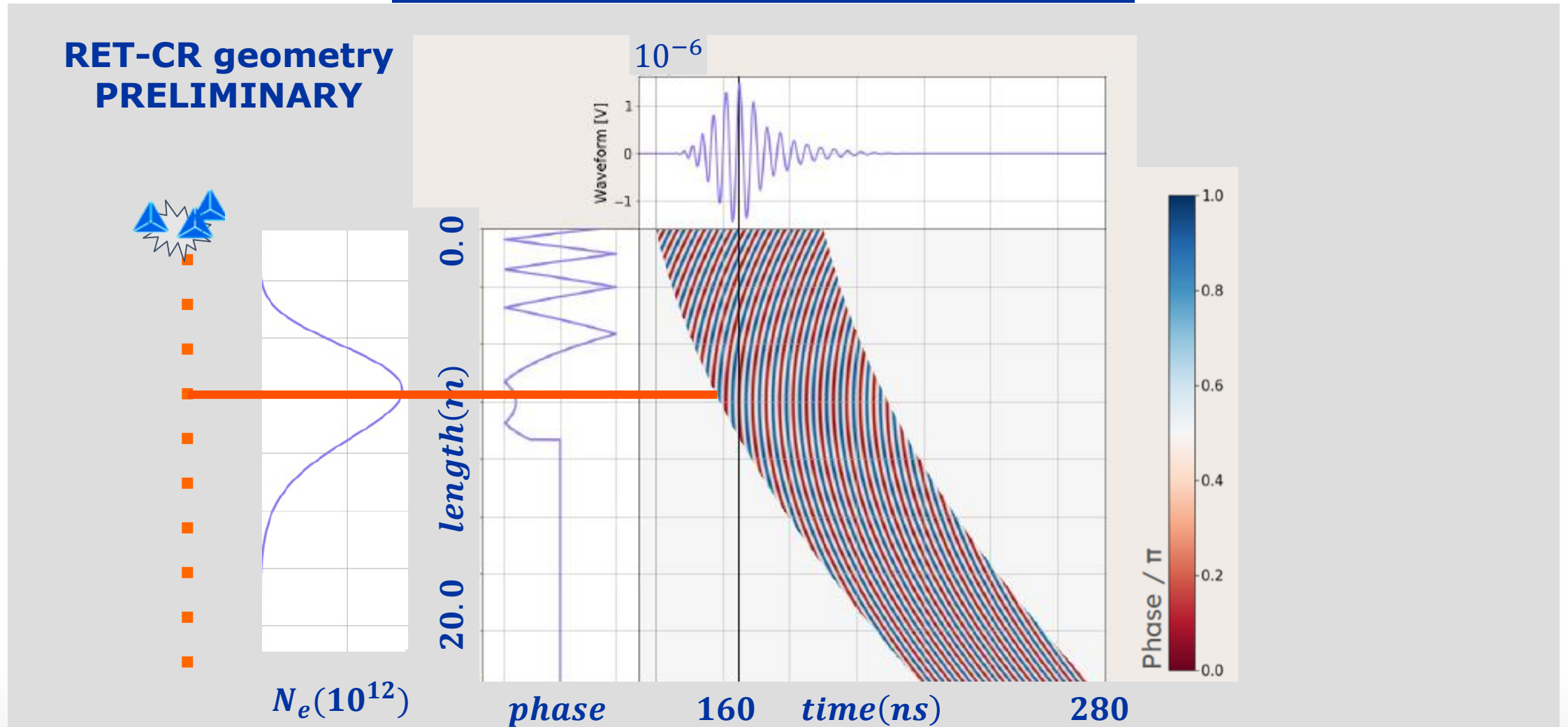
0.2

0.0



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

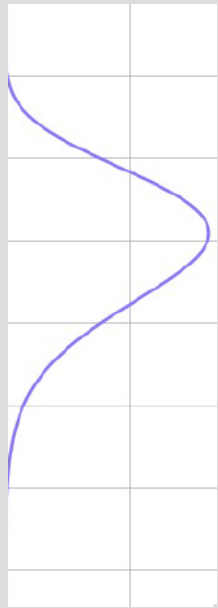
## SIGNAL PROPERTIES: PHASE ALIGNMENT



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: PHASE ALIGNMENT

RET-CR geometry  
PRELIMINARY

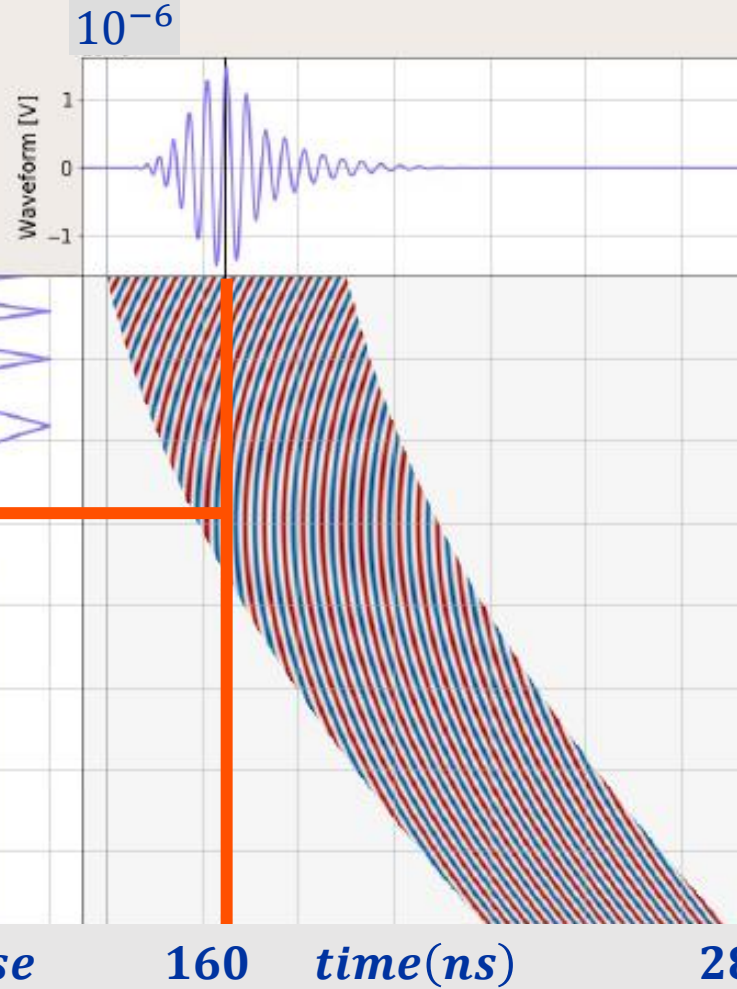


$N_e (10^{12})$

length(m)

0.0

20.0



$10^{-6}$

Waveform [V]

1

0

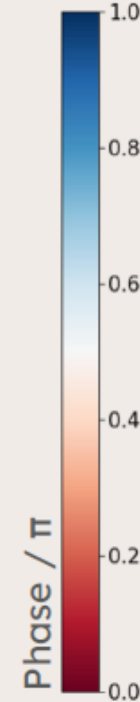
-1

phase

160

time(ns)

280



Phase /  $\pi$

1.0

0.8

0.6

0.4

0.2

0.0



# Thanks!!

[www.radarechotelescope.org](http://www.radarechotelescope.org)

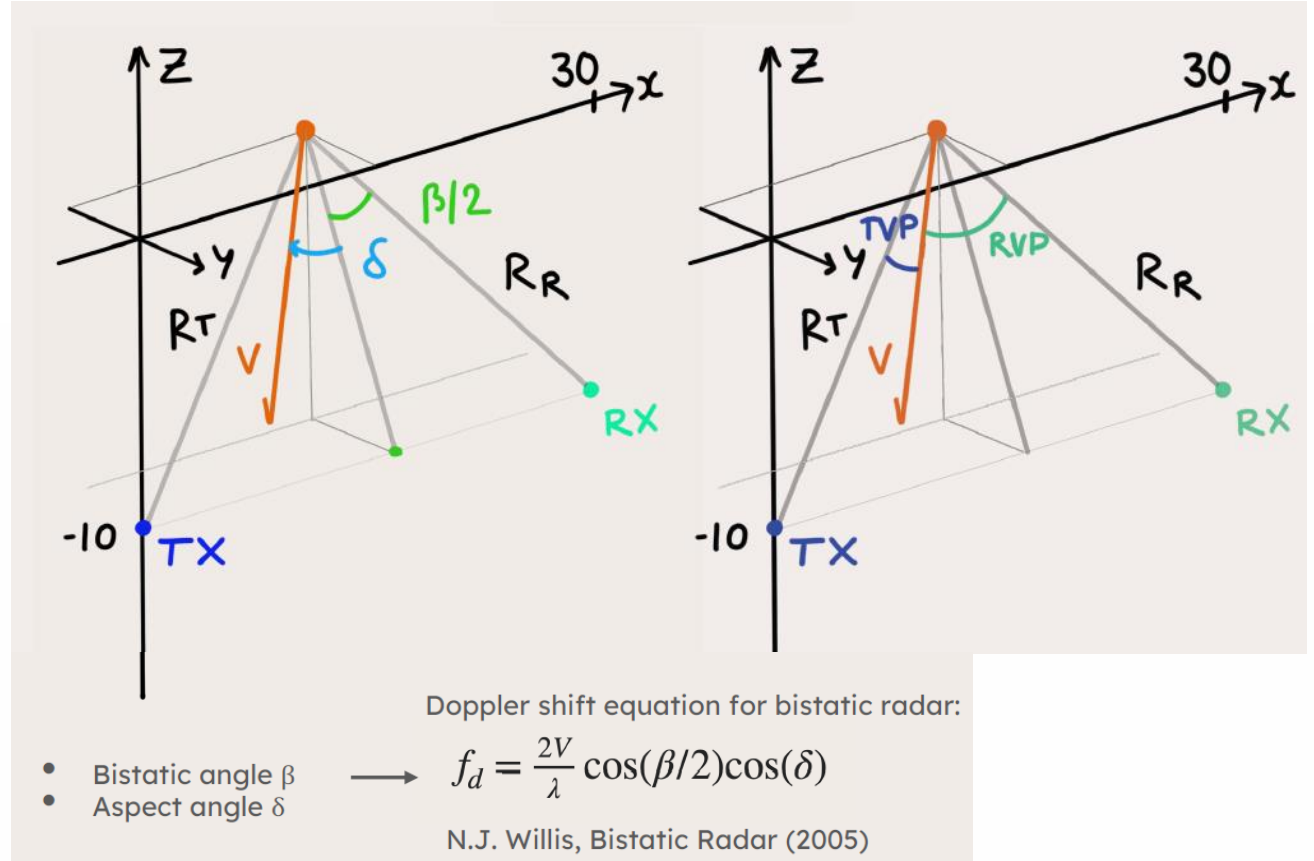
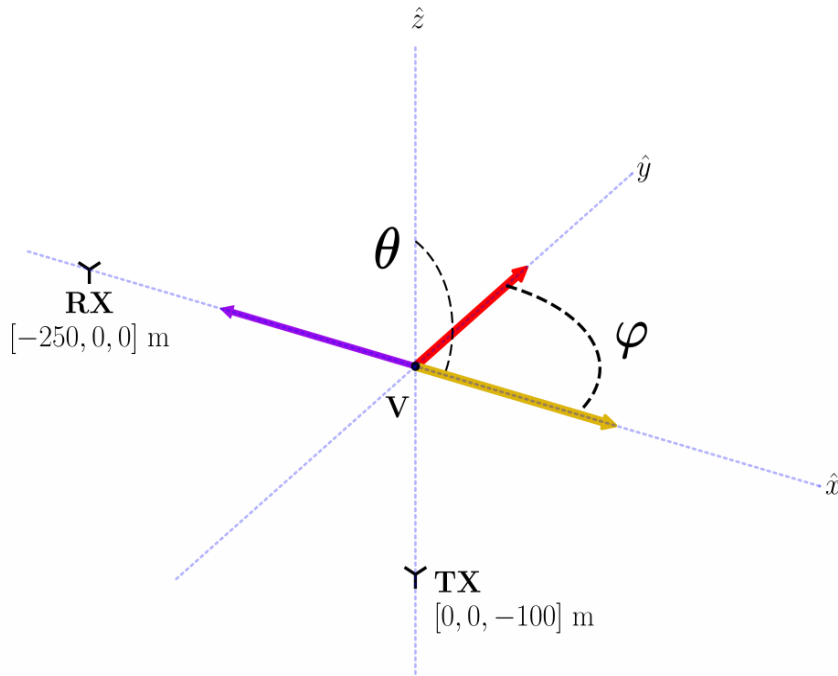


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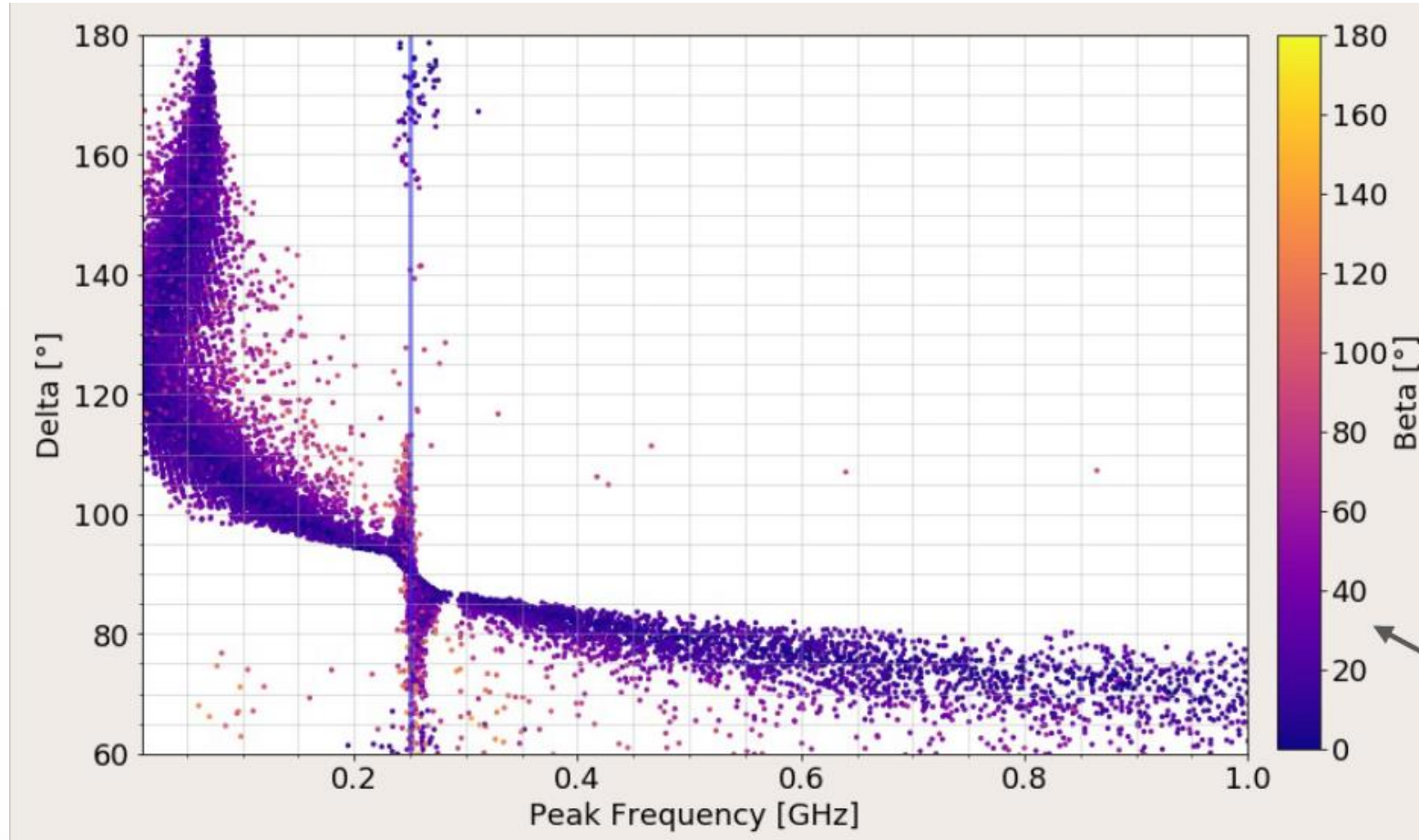
# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## COORDINATES



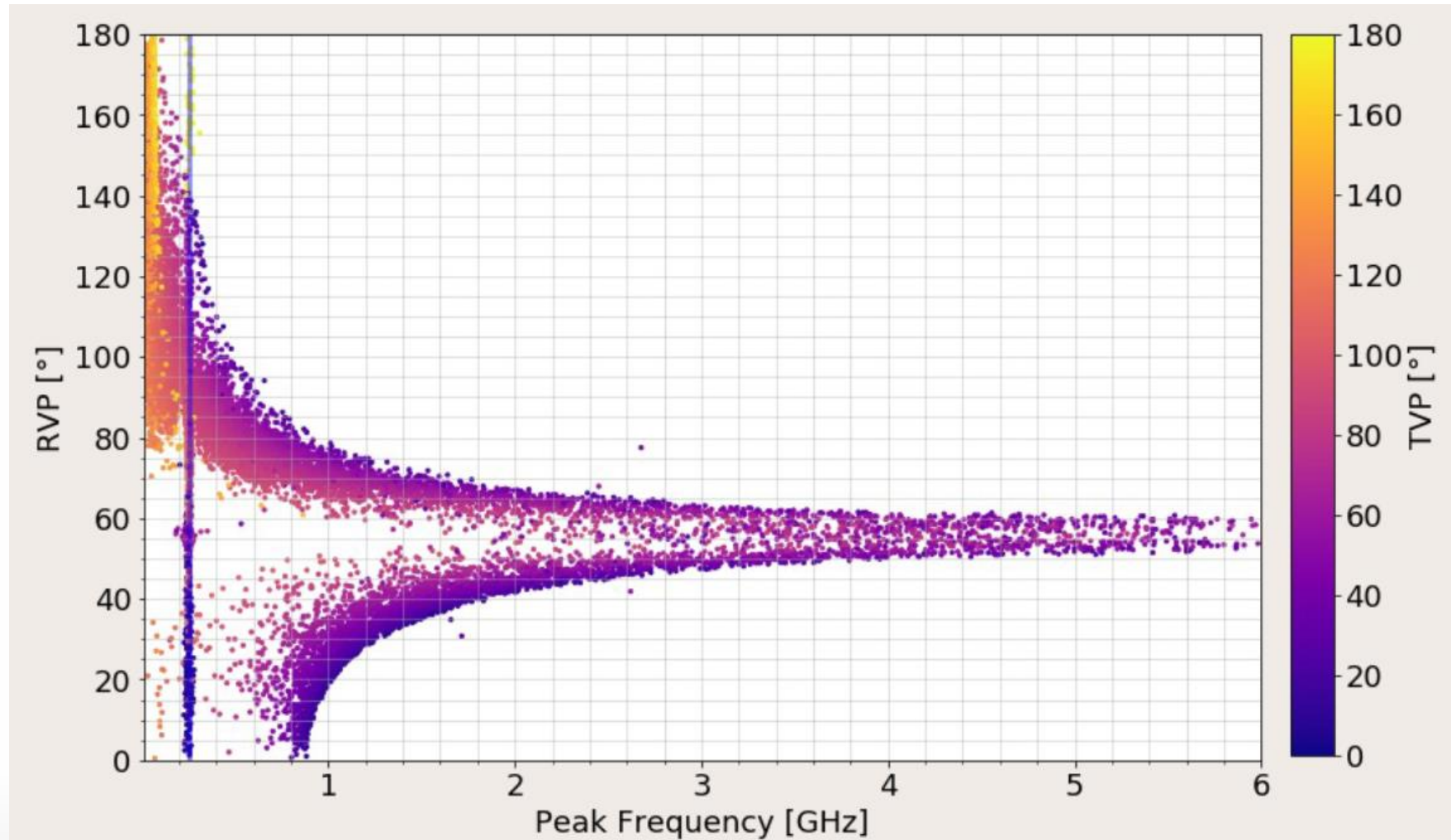
# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## COORDINATES



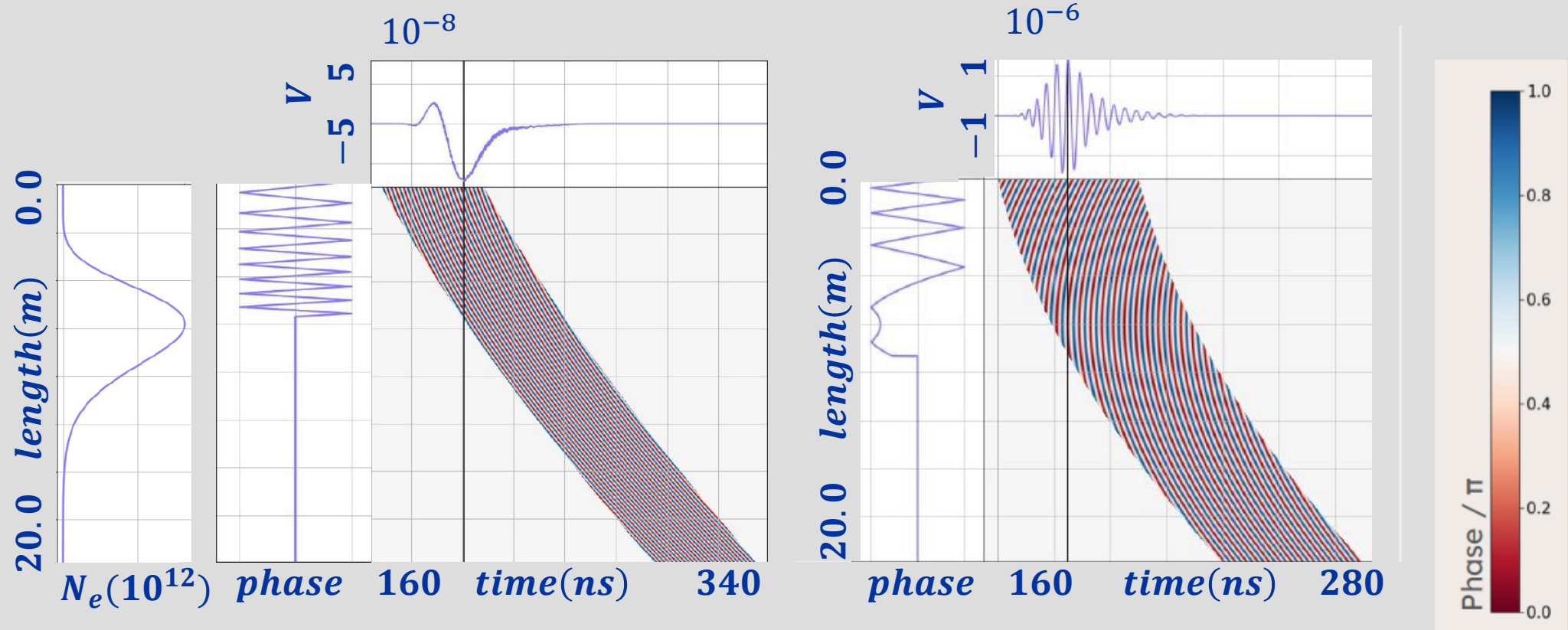
# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## COORDINATES



# MODELING AND UNDERSTANDING RADAR ECHOS FROM PARTICLE CASCADES

## SIGNAL PROPERTIES: PHASE ALIGNMENT



Phase coherence determines pulse strength

Dealignment away from high-intensity swirl

Alignment at high-intensity swirl