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Summary

Alongside upstream and downstream experiments in the cooling demonstrator, instrumentation along the beamline is necessary for measurement and tuning of the accelerator during operation. Beam instrumentation must non-destructively measure spatial distribution on the order of millimeters and bunch timing structure on the order of 10 picoseconds. However, a beam in the cooling demonstrator is expected to be very lowintensity, $\sim 10^5-10^6$ muons per bunch. We examine several conventional beam instrumentation methods and their limitations.

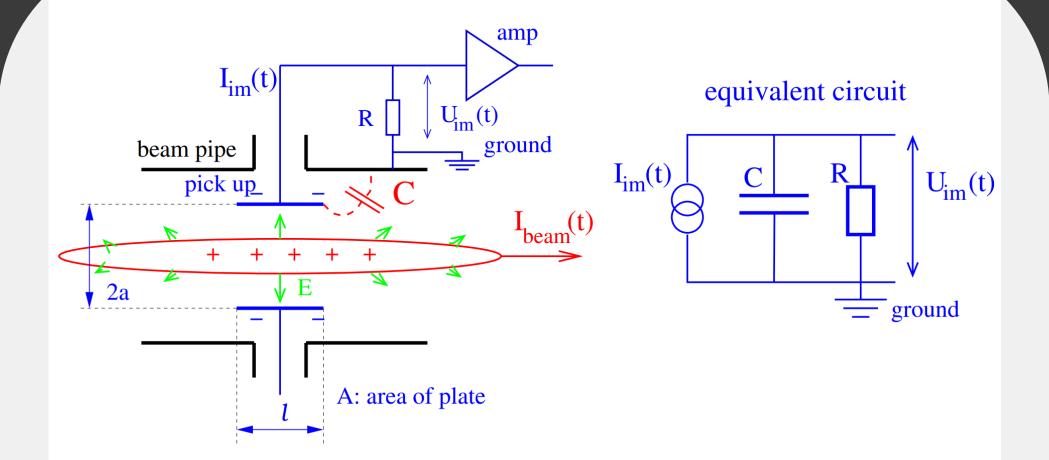


Fig. 1: Scheme of a BPM pick-up electrode and its equivalent circuit, from [1]. The capacitance C comes from the distance between the plate and the beam pipe, and the cable from the plate to an amplifier. The resistance R is largely the resistance of the amplifier. The circuit itself forms a high pass filter, and the coaxial cable that transmits the signal is a low pass filter.

Multi-Wire Monitors

Multi-wire monitors are a grid of thin wires, placed in the beamline to measure the beam profile.

- Poor SNR at intensities below 10⁷ particles/bunch
- Wires that are thin enough not to interfere significantly with the beam are liable to burn out

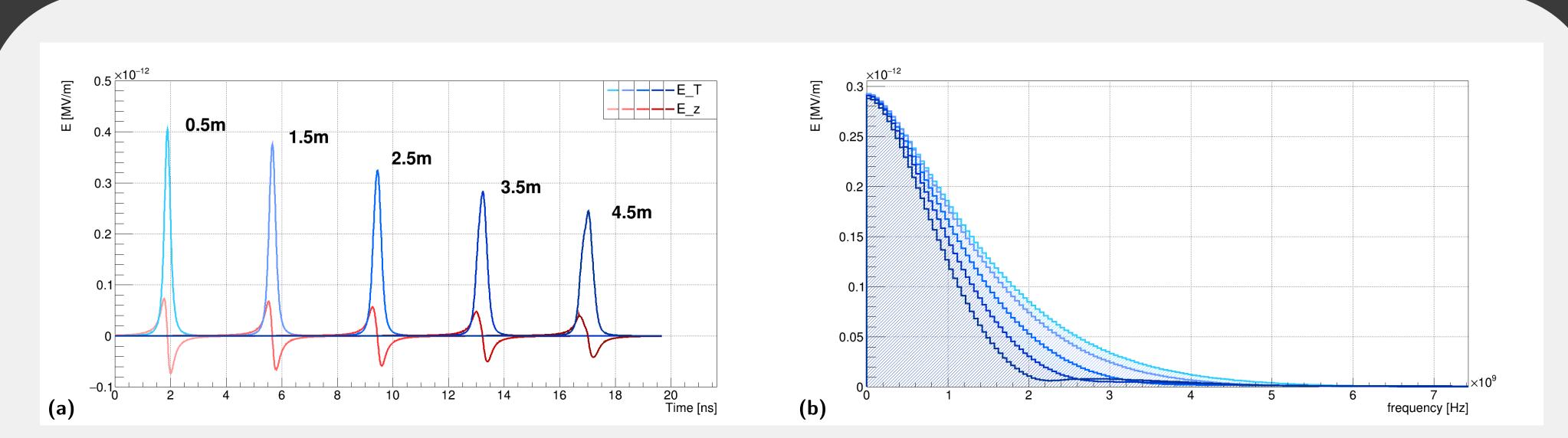


Figure 2: The E_{\perp} and E_{z} fields induced by a single bunch passing by, measured 1 mm away from the surface of the beam pipe. The pipe is aluminum and conductive, necessary to allow the calculation of fields in G4beamline collective mode. 1(a) shows E_{\perp} and E_{z} , measured 1 mm away from the inside wall of the beam pipe. 1(b) shows the FFT of E_{\perp} . At 6 GHz, the attenuation of a low loss RG58 coaxial cable is 1.532 dB/m ($\sim 30\%/m$) [4]. Parameters for the demonstrator bunch structure are from [2].

Parameters	Cooling Demonstrator	G4beamline simulation
Intensity	$\sim 10^5-10^6~\mu/ ext{bunch}$	$10^6~\mu +$
Momentum	$200\pm10 \text{MeV}$	$200\pm10{ m MeV}$
Bunch length	~ 100 ps	$\sigma_{\rm z} = 12.72 \ {\rm mm} \ (1/2 \ \beta c \cdot 100 \ {\rm ps})$
Beam spot size	10-20 mm RMS + dispersion	$\sigma_{x} = \sigma_{y} = 5 \text{ mm}$
Beam pipe radius	81.6 mm	81.6 mm

Beam Position Monitors

Beam position monitors measure image charges induced by beam on the instrument's conducting surfaces as it passes.

- Resolutions \sim pA $\sim 10^{19} * 10^{-12} = 10^7$ particles. Still measurable with amplifiers, low noise background.
- The capacitive pickup BPM in Fig. 1 can be described by a simple circuit with capacitance C, resistance R. Modeling the passing bunch as a current source I_{beam} , the impedance Z is

$$\frac{1}{Z} = \frac{1}{R} + i\omega C \iff Z = \frac{R}{1 + i\omega RC}$$

and thus the transfer function U_{im} is

$$U_{im} = \frac{R}{1 + i\omega RC} \cdot I_{im} = \frac{1}{\beta c} \frac{1}{C} \frac{A}{2\pi a} \frac{i\omega RC}{1 + i\omega RC} I_{beam} \equiv Z_t(\omega, \beta) \cdot I_{beam}$$

• This equation has the form of a first order high pass filter with cutoff frequency $f_{\rm cut}=\omega_{
m cut}/2\pi=(2\pi RC)^{-1}$.

Laser Wire Scanners

A cooling demonstrator bunch simulated in G4beamline, rendered in Blender.

A tightly focused laser beam is scanned across a (e^+/e^-) beam. An image of the beam is reconstructed from Compton-scattered photons.

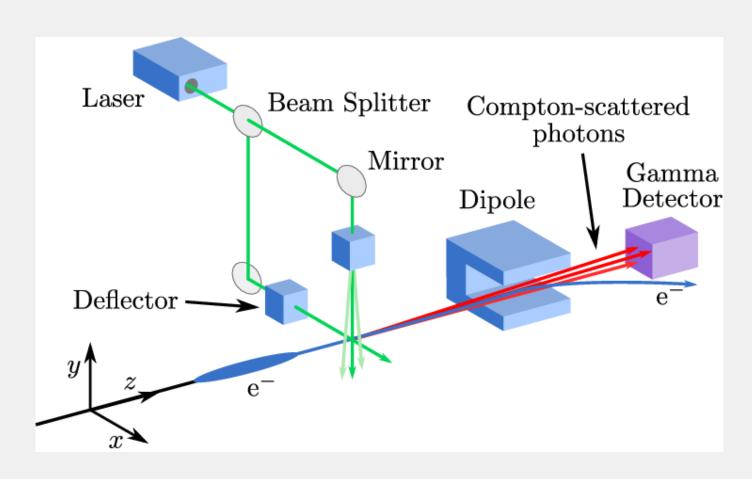


Figure 3: A conceptual schematic of a laser wire scanner, from [3]. Such scanners are used at SLAC, PETRA-III in DESY, and the ATF-II at KEK, and have been proposed for the ILC and CLIC.

- Compton scattering: $v_0 h \approx m_e c^2$; for electrons, requires hard x-ray lasers.
- For muons, Compton scattering requires ν 200x higher, so a scanner would rely on Thomson scattering (ν_0 h << m_e c²).
- Thomson cross section is $(m_{\mu}/m_e)^2 \approx 40,000 x$ smaller for muons than electrons, $\sim 1.5 E-5$ barn.
- A demonstrator bunch, using parameters of laser wire scanners at PETRA and ATF, would Thomson scatter
 5 photons; could increase laser light intensity.
- Differentiate photons scattered by the muon bunch and by background electrons, background photons.

References

[1] P. Forck, P. Kowina, and D. Liakin. "Beam Position Monitors". In: Synchrotron Radiation News 1 (Jan. 2008).

[2] P. B. Jurj, C. Rogers, and I. Ortega. "Beam parameters and functional specifications for Demonstrator and Muon Collider instrumentation". In: Proceedings of the 17th BIFT - Muon Collider. Jan. 2025.

[3] L. J. Nevay, R. Walczak, and L. Corner. "High power fiber laser system for a high repetition rate laserwire". In: Phys. Rev. ST Accel. Beams 17(7 July 2014), p. 072801.

[4] RFI Technology Solutions: Coaxial Attenuation Chart. 2021.